



SPATIAL ANALYSIS OF COMPLEX BIOLOGICAL TISSUES  
FROM SINGLE CELL GENE EXPRESSION DATA

Clustering and visualizing functional tissues in *Platynereis dumerilii*'s brain

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This dissertation is submitted for the degree of Doctor of Philosophy



## DECLARATION

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This thesis:

- is my own work and contains nothing which is the outcome of work done in collaboration with others, except where specified in the text;
- is not substantially the same as any that I have submitted for a degree or diploma or other qualification at any other university; and
- does not exceed the prescribed limit of 60,000 words.

*Cambridge, November 2014*

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Jean-Baptiste Olivier  
Georges Pettit





## ABSTRACT

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This thesis revolves around single cell gene expression datasets in the context of the marine annelid or ragworm *Platynereis dumerilii*, an important model organism, part of the lophotrochozoan taxon of the bilaterians. After describing single cell expression data acquired from Wholemount in Situ Hybridization assays for 169 genes as well as single cell RNA-seq data for 72 cells in the developing brain 48 hours post fertilization of *P. dumerilii*, I discuss the main advantages of both methods and propose a back-mapping method to generate a spatially referenced data set of whole transcriptomes at the single cell level.

As the spatial characteristics of the data are crucial to the work presented in this thesis, I also present a 3-dimensional visualization tool that facilitates greatly the upstream and downstream analysis of such datasets. The rest of the thesis focuses on answering the question of identifying cell types from single cell expression data, that is clustering cells together in a meaningful, functional way. Specifically, to take advantage of both the cells' location within the tissue and the pattern of gene expression within each cell, I propose a statistical method based on Hidden Markov random fields to cluster the cells according to their gene expression patterns as well as their spatial localization. The method is validated by a simulation study and the quality of the results are compared to those of other clustering methods. Finally the method's output when applied to the *P. dumerilii* in-situ hybridization dataset are biologically validated and functional hypotheses about putative unstudied regions of the brain and their function are formulated.



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## Part I

### CELL TYPES AND SINGLE CELLS, A VERY SPATIAL RELATIONSHIP



## INTRODUCTION

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### 1.1 BIOLOGICAL CONTEXT AND GENERAL QUESTIONS

The work presented in this thesis revolves around several key biological concepts such as *tissue*, *cell type*, *spatial coherency* and *gene expression*. In the Introduction, I first give an overview of the model organism central to the work presented in this thesis, *Platynereis dumerilii*, and then define the main biological questions addressed throughout this work.

The global goal of this thesis is to study single cell gene expression while taking into account the spatial context of each cell. My main contribution is the development of a method that demonstrates that taking into account the spatial information improves the clustering of single cells into functional tissues.

#### 1.1.1 *Platynereis dumerilii*, an ideal organism for studying brain evolution

##### 1.1.1.1 General description

*Platynereis dumerilii* is a marine annelid of the class Polychaeta, which has been established as one of the main marine animal models in the fields of evolutionary and developmental biology as well as ecology, toxicology and neurobiology [54, 118, 48, 33, 39, 40].

*P. dumerilii* populates shallow (no more than 3m deep) ocean floors around the world. It is commonly found in the Mediterranean sea, the north Atlantic coast of Europe as well as in the shallow seas surrounding Sri Lanka, Java and the Philippines. Eggs, embryos and larvae are roughly 160µm long while the adults can measure up to 6cm in length.

There are several reasons why *P. dumerilii* has been chosen as a model by numerous laboratories. As a member of the bilaterians *P. dumerilii* has a defined bilateral symmetry. It belongs to the lophotrochozoan taxon of the bilaterians as opposed to most of the well estab-



(a) Larval form of *P. dumerilii*. Image: MPI for Developmental Biology. (b) Adult *P. dumerilii*. Image: Arendt group, EMBL

Figure 1: *Platynereis dumerilii*'s larva and adult forms.

lished model animals which either belong to the ecdysozoans (*Caenorhabditis elegans*, *Drosophila melanogaster*) or the deuterostomes (mouse, human). *P. dumerilii*, as one of the only lophotrochozoan models is needed in order to use comparative approaches for studying the full range of bilaterians [40].

*P. dumerilii* also exhibits an exceptionally slow evolving nature and it has even been described as a “living fossil” for that reason [40]. Consequently, the numerous ancestral developmental characteristics of *P. dumerilii* partly reflect the common ancestor of all bilaterians. An interesting example described in [29, 119] is the conserved molecular topography of the genes responsible for the development of the central nervous system between *P. dumerilii* and all vertebrates. This slow evolving nature makes *P. dumerilii* a better comparison with vertebrates than fast evolving species like *Drosophila* and nematodes where derived features can obscure evolutionary signal [40, 3].

From a practical experimental perspective, model organisms are chosen for several characteristics that make them easy to use in the laboratory. These characteristics include, but are not limited to, the size of the animal, the conditions required for the organism to develop, gestation and development time as well as the ease with which a new generation can be produced.

In this regard *P. dumerilii* is nearly an ideal animal. Even in their adult form, they are relatively small, they can easily be kept and bred in captivity producing offspring throughout the year [39]. Further-

more, the behavioural characteristics of *P. dumerilii*'s mating ritual have been well studied and can be reproduced on demand in the laboratory. The “nuptial dance” happens on the water surface. Males and females respectively release the sperm and eggs synchronously. This activity is synchronized by pheromones released into the water [134]. Over 2000 individuals can be produced within a single batch. Every new individual will undergo embryonic then larval development before reaching *P. dumerilii*'s adult form.

#### 1.1.1.2 Larval development

Similarly to the other polychaetes, the larval development of *P. dumerilii* can be decomposed into three main anatomical stages, as detailed in [50]: the trochophore, the metotrochophore and the nectochaete. The trochophore is spherical and moves thanks to an equatorial belt of ciliated cells as well as an apical organ displaying a ciliary tuft [104, 90] as seen in Figure 1a and schematically in Figure 2. The metotrochophore stage is characterized by the development of a slightly elongated segmented trunk compared to that of the trochophore [47]. The next developmental stage is referred to as the nectochaete larvae which resembles the adult (figure 1b) in many traits, especially with parapodial appendages used for swimming and crawling [47].

Aside from this purely anatomical description, an additional staging system exists and has become the norm for current studies. The development is measured in *hours post fertilization* (hpf) at 18°C.

A key factor making *P. dumerilii* such an interesting model to work with is the fact that after fertilization, the  $\approx 2000$  larva will start developing at the exact same time, in a synchronous fashion. Furthermore, the larval development of *P. dumerilii* follows a very stereotypical pattern with little variation from one individual to the other; this is true even between batches provided the temperature is kept constant [39, 33]. An illustration of this synchronous development is shown in Figure 3. This is a very important feature as it allows biologists to repeat experiments on several individuals at a very close developmental stage even if they are from different batches.

## Late trochophore : 48hpf

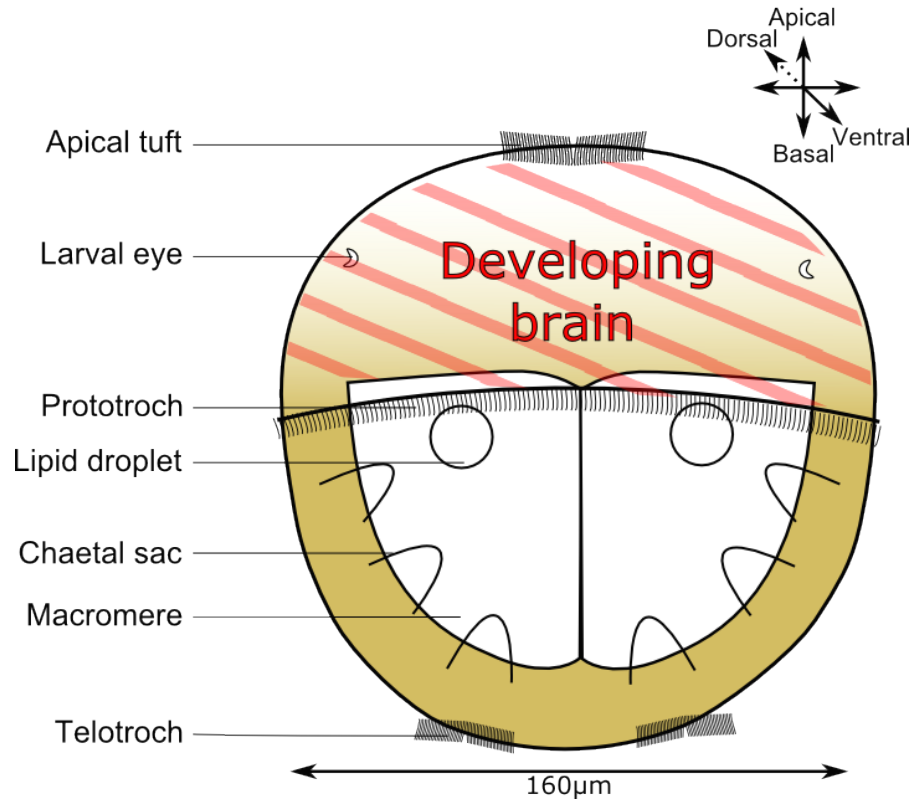


Figure 2: *Platynereis dumerilii*'s larva development at 48hpf (late trochophore). Red stripes indicate the area that forms the developing brain of the larvae.

#### 1.1.1.3 *Platynereis*' nervous development until 48hpf

Describing the entire development of *P. dumerilii* does not fall within the scope of this thesis. Indeed, I will only be interested in the brain of *P. dumerilii*'s larvae at 48hpf. Therefore, it is important to have an anatomical idea of what the brain looks like at this time in development and what inherent characteristics will be the most interesting to investigate. A more general discussion of *P. dumerilii*'s larval brain development is detailed in [40].

From the early trochophore (24-26hpf), neural system development starts taking place. The apical ganglion which contains one serotonergic cell and a few neurons linked to the nerve of the ciliary band of the larva called the prototroch forms at the apical tuft, (see Figure 2). This allows the first movements of the larvae thanks to the ciliated



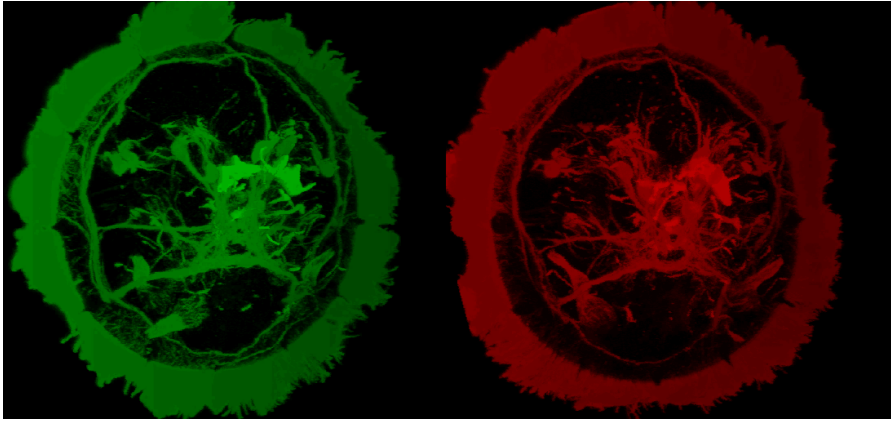


Figure 3: *Platynereis dumerilii*'s stereotypical and synchronous development. In green and red are two different *P. dumerilii* individuals' with the same gene expression being highlighted. They show extremely similar patterns of development for the nervous system.

cells of the prototroch.

The mid-trochophore (26-40 hpf) sees the formation of the first cerebral commissure: a band of nerves interconnecting the ventral nerve cord and the brain, which is a typical feature of annelid neurobiology. During this phase the apical ganglion becomes bigger with three more serotonergic cells.

The late trochophore (40-48hpf) sees the formation of the second commissure in the ventral nerve cord. It is at the end of this stage that the tissues of the brain become more complex with a notable increase in the number of neurites [40].

The data used in the rest of this thesis will not encapsulate the whole larvae, just the developing brain (see Figure 2) thus excluding the ventral part of the nervous system. The best studied areas of the developing brain are the larval eyes, the developing adult eyes and the apical organ on the dorsal side. On the ventral side are located the mushroom bodies, a pair of structures that are known to play a role in olfactory learning and memory in insects and annelids [120].

Consequently, even at this early stage in a relatively "simple" organism, the brain quickly becomes an extremely complex tissue. Cell types diverge and functional areas are formed. Before trying to understand more about *P. dumerilii*'s brain organization, it is interesting

to ask the more general question of how complex tissues such as the brain are defined spatially.

### 1.1.2 *Defining complex biological tissues and cell types*

The first written study of human anatomy that has survived through time and is sometimes attributed to Imhotep - physician, high priest and architect during the Old Kingdom of Egypt (3000-2500 BC) is the Edwin Smith Papyrus [44, 13]. Although mainly descriptive, some organs such as the heart or blood vessels were defined functionally. A more scientific approach to anatomy based on animal and human dissections and vivisections arose in ancient Greece and was led by scientists such as Alcmaeon (510 BC), Empedocles (480 BC) and later Aristotle (356 BC) [109]. In these early studies the global *function* of each organ was often inferred by analysing the result of accidental, war related or intentional injuries [109].

As science developed and the scale of the smallest biological unit was reduced to the cell, organs were described as complex tissues: coherent structures composed of large numbers of cells. These cells are not identical to one another. First, visually, cells composing the tissue may have different physical characteristics. Second, when observing cells *in vivo*, different cells in different parts of a complex tissue will exhibit different behaviour. Consequently, biological *tissues* can be viewed as an interconnected mosaic of cells having different functions and working together to assume the global function of the tissue. When looking closely at this mosaic, it is sometimes possible to observe under a microscope [132] that the cells' spatial organisation is not random, thus leading to a classification of cells with respect to their appearance and behaviour. These categories are known as *cell types*. Consequently, the definition of a complex biological tissue may be an ensemble of cells belonging to different cell types grouped in the same spatial structure. If historically *function* and physical characteristics of the organ were directly linked, microscopes and the observation of cells behaviour within a particular tissue changed this one to one relationship.

As described in the previous section, the developing brain of *Platynereis dumerilii* can be defined as a globally as being the central nervous system of the animal. This global functional definition encapsulates the

sub-functions of all the sub-tissues in the brain. For instance, when changing the scale of study from the organ to the tissue level, one can anatomically distinguish very different tissues (e.g. photosensitive regions in the eyes and developing neurons).

Interestingly, the cells making up specialized sub-tissues in the brain belong to the same organ but have very different functions. For example, photosensitive regions are composed of extremely specialized cells that display the ability to react to light stimulation [4] while developing neurons are part of the complex network that allows information to be transmitted and processed in the brain [40]. Importantly, the brain has a coherent overall function, but it is fascinating to observe that a wide variety of sub-functions are displayed by different types of cells. Hence, my definition of a *complex biological tissue* will be a spatially coherent ensemble of cells organised in sub-tissues, each of which possesses a specific function.

The sub-tissues in complex biological tissues tend to be spatially coherent. In other words, cells that belong to the same cell type are usually structured spatially and as a result it seems sensible to assume that cells spatially close to one another have a greater probability of belonging to the same cell type. However, the spatial coherency of these sub-tissues is not always the same. Some cell types may consist of individual cells that are scattered inside another more spatially coherent tissue. An interesting example is the difference between the spatial coherency of cells forming the neuronal tissue in the brain and that of cells forming a well defined region in the brain like an endocrine gland. When asking the question: “is it likely that this particular cell is fully surrounded by cells belonging to the same cell type?”, the extensions created by the axons of neurons (as shown in Figure 4) will decrease this probability. Indeed, axons will grow through other types of tissues to reach their destination [6, 24], making the overall spatial coherency of neural tissues smaller than that of very well spatially defined tissues.

Organs and cell types have been defined mainly by their anatomical traits. However, the functional heterogeneity of complex tissues goes deeper than this. In the case of the neurons presented above, every one of them has roughly the same appearance in different parts of the brain as neuronal tissue makes up a substantial proportion of cerebral volume. However, looking closely at the function of the neu-

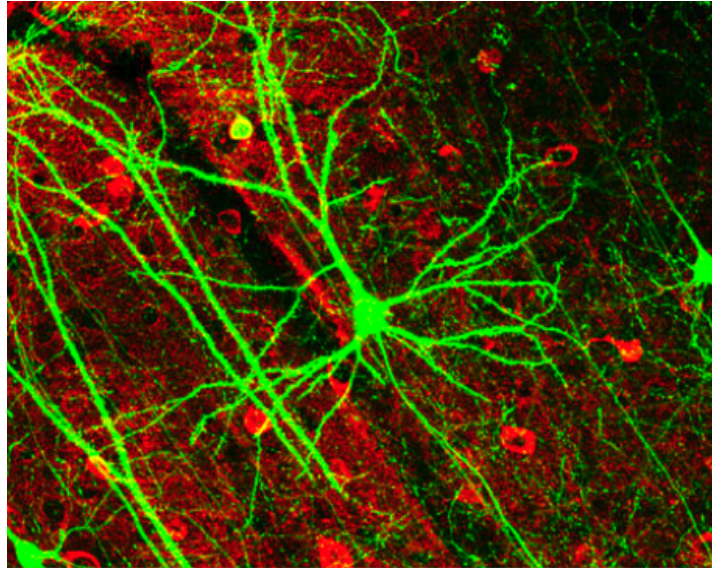


Figure 4: GFP staining of a pyramidal cell in mouse cortex showing dendrites and axons of a neuron linked and at the center the soma where the nucleus is located. In *P. dumerilii* the developed neurons display the same spatial characteristics. This Figure has been published under Creative Commons Generic license in [70].

rons from different parts of the brain unveils a different story. Indeed, despite their apparent similarity, some neurons will for instance react to the neurotransmitter *acetylcholin* while others will use *glutamate* (examples in the human brain [51, 122]). This type of difference may lead to very different functions.

This illustrates that defining cell types based on their anatomical traits is clearly insufficient to characterize tissues. As a result, I will now discuss a trait that fundamentally defines how cells are functioning, namely *gene expression*.

### 1.1.3 Generalities about gene expression and development

Throughout this thesis the term *cell* will be used to refer to eukaryotic cells and, more specifically, those of multicellular organisms. Every cell in a complex organism possesses the same genome, that is, the sum of all the genetic information contained in the cell (nucleus and other compartments). This fundamental homogeneity is in plain contradiction with the heterogeneity observed anatomically. If every cell has the exact same DNA, where does the great variability between

cell types come from? In other words, what makes a neuron become a neuron and not a pancreatic cell? Answering this type of question defines the field of developmental biology.

A concise answer to this question is: same genome but different pattern of gene expression. As a central cellular activity, numerous traits exhibited by cells throughout their life from their differentiation to their death, are defined by the way they express some specific parts of their genomes.

To understand what gene expression is, the notion of *gene* must first be defined. The precise definition of a gene remains controversial. The concept of a “*factor that conveys traits from parents to offspring*” was laid down by Gregor Mendel in 1866 [83] when the accepted theory at the time was based on blending inheritance where the traits of the parents appeared mixed in the offspring following a continuous gradient. The most recently published definition of a gene followed the publication of the ENCODE project [37]. It states that a gene is “*a union of genomic sequences encoding a coherent set of potentially overlapping functional products.*”. The lack of specificity in this definition underscores the complexity hidden behind apparently simple concepts in biology. Throughout this thesis *genes* will simply be considered as expressed portions of the genome.

Gene expression describes the way cells express their genes. Expression of a gene is the process of transcribing the DNA of that particular gene. It is interesting to note that there are several ways to look at gene expression. Indeed in a cell or a tissue, at a given time point it is possible to examine whether a gene is expressed or not (binary expression) or how much a certain gene is expressed (quantitative expression). The product of gene expression is RNA molecules. Technically, for transcription to occur in the nucleus a complex system of proteins will attach itself onto the DNA double helix. In the case of protein coding genes, this complex is the RNA polymerase II. Once this complex becomes attached to the promoter region of the gene, transcription can begin. The RNA polymerase complex will move along the gene and replicate the template strand of the DNA in a process known as elongation. The resulting RNA molecule will be a copy of the coding strand of the DNA created by the complementary sequence of the template strand. When the polymerase reaches an “end codon”, transcription terminates and the RNA molecule is

released and polyadenylated in order to protect the transcript from degradation in the cytoplasm [25].

A portion of RNA molecules are translated into proteins that can have very different purposes. Some will serve directly in cellular life as functional/structural agents (elements of the ATP synthase for example [12]), others will be excreted by the cell and will serve a purpose at the scale of the organism [63]. Others called transcription factors will have a regulatory effect on gene expression [86]. In other words the expression of gene  $G_a$ , coding for protein  $P_a$  might activate, accelerate, inactivate or decelerate the expression of gene  $G_b$  and potentially others. This outlines the complex interdependent regulatory system that is gene expression, see Figure 5. For precise examples of gene regulatory networks, see [45, 108, 43, 5].

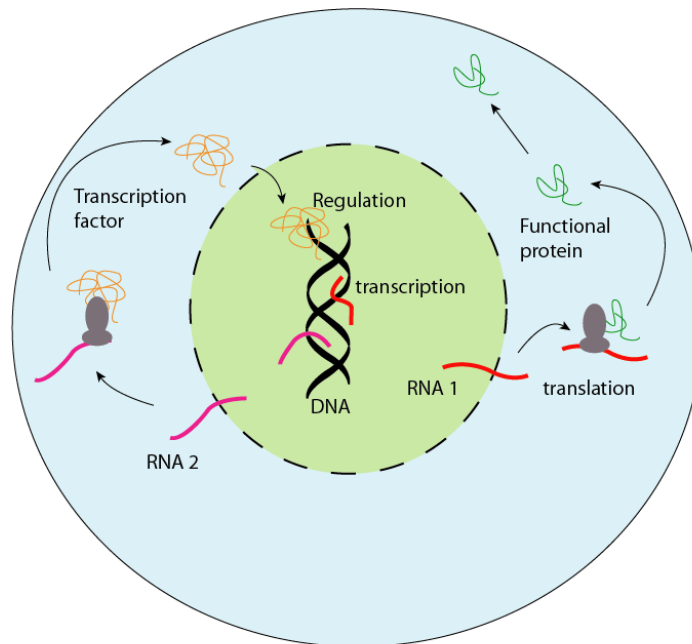


Figure 5: Gene expression and protein translation and gene regulatory networks. The schematics shows that genes in the DNA are transcribed to RNA molecules that are further translated outside the nucleus into proteins. Those proteins can serve various purposes inside the cell or come back to the nucleus to regulate gene expression.

During development, different mechanisms exist that allow cells to develop differently from one to the other. This is how the asymmetri-

cal axis (dorso-ventral, and basal-apical) of the body are defined. The main mechanisms for two cells to take two different differentiation pathways are signalling gradients and epigenetic control. They both act on the gene expression pattern of the cells. Epigenetic factors are directly coded onto the DNA structure but are not linked directly to the DNA sequence. Epigenetic modifications such as methylation or histone modifications influence gene expression by changing the accessibility of certain regions of the chromatin by modifying the chromatin state or the promoter strength [60]. Signalling gradients are environmental factors, they occur when cells grow in a medium containing certain chemicals. These chemicals will influence which gene they express [22]. They can either penetrate the cells and directly regulate transcription as transcription factors [35] or be recognized by some receptors at the surface of the cells that in turn will release transcription factors inside the cell [123].

Consequently, gene expression is one of the key factors that drives tissue development. Therefore, the ability to study gene expression patterns has revolutionized the field of developmental biology. Technological innovation has been the main driving factor of this revolution and, in the next section, I will present two methods for assaying gene expression that are used throughout this thesis.

## 1.2 CAPTURING GENE EXPRESSION IN THE LABORATORY

### 1.2.1 *In-situ hybridization assays*

In-situ hybridization (ISH) is an experimental technique where the practitioner is able to determine in which cells of the tissue under study a particular RNA is present. As opposed to Southern blotting [110], ISH assays not only enable the experimentalist to know whether a gene is expressed or not, but also where in the tissue it is expressed. First proposed in 1969 by Pardue [92] and John [61] independently, in-situ hybridization (ISH) used radioactive tritium labelled probes on a photographic emulsion to reveal parts of the studied tissues where particular RNA or DNA sequences were present.

With the development of fluorescent labelling techniques [68, 100] allowing for faster, more sensitive and of course safer hybridization assays compared to radioactive probes [114], Fluorescent in-situ hy-



bridization (FiSH) quickly became the standard technique to study gene expression in the spatial context of biological tissues. Importantly, using multiple fluorescent probes of different colours allowed the simultaneous localization of several RNA fragments within a tissue [89].

For small enough tissues under study, it is possible to hybridize the probes in the whole animal. This method is called Wholemount in-Situ hybridization (WiSH) and a 3-Dimensional representation of the expression map of a gene can be deduced by using confocal microscopy to study the patterns of gene expression in the tissue slice by slice [120].

### 1.2.2 RNA sequencing

Whole Transcriptome Shotgun Sequencing (WTSS) also called RNA sequencing (RNA-seq) [87, 125] has developed alongside Next Generation Sequencing (NGS) techniques used to sequence genomic DNA. In RNA-sequencing, only the fraction of RNA molecules in the cell are targeted. Protein coding mRNA molecules can further be selected by isolating transcripts using their polyadenylated 3' tail, a characteristic exhibited by protein coding transcripts and a few other types of transcripts only (lncRNAs for example). Most current technique use magnetic beads to achieve this separation [88, 87].

Once isolated from a population of cells, transcripts undergo fragmentation to obtain an average length of 200-300 nucleotides. The next step is the reverse transcription, which creates a complementary DNA (cDNA) library using viral reverse transcriptase enzymes. After amplification using quantitative Polymerase Chain Reaction (qPCR), the cDNA library is ready to be sequenced by NGS technology.

NGS refers to numerous experimental techniques used to acquire the DNA sequences from a sample with a high throughput. I will not extensively describe all of these methods in this thesis but succinctly present some of them.

- 454 pyrosequencing [75] is a sequencing technique that revolves around luciferase binding, a light emitting protein, to detect and sequence the nucleotides while the complementary strand of single stranded DNA molecules are synthesised by DNA



polymerase. The process of using DNA replication of single stranded DNA (ssDNA) molecules is referred to as *sequencing by synthesis*. When the ssDNA molecule is entered in the sequencing machine, it is bound to the DNA polymerase using previously attached primer. The reaction is supplied with energy in the form of dATP $\alpha$ S which does not react with the luciferase.

One of the four possible denucleoside triphosphates (dNTP) is then added to the reaction. If the next nucleotide of the ssDNA strand to copy is complementary to the current dNTP, the DNA polymerase will catalyse the reaction, inserting the new nucleotide in the newly created strand and realising an inorganic phosphate (PPi). The enzyme ATP sulfurylase added to the reaction will transform the PPi in ATP which will in turn react with the luciferase and emit light, signalling that the base complementary to the current dNTP was the next nucleotide of the ssDNA.

If two or more nucleotides added at the same time (in the case of nucleotide repetition), this can be detected by analysing the intensity of the emitted light which is proportional to the number of PPis released. Repeating this procedure in turn for each dNTP until the whole ssDNA has been replicated allows the sequence to be fully determined.

- Illumina sequencing [9] is one of the most commonly used NGS technology. Similarly to 454 pyrosequencing, light emission is used through dyes to detect the nucleotides of “DNA colonies”. During the library preparation step, the double stranded DNA is fragmented and the sheared ends are repaired and adenylated. Adaptors are then bound to each end of the fragments which are subsequently size selected and purified.

The next step is cluster generation where single DNA molecules are isothermally amplified to prepare them for sequencing. To this end, the adaptors ligated to the DNA molecules are bound on a surface with numerous oligo primers. Once the ssDNA molecules are bound from one end to the surface, the DNA strand is copied and ssDNA copies are bound to the surface on the other end as well, creating bridges. These bridges are amplified through a process know as isothermal bridge ampli-

fication resulting in millions of “DNA clusters”. The bridges are destroyed on one side and sequencing primers are then hybridized on the free end of the ssDNA molecules.

Finally the DNA clusters can be sequenced. Each fragment is sequenced base by base, by adding the four possible denucleoside triphosphates (dNTP), each bound to a different fluorescent marker. The dNTP will compete with each other to bind to the DNA template which means that the dNTP complementary to the current DNA nucleotide is very likely to be incorporated. Once the non-reacting dNTP fragments are washed away, the clusters are excited by a laser emitting a light with a specific frequency that identifies the newly added base. The fluorescent block is then removed and the sequencing cycle is repeated until the complete fragment has been sequenced.

The described sequencing methods generate large datasets of short reads, which need to be mapped back to the reference genome of the considered species, providing this genome is available. In this case, the resulting dataset will reflect a snapshot of the whole transcriptome in the studied cell population. In the case where the reference genome is not fully available, an alternative option is to map the reads back to a list of known gene sequences. The resulting dataset will represent a quantitative image of the considered genes in the cell population at one point in time.

Because of technical limitations in these sequencing protocols, until very recently the starting quantity of RNA was relatively important (this issue is discussed further in [7.1](#)). This is why most of the published RNA sequencing studies use a population of cells as a starting point. This, however, means that the gene expression landscape obtained as an output will represent an averaged expression over all the cells used as an input.

Importantly, when comparing RNA-seq to the previously described in-situ hybridization technique, while the methodological burden for analysing the expression of many genes at the same time is greatly reduced, the spatial localisation of the cells is lost during the protocol.

### 1.3 SUMMARY

In the introduction, I have presented a central aspect of cell and developmental biology, namely, gene expression. I have given an overview of how cells express their genomes and how the expression of specific signalling genes can influence the fate of cells during development. I have also described two methods that can be used to capture gene expression from a biological tissue: in-situ hybridization and RNA-seq.

I have described *Platynereis dumerilii* and the advantageous traits it exhibits for developmental biologists especially in the field of neural development. I have discussed the fact that anatomical traits are not sufficient to fully comprehend the deep heterogeneous patterns of functionalities inside a complex organ such as the brain. In order to push this understanding further I have discussed how gene expression levels can be used to characterise different tissues.

So far, I have considered biology at the scale of the tissue, or the sub-tissue. However, the heterogeneity of complex biological tissues does not stop at this scale of study. In fact, with a top-down approach looking at whole tissues and then separating them into smaller sub-tissues until “true” functional tissues are defined is an extremely complicated problem. A solution to this problem would be to reverse the approach from a top-down to a bottom-up mindset. This means reducing the scale of study to the smallest biological unit available, the single cell, defining the heterogeneity of gene expression at the single cell level and going back up to the functional tissue level from there. Instead of a fragmentation problem, this becomes a clustering problem, attaching single cells to a certain number of categories. In order to implement such an approach, single cell gene expression data is therefore needed.

Given this context, I will describe in the rest of this thesis my main contributions to the understanding of the the brain of *Platynereis dumerilii* with a special focus on developing methods to analyse single cell expression data in a spatial context.

In Chapter 2, I describe the main dataset I will be using in this work, an image library of in-situ hybridization assays reflecting gene expression at the single cell level for 169 genes in the brain. I then describe the data preprocessing applied to the in-situ hybridization at-

las in order to apply the methods presented in the following chapters. I finally present the results of hierarchical clustering, a non-spatial means of clustering the data.

In Chapter 3 I present the method central to my work, developed to answer the question of recovering cell types from single cell gene expression data. In this chapter, I give the theoretical background underlying the Hidden Markov random fields (HMRF) spatial clustering and how this method diverges from previously described HMRF methods.

I then evaluate in Chapter 4 the performances of the HMRF method on simulated data. I describe how binarized gene expression data with a spatial component was simulated, then validate the parameters estimation by the method and finally compare the performance of the method to other non spatial clustering methods in terms of clustering quality and computing resources.

I present in Chapter 5 the results of the HMRF method when applied to the binarized single cell in-situ hybridization data in the brain of *Platynereis dumerilii*. First, I propose a scoring method in order to use the clustering results to functionally define the regions. I then validate the method further by describing known regions of the brain that are found by the method. Finally I discuss how functional hypothesis can be made for unstudied regions of the brain.

In Chapter 6 I present a tool I developed to allow an easy visualization of 3D information and more specifically clustering results. This tool is central to the upstream and downstream analysis of the data and the results used in the thesis.

Finally, in chapter 7, I present a different project that aims to combine single-cell transcriptomic profiles generated from single-cell RNA-sequencing with the spatial location of the cell within an organism of interest, namely *Platynereis dumerilii*.

## MAIN DATASET USED IN THIS STUDY AND DATA PREPROCESSING

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### 2.1 BUILDING A IMAGE LIBRARY OF GENE EXPRESSION IN *p. dumerilii*'S BRAIN

During his PhD, Raju Tomer and other members of the Arendt lab in EMBL, used wholemount in-situ hybridization to create an image library of gene expression in the brain of *P. dumerilii*. They were able to record gene expression in the full brain at 48hpf for 169 genes. In practice, each individual larvae was dissected to isolate the region containing the developing brain. Each brain was then stained with two different fluorescent probes corresponding to two messenger RNAs (mRNA). One of the genes is considered a reference, as it is always hybridized in all the assays (the main reference gene used was *Emx*) alongside another gene of interest, see Figure 6. Each brain was then visualized with laser confocal microscopy to reveal the gene expression patterns in the brain slice by slice, generating at the same time 3D coordinates for each slice.

As mentioned in the Introduction, the larval development of *P. dumerilii* is highly similar in every individual larvae. In the case of this study where WiSH was performed on many independent animals, the stereotypical development of *P. dumerilii* has proven essential. Indeed, having the same reference gene localized in all assays allowed Tomer *et al.* to align all other gene expression patterns onto this scaffold. The result is an image library of 169 gene expression patterns in the full brain of *P. dumerilii* with a exploitable spatial reference that allows for a very precise mapping.

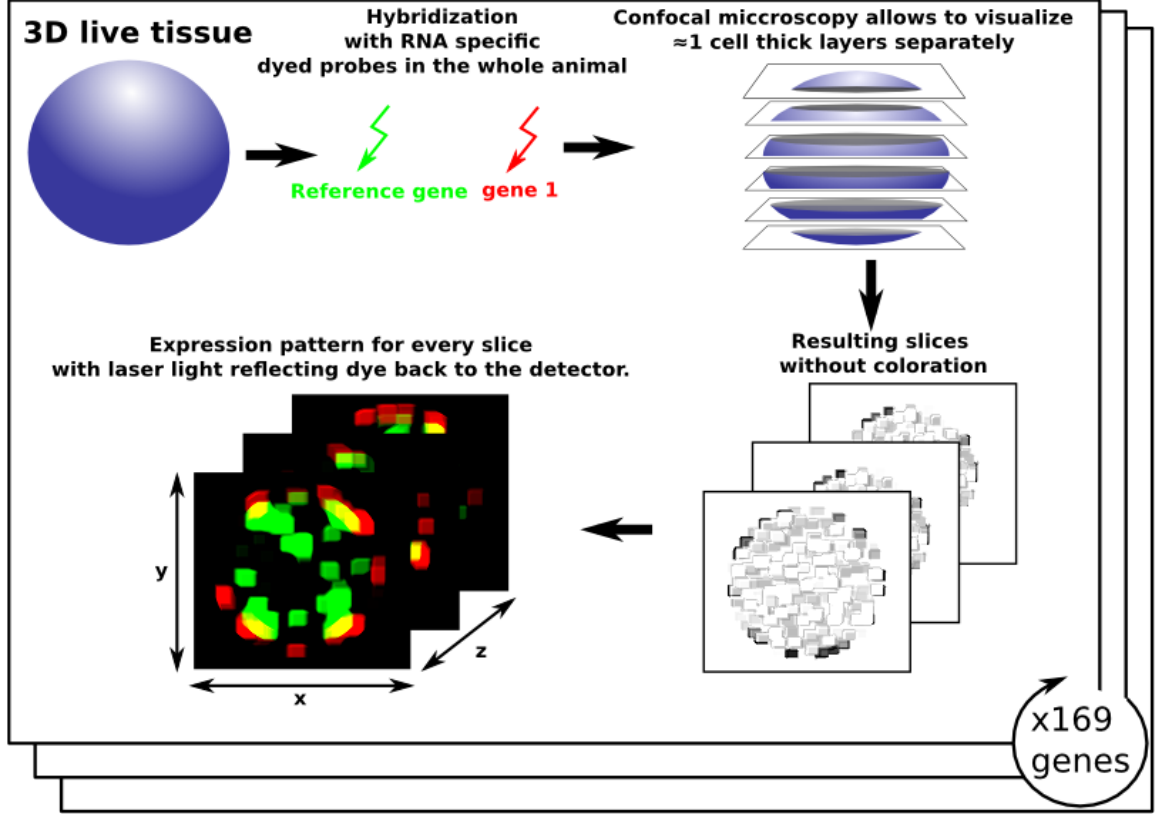


Figure 6: Wholemount in-situ hybridization assays used to create a 169 genes catalogue of gene expression in the brain of *P. dumerilii*. From the live tissue cut into thin fixed layers, every slice is stained with a reference gene and a gene of interest that will reveal areas of expression under fluorescent microscopy. The process repeated 169 times for key genes in *P. dumerilii* neural development has been generated by [120]

## 2.2 SPATIALLY REFERENCED SINGLE CELL-LIKE IN-SITU HYBRIDIZATION DATA

### 2.2.1 Dividing images into "cells"

Because in-situ hybridization preserves spatial information in the tissue under study, measuring gene expression at single cell resolution from an image obtained through confocal microscopy is a matter of microscope performance and cell size. For big enough cells, single cell resolution has been documented as far back as 1989 [116, 101].

When considering the *P. dumerilii* brain dataset, with current microscope technology, achieving single cell level resolution on one particular image is feasible. However, the main limitation is analysing

the quantity of data involved; indeed, each brain is separated into 20 slices, for 169 genes this yields 3380 images that require inspection. This technical bottleneck can be overcome with an automated way of analysing the fluorescence images. However this is not an easy task, as the computer program required needs to be able to *see* and divide the global picture into cells. Considering that all cells do not exhibit the same shape and size, constructing this *cell model* is a very complicated task.

It is for instance possible to highlight the limits of the cells and to automatically acquire those boundaries through computer vision methods. This process relies on targeting proteins in the membrane or in the extracellular matrix of the cells with specific fluorescent probes. Once the boundaries are acquired, defining every cell is a matter of finding enclosed spaces. To that end, numerous contour detection algorithms exist [72, 36, 2].

Unfortunately, a dataset with the cell limits highlighted does not yet exist for *P. dumerilii*'s brain, making a precise division of the images into cells very difficult. Instead, Tomer used a simple approach that divides the images into "cubes" [120].

### 2.2.2 A simple cell model, the "cube" data

Every slice of *P. dumerilii*'s brain being aligned onto the reference gene scaffold (see section 1.2) for all 169 genes, the "cube" model simply consists of dividing each image into squares approximately the size of an average cell. In the *P. dumerilii* dataset, the size chosen was  $3 \mu\text{m}^2$  [40]. Importantly, this is actually smaller than the average cell size in *P. dumerilii*'s brain. Each slice of the brain being approximately  $3 \mu\text{m}$  thick, the resulting dataset, spatially referenced in 3D, will contain  $3 \mu\text{m}^3$  cubes, each of which is associated with the luminescence data for each of the 169 genes.

Of course this cell model is far from perfect: it assumes that every cell in the brain is roughly the same size and cubical, which is clearly not the case. Consequently, the "cube" model will introduce errors in the dataset. The first type of error occurs within areas where the genes under study are highly expressed. In that case, the light emission might contaminate the surrounding cubes that do not nec-

essarily express the same gene (see Figure 7A). The second type of error is introduced by the choice of  $3 \mu\text{m}^3$  cubes. As they are smaller than the average cell, some cubes will fall on areas that may be artificially empty. Indeed, transcription in the cells mainly happens in the nucleus. mRNA molecules then travel to the cytoplasm to be translated but they are not evenly distributed across the cell; in particular for some large cells, parts of the cytoplasm may record no expression in a cell that actually contains a lot of transcripts (see Figure 7B).

Hence, the data will tend to exhibit spatial discontinuity and inconsistency. With this fact in mind, any automated way of interpreting this data (in the case of this thesis: clustering “cubes” into cell types) will have to take into account this spatial discontinuity and try as much as possible to smooth over those potential expression gaps.

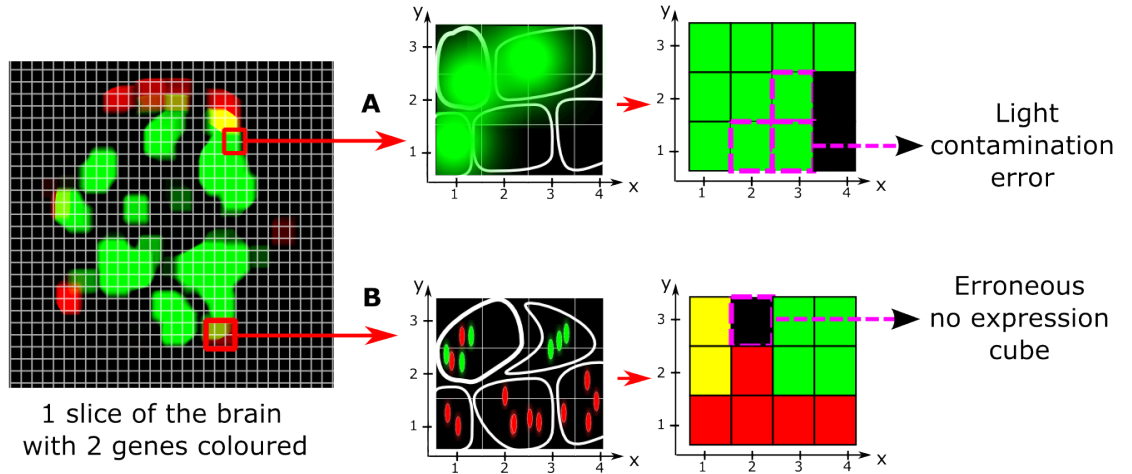


Figure 7: Errors introduced by the “cube” cell model. Path A shows how regions with highly expressed genes can introduce errors through light contamination. Path B shows how some cubes may appear artificially void of expression because of the uneven distribution of transcripts inside the cytoplasm especially for large cells.

However, even with this simple cell model, the data generated by [120] is highly valuable. Indeed, not only does this dataset give a snapshot of gene expression for 169 genes in the full brain of *P. dumerilii*, it also attaches spatial information to each data point.



## 2.3 ABOUT THE QUANTITATIVE TRAIT OF SINGLE CELL EXPRESSION DATA

### 2.3.1 *Light contamination in in-situ hybridization data*

The light intensity value obtained from in-situ hybridization assays can be considered as a quantitative measure of gene expression [33]. Indeed, the light emitted by every cell in the considered tissue is correlated with the number of RNA fragments of the gene of interest present in the cell as each fragment bound to a probe is an independent source of emission and the probes are hybridized in the cells in large excess. This means that if the targeted gene is highly expressed in a cell, there will be more sources of emission, thus making the overall light intensity captured on this area higher than in a cell expressing the gene at a low level.

As mentioned in Section 2.2, in-situ hybridization assays at the single cell level are prone to localized errors due to the cell model. One explanation for those errors, as shown in Figure 7B is the phenomenon of light contamination. When a large group of neighbouring cells express the same gene, the additivity of light intensity mentioned above means that even though the cells express the gene at the same rate, cells surrounded by a lot of other cells expressing the same gene will have abnormally high light intensity readings due to light contamination from the adjacent areas. As a result, when considering a hypothetical circular portion of tissue where a gene is monotonously expressed, the recorded light intensity will show a gradient with the maximum localized on the circle's centre.

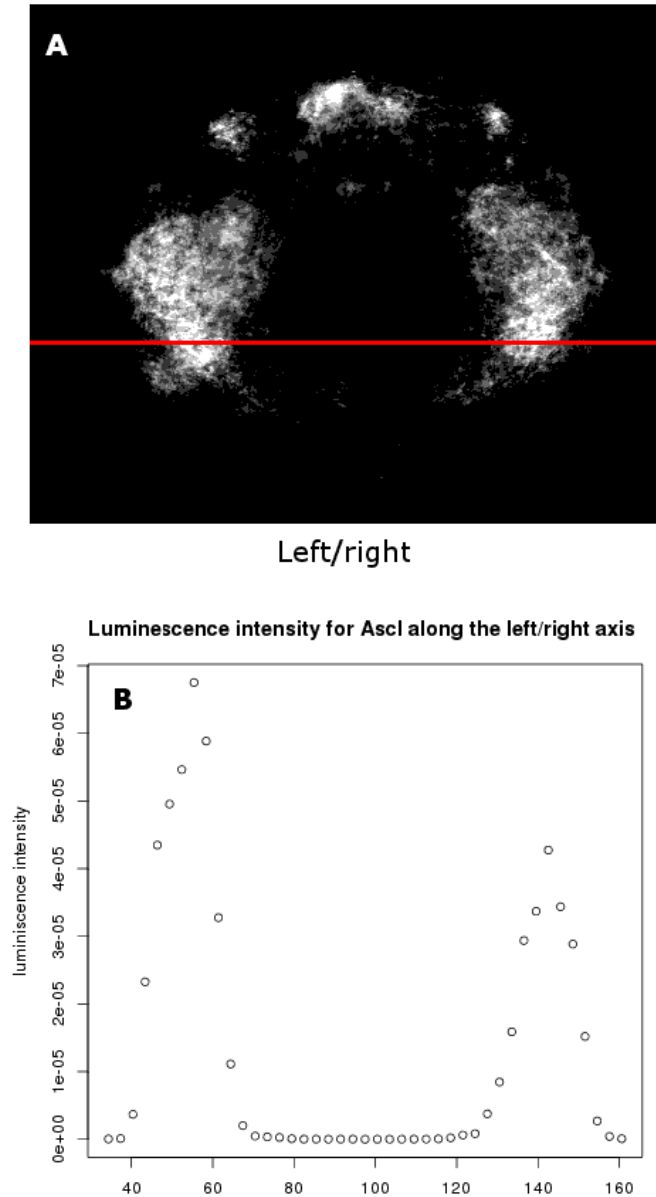


Figure 8: **Light contamination in in-situ hybridization luminescence data seen with the example of the gene *Ascl*.** Panel A shows the raw fluorescent microscopy capture of the gene's expression for one layer in the brain of *Platynereis*. Panel B shows the light intensity measured along the red line in panel A. Because of the small scale of study, cells surrounded by other cells expressing a particular gene will have higher intensity values because of nearby light contamination.

As shown in Figure 8, the issue of light contamination seems to occur when using the  $3 \mu\text{m}^3$  "cube" model. In this context, and because of the single cell scale of this study, considering the in-situ hybridiza-

tion data as quantitative may introduce significant errors. In order to avoid this light contamination bias a solution is to transform the quantitative data into binary data where, for a given “cube”, genes are simply expressed or not.

### 2.3.2 Binarizing in-situ hybridization datasets

As shown in Figure 8 and discussed in the previous section 2.3, the various problems linked to light contamination can be avoided by transforming the “quantitative” fluorescence information into binary data. In other words, if  $S$  is the set of all “cubes” in the brain,  $M$  the set of all the considered genes and  $y_{i,m}$  the value retrieved from the in-situ hybridization data for “cube”  $i \in S$  and gene  $m \in M$ , then  $y_{i,m} = 1$  if gene  $m$  is expressed at site  $i$ ,  $y_{i,m} = 0$  otherwise. The binarization process itself is not trivial. Indeed, defining the light intensity threshold above which a gene is considered expressed is a complicated problem, especially for noisy data.

Looking at the density of intensities across all the “cubes” for each gene yielded two very different scenarios: some densities were separated into two clear peaks, making the threshold easy to find while others exhibited a single peak making it hard to choose a clear cut value as shown in Figure 9. After trying different thresholding methods based on those densities, I found, in collaboration with Kaia Achim and Maria Tosches from the Arendt group in EMBL Heidelberg that none of them resulted in binary expression that was satisfying for many genes when compared with a manual inspection of the in-situ hybridization raw images. Considering that this binarized dataset will be the cornerstone of the work presented in this thesis, it was very important to achieve a high confidence thresholding. Given the small number of genes studied (169), and the collaboration with a team of biologists working specifically on *Platynereis dumerilii*’s brain, a manual thresholding approach was developed. Indeed, by going through the 169 genes one by one, it was possible to adjust the thresholds manually until the resulting binarized expression pattern corresponded perfectly to 1) the fluorescent stack images from in-situ hybridization data; 2) the biologically known expression patterns in the brain of *P. dumerilii* expected by the biologists.

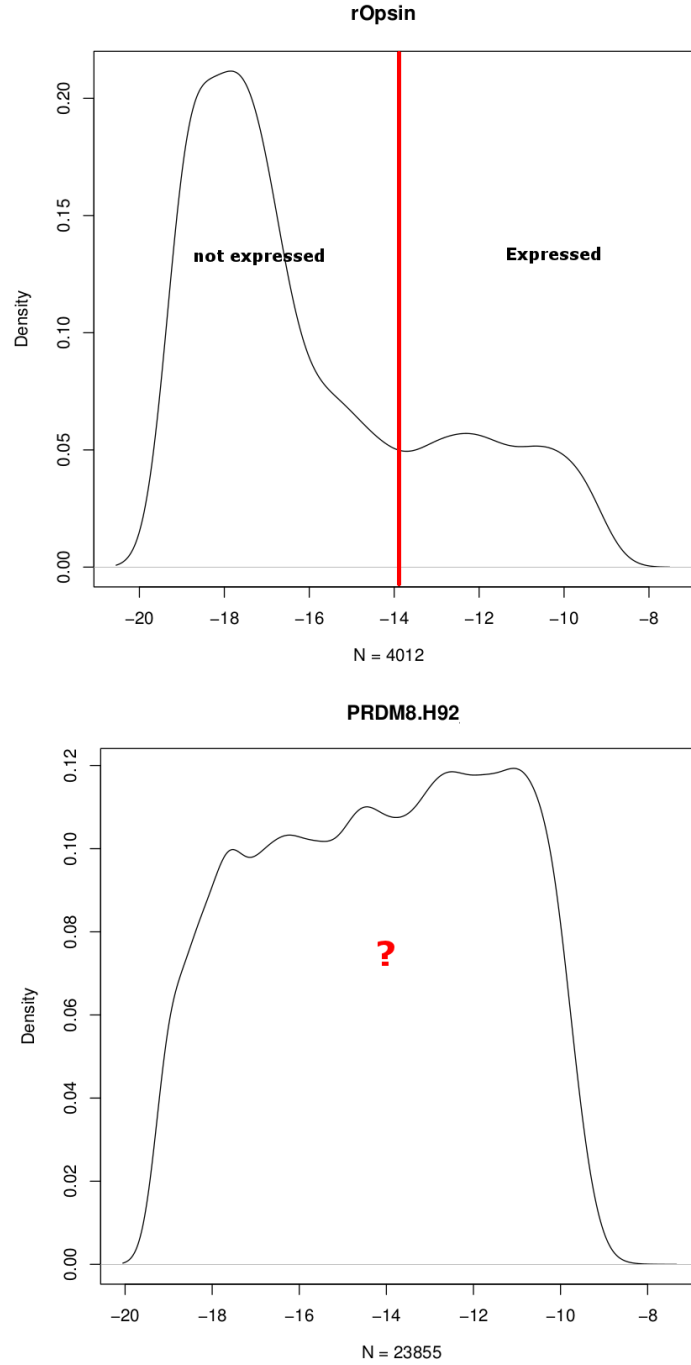


Figure 9: **Densities of log luminescence values for two genes (rOpsin, PRDM8) over the 32,302 cells.** For *rOpsin*, the density exhibits two clear peaks making the choice of a binarizing threshold easy. By contrast, for *PRDM8* there is no such clear threshold, making an automated binarization method hard to implement.

This method resulted in a high confidence binarized dataset for 86 genes. Several reasons explain why 83 genes out of the starting 169 were removed from the dataset. For some of the genes no good thresh-

old could be found, this was due to high noise level in the in-situ hybridization images. Other images suffered from experimental errors that yielded blurred and unexploitable expression patterns. Finally some images were polluted by a well known experimental artefact linked to confocal microscopy imaging as shown in Figure 10.

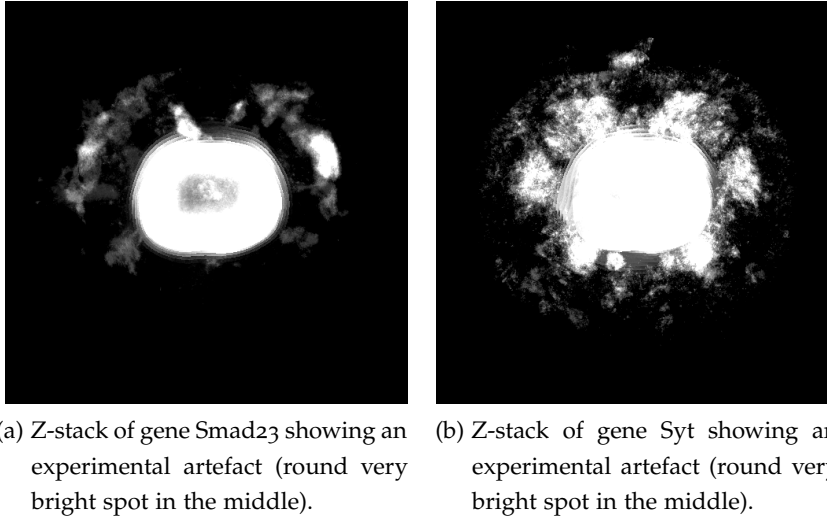


Figure 10: Confocal microscopy experimental artefact for 2 genes of the original 169 studied genes.

Although the aforementioned method resulted in a high quality binary dataset, it has been possible only because the number of genes considered was small. This will not be the case when dealing with RNA-seq data.

## 2.4 ELEMENTS OF CLUSTERING FOR BIOLOGICAL TISSUES

### 2.4.1 Motivations

Given the ability to study gene expression at the single cell level, the first question that seems natural to answer for developmental biology is the following: analysing single cell gene expression data only, is it possible to classify cells that are the most alike together and define the organization of complex biological tissues like the brain of *Platynereis dumerilii*?

This is fundamentally a clustering or a classification problem. Indeed, small units need to be put in a determined number of classes

or clusters because they are alike in one way or another. As anatomical and functional information about some tissues in the brain of *P. dumerilii* is already available (see Chapter 1), the obvious validation for any clustering/classification method developed is to check that the single cell level information leads to the definition of these known tissues. Once this has been validated, it seems important to determine whether the single cell expression data *adds* to the known biology by redefining (subdividing for example) known tissues or finding new ones. Identifying putative cell type is already a major challenge but it may be possible to go further. As mentioned in the Introduction, because gene expression is a key process in a cell's life, studying the genes that characterize a cluster can provide insights into the functional role of the cells it contains.

#### 2.4.2 General considerations about clustering

I mentioned before that methods developed to answer those questions could either be clustering or classification methods. In the field of machine learning, these two notions are fundamentally divergent. Clustering describes a method that assigns points to an unknown number (*a priori*) of sets in an undirected way, while classification takes advantage of an already known labels to assign, in a directed manner, new elements to a determined number of clusters.

In my case, the number of tissues in the brain of *P. dumerilii* is unknown and there is no previous classification or sufficient biological knowledge of each and every cell to opt for a directed classifier. Therefore the methods presented hereafter will be clustering methods with respect to the machine learning definition of the word.

As a general consideration about clustering, it is important to note that unless working on simple datasets, there is no perfect method. This is especially true when dealing with biological data, where the complexity and the noise level (see 2.3) tend to be extremely high.

To illustrate this notion, for the single cell expression data in *P. dumerilii*'s brain, the question of finding the "true" number of tissues is extremely complicated. Without any prior knowledge, the statistical methods to determine the number of clusters presented in this thesis will yield indications about what the optimal number of "tis-

sues” is given the data and the model, which does not necessarily means that this number is biologically *true*.

### 2.4.3 Hierarchical clustering

The first method I investigated was hierarchical clustering (hClust) [62]. Indeed, in the field of molecular biology and biology in general, this clustering method is extremely popular mainly because it is relatively straight forward to use, and because the obtained dendrogram helps the downstream analysis of the data.

hClust relies on the computation of a distance matrix. To calculate this I considered the matrix  $D$  of the in-situ hybridization data, with 86 columns corresponding to the 86 genes considered and 32,203 rows corresponding to every cell in the dataset. The computation of the distance matrix was performed using the *dist* function in R with the *euclidean* metric (or *Manhattan* which is equivalent for a binary dataset) in order to compute the  $32,203 \times 32,203$  matrix of distances between rows.

It is interesting to note that this step, in addition to being computationally expensive, creates a very large object in memory making it a limiting factor for very large datasets. Based on this distance matrix, the hierarchical clustering can take place using the “hclust” function in R. With the “complete” option turned on, the resulting object will be a dendrogram representing the hierarchical classification of all 32,203 cells as shown in Figure 11.

Importantly, once this dendrogram is outputted, the hClust method gives very little indication on where to “cut” the dendrogram to output the actual clustering results. This highlights a very important issue in all clustering methods, namely identifying the optimal number of clusters needed for a certain dataset when there is no prior information. For the rest of this thesis this crucial parameter will be referred to as  $K$ .

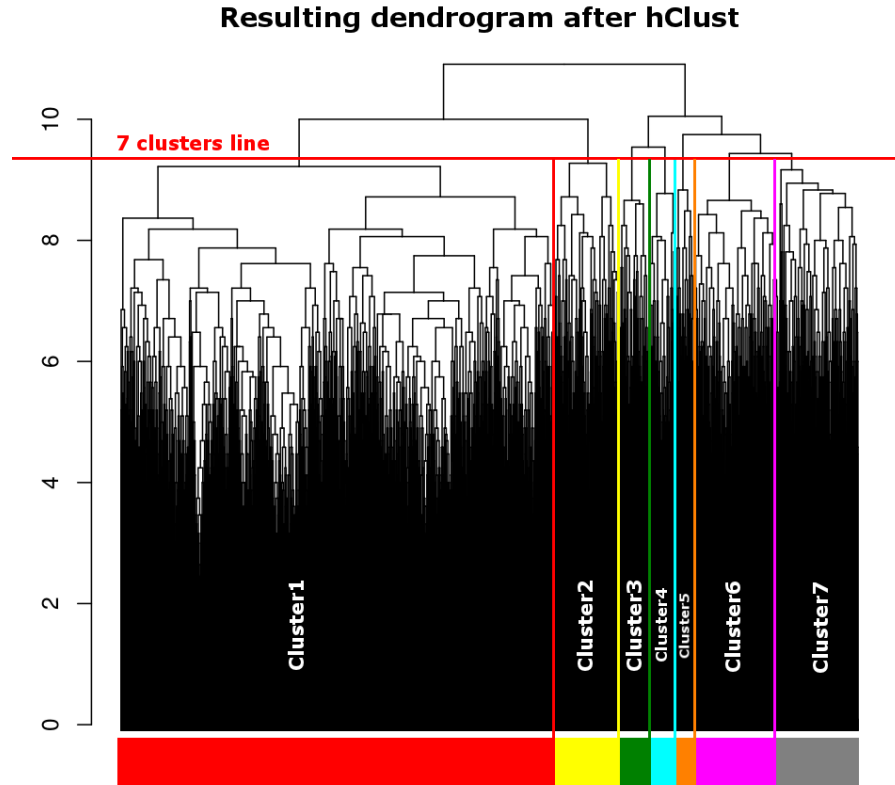


Figure 11: Dendrogram outputted by the hClust clustering method. This is the full dendrogram, to get the resulting clustering partition, the tree must be cut. The red line shows the cut needed to get 7 clusters out of the dendrogram. Importantly, a dendrogram does not provide a clear rationale about the best number of clusters.

#### 2.4.4 Other clustering methods adapted to gene expression data

There are several other clustering methods that could be applied in order to create a partition of gene expression data. They include but are not limited to K-means clustering [74] and independent mixture models [28]. Those methods are well suited to cluster gene expression data. However, they all fail to take into account the spatial information linked to the gene expression dataset.

## 2.5 DISCUSSION

### 2.5.1 Spatial clustering techniques

Using a clustering method that would in addition to the gene expression pattern of each cell, take into account its spatial localization,



that is the context of each cell regarding the other cells around it, I hypothesise that this supplementary information could theoretically improve the clustering performances for several reasons.

As mentioned in the Introduction, many of the underlying processes implicated in tissue development, the best example of which is the process of asymmetrical cell divisions, lead to highly structured spatial organization. In this context and without any other prior knowledge, not taking into account the spatial localization of each cell into the clustering scheme would seem to be an example of unexploited potentially important information.

Single cell gene expression datasets whether they are generated from in-situ hybridization (see details on Figure 7) or single cell RNA-seq (Figure 33), are prone to errors and incoherency. A clustering method that would be able to compensate “erroneous” data points by taking into account the spatial context of each cell, could potentially dramatically decrease the effect of noise level upon the clustering results. Additionally, from a downstream analysis perspective, as far as general hypothesis about clusters are concerned, less scattered clusters are easier to interpret when visualizing the results.

### 2.5.2 *Hidden Markov random fields for clustering*

In order to utilise both the spatial and the gene expression information, it was decided to extend a graph theoretical approach developed for image segmentation to reconstruct noisy or blurred images [26], a method that finds its roots in the field of statistical mechanics as the Ising model [56] and its generalization, the Potts model [130]. The core concept of this method is to use an Expectation-Maximization (EM) procedure to estimate the parameters of a Markov Random Field based model using mean-field approximations to estimate intractable values as described in [20].

This approach exhibits several important advantages as will be described in detail in the next sections. Indeed, in addition to providing a way to take into account the spatial information in the clustering results, it also offers some nice features in terms of downstream analy-

sis through the analysis of the optimal parameters upon convergence.

In the next three sections, I will first describe the theoretical framework underlying this model followed by an assessment of the method's performances compared to other non spatial clustering method on simulated data. Finally I will show and analyse the clustering results obtained through the developed method on the single cell in-situ gene expression data in *P. dumerilii*'s brain described previously.

## 2.6 CONCLUSIONS

I have described how a 3D image library of gene expression for 169 genes was built in the the brain of *Platynereis dumerilii*. I described how a simple cell model was developed to be able to reach a single cell level resolution of gene expression. I have also explained why, at the time of writing, it is still not safe to assume that this dataset is quantitative. To avoid this problem, turning those datasets into binary gene expression is an attractive solution. However the binarization process is not trivial and I have presented ways to obtain a high confidence dataset.

As mentioned previously in the Introduction (1), if the ability to study the heterogeneity of cell populations at the single cell level offers incredible possibilities for the future of developmental biology, the development of new statistical methods adapted to this single cell scale, allowing conclusions to be drawn at the tissue level, is crucial.

I have presented some considerations about clustering, in particular I have described how a clustering method may answer the main biological questions this thesis aims to answer. I have described a non-spatial method, hierarchical clustering.

The work presented hereafter aims to answer simple but important questions: can a spatial clustering method out perform a "standard" method like hClust? Can known functional tissues of a complex organ like the brain be defined and localized from single gene expression data? Can unknown regions in such a complex tissue be detected and finally, is it possible to hypothesize the functional role of those unknown regions based on single cell expression data?

## HIDDEN MARKOV RANDOM FIELDS FOR BIOLOGICAL DATA CLUSTERING

---

This Chapter gives a theoretical overview of a Hidden Markov Random Field based approach that is designed to cluster single cell in-situ hybridization gene expression data “cubes” as described in Chapter 2, into  $K$  clusters ( $K \in 2, 3, \dots$ ). Subsequently, we will describe our approach for estimating  $K$ .

### 3.1 BACKGROUND

Markov random fields (MRF) are statistical models that provide a way of modeling entities composed of multiple discrete sites such as images where each site is a pixel or in our case a biological tissue where each site is a single cell, in a context-dependent way [73]. MRF based methods find their roots in the field of statistical mechanics as the Ising model [56] and its generalization, the Potts model [130]. Since then, they have been and are still mainly used in the field of image analysis, and the literature about them is ever growing [105, 72]. More specifically MRF methods are found in a wide range of applications such as image restoration and segmentation [138], surface reconstruction [93], edge detection [135], texture analysis [23], optical flow [52], active contours [78], deformable templates [85], data fusion [129] and perceptual grouping [38].

MRF have also been used in a variety of biological applications from analysing medical imaging data [138, 53, 31] to analysing networks of genomic data [126]. In the context of the shift from the tissue to the single cell scale in transcriptomics assays described in the previous chapters, MRF based method represent a natural way to model gene expression in single cells while accounting for the relationship between sites.

Mathematically, MRF models are built around two complementary sub-models. On the one hand, the field represents the sites and their spatial structure central to the MRF theory. It is given a mathematically sound form through the Hammersley-Clifford (1971) theorem

which states that the influence between sites in a field following the Markov property follows a Gibbs distribution dependent upon an Energy function in which the spatial coherency parameters of the model are incorporated. This theorem gives a strong mathematical bases for modeling spatially dependent data. In this part of the model, some essential technical choices have to be made namely the *neighbourhood system* and the *Energy function* used. On the other hand, the emission model represents the data and it is necessary to make some distributional assumptions depending on the type of data modeled.

In the next few paragraphs I will present the technical choices made to apply this mathematical framework to the single cell in-situ hybridization dataset generated from *P. dumerilii*'s brain. I will also present the implementation of a EM algorithm used to find the maximum a posteriori (MAP) estimates of the model's parameters.

### 3.2 MARKOV RANDOM FIELDS

#### 3.2.1 Neighbourhood systems

Let  $S$  be a finite set of sites, each of which represents one "cube" of data. Given the 3D coordinates of each site, the first challenge that needs to be overcome in order to use the spatial characteristics of the data in the clustering scheme is to express the data and their spatial relationship in a mathematically formal manner. To this end, starting from the spatial coordinates in 3D of each "cube", instead of a list of isolated measurements, it is possible to build a connecting graph representing the same data and the spatial dependence between the "cubes". In the context of this study, each node of the graph will represent a "cube" in the single cell expression data. Nodes that are linked together by an edge will be spatially dependent upon each other.

With prior biological data, one can manually create the spatial dependency graph by linking nodes together that are known to be functionally similar. In the case of this study, however, no such prior knowledge being available, it is necessary to define the spatial dependences in a different way.

The central hypothesis while developing this method is to assume that "cubes" that are close to one another are more likely to belong

to the same cell type (i.e cluster). Consequently, these spatial dependencies will be incorporated into a *neighbourhood graph* where “cubes” close to each other will be joined.

In the case of this study, because of the cell model used the graph will be a regular grid. In this context, there are several ways to translate the spatial relationship into neighbourhood graphs depending upon the number of neighbours considered for each site. As shown in Figure 12, the choice between a first or a second order neighbourhood system is purely technical. However, having more neighbours for each site will increase the complexity and ultimately the computational burden. Within  $G$ , a *clique*  $c$  is a subset of nodes that are all interconnected, i.e it is possible to go from any nodes in  $c$  to any other node in  $c$  by simply following one single edge.

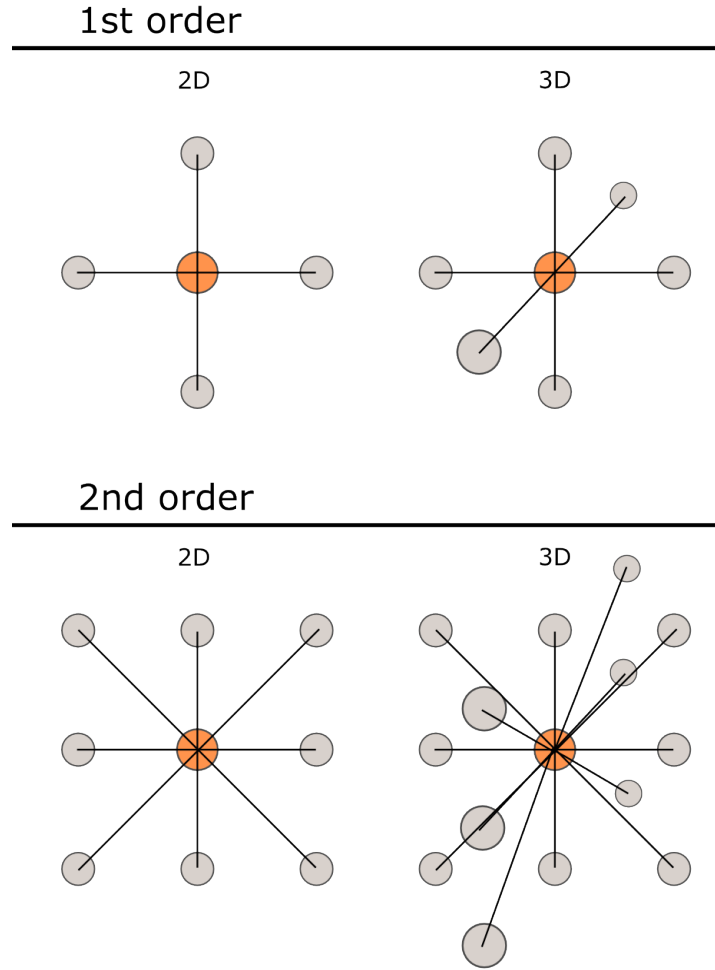


Figure 12: **First order and second order neighbourhood systems.** In the first order neighbourhood system, each site in the graph is linked to a maximum of 6 other sites in 3D while in the second order neighbourhood system each site can be linked to a maximum of 14 other sites. The Markov property on the graph implies that the state of any node (the orange one for example) can be fully determined by knowing the state of its neighbours (the grey ones).

Let  $C$  be the set of cliques of  $G$ . In a first order neighbourhood system,  $C$  is therefore the set of all sites alone and all the pairs of sites that are neighbours of one another. These are first and second order cliques, containing one or two sites. In a second order neighbourhood graph however, the set of all cliques in  $G$  also contains 3rd and 4th order cliques. Because the method implies iterating over the set of all cliques of the graph as I will detail in the next paragraphs, I decided to use a first order neighbourhood system to decrease the computational burden.

### 3.2.2 Field distribution

Let a Random Field  $Z$  be defined as a set of random variables  $Z = \{Z_i, \forall i \in S\}$  where  $Z_i \in 1, \dots, K$ . For every site  $i \in S$ , let  $N(i)$  represent the set of its neighbours (see 3.2.1) and  $z_{S-\{i\}}$  a realization of the field restricted to  $S - \{i\} = \{j \in S, j \neq i\}$ .  $Z$  is a *Markov Random Field* if and only if it follows the Markov property at every site :

$$\forall i \in S, P_G(z_i | z_{S-\{i\}}) = P_G(z_i | z_j, j \in N(i)) \quad (1)$$

Equation (1) states that the realization of the field,  $z_i$  at any site  $i \in S$  can be fully determined using only the state of its neighbours  $N(i)$ . In other words the probability that a “cube” is in a given state depends only upon the state of its neighbours.

The Hammersley-Clifford theorem states that if  $Z$  is a Markov Random Field, the joint distribution of the field  $P_G$  follows a Gibbs distribution such that :

$$\begin{aligned} P_G(z; \beta) &= W(\beta)^{-1} \exp(-H(z; \beta)) \\ &= \frac{e^{-H(z; \beta)}}{\sum_{z'} e^{-H(z'; \beta)}} \end{aligned} \quad (2)$$

with  $H(z, \beta)$  the Energy function summed over the cliques  $C$  of the graph  $G$ . Since we are working with a first order neighbourhood system,  $C$  is the set of all pairs of sites  $(i, j)$  that are neighbours. I chose to consider  $H$  as a function of a vector  $\beta = (\beta_1, \dots, \beta_K)$  containing  $K$  parameters as detailed in the next paragraph, and  $v_{i,j}$  a potential function set to 1 in our method because we are working on a regular grid graph. If the distances between sites were heterogeneous we could have used this function to weight the spatial dependence between sites. Given this set up, we can write

$$H(z) = - \sum_{i \in S} \beta_{z_i} \sum_{j \in N(i)} v_{i,j} \times \mathbf{1}_{[z_i = z_j]} \quad (3)$$

The denominator in (2), where  $z'$  represents all the possible realizations of the field, is a normalizing constant referred to as  $W(\beta)$ .

### 3.2.3 *Single and multiple beta models in a biological context*

This model is closely related to a K-colour Potts model [130]. However, the unusual nature of the data used in this thesis led to the idea of extending the model commonly used in the field of image segmentation. In particular, the K-colour Potts model defines a single spatial coherency parameter  $\beta$  that is shared by all clusters [113, 136]. Importantly, the method presented here was extended by assigning one  $\beta$  per cluster so that:

$$\beta = (\beta_1, \dots, \beta_K)$$

Interestingly, equation (3) is a decreasing function of every component of  $\beta$ . Indeed, for a particular cluster  $h \in K$ , a high value of  $\beta_h$  will accentuate the increase of the likelihood of the model through equation (2) when cluster  $h$  is spatially coherent. In other words, when a site has all its neighbours clustered in cluster  $h$ , classifying the site in cluster  $h$  (making cluster  $h$  spatially more coherent) will have an impact on the likelihood of the model proportional to the value of  $\beta_h$ . This Energy function thus favours spatially regular partitions and a higher value of  $\beta_h$ , with  $1 \leq h \leq K$  will amplify the smoothing effect, or coherence over cluster  $h$ .

The choice of an extended model with a multiple  $\beta$  parameter, is inherent to the data used in this thesis. The first motivation is purely cytological: In a biological context, it is expected that some tissues will be more spatially coherent than others. As mentioned in the Introduction and visualized in Figure 5, tissues composed of different cell types may interact differently with their neighbours. For example, differentiated neural cells with long axons are likely to be in contact with numerous other cell types that they pass through.

The second motivation for the extended model lies in the cell model described in 2.2. As described in Figure 7, some “cubes” may have inconsistent gene expression patterns. This type of error in the data will introduce spatial incoherence in the gene expression patterns. I also mentioned in Chapter 2 that the rate of errors linked to the experimental protocol may be dependent upon the cell type considered. Indeed, the errors described in Figure 7 are respectively more likely to arise in cell types with small and big cells. In summary, I believe that allowing one spatial parameter for each cluster enables a better smoothing of these potential experimental errors by accounting for



cell type specificity.

### 3.2.4 Field parameters

The field distribution contains  $K$  unknown parameters  $\beta = (\beta_1, \dots, \beta_K)$  that have to be estimated by the model. It is important to note that  $W(\beta)$  is summed over all possible realizations of the field  $Z$ , which is an exponentially complex sum as the cardinality of  $S$  rises. Therefore the computation of the normalizing factor becomes intractable very quickly. To address this problem, we are going to need to make some approximations in order to compute this quantity (Mean Field Approximations).

## 3.3 THE EMISSION MODEL

We have described the field distribution of a Markov Random Field representing our graph, we now need to describe the relationship between  $Z$  and the data.

### 3.3.1 Conditional independence in the observed data

As  $Z$  is unknown a priori and represents the partition, let  $Y$  be a set of random variables representing the observations (the in-situ hybridization data). The model requires a conditional independence assumption with regard to the observations  $Y$  given the partition  $Z$  so that, with  $f_{z_i}$  the density function relative to cluster  $z_i, i \in S$  (the realization of the field at node  $i$ ):

$$\begin{aligned} p(\mathbf{y} \mid \mathbf{z}; \Theta) &= \prod_{i \in S} p(y_i \mid z_i; \Theta) \\ &= \prod_{i \in S} f_{z_i}(y_i \mid z_i; \Theta) \end{aligned} \quad (4)$$

Equation 4 defines one unknown parameter per cluster:  $\Theta = (\theta_1, \dots, \theta_K)$ . It is interesting to note that this part of the model is equivalent to an independent mixture model [81]. Indeed, Markov random fields can be viewed as independent mixture models where  $Z$  is a set of independent, identically distributed random variables, which happens

when  $\beta = 0$ .

Given a particular cluster  $h \in 1, \dots, K$  and  $M$  the set of considered genes, the expression of each gene  $m \in M$  in cluster  $h$  is modelled by a Bernoulli distribution with parameter  $\theta_{h,m}$ . This leads to one unknown Bernoulli parameter per gene per cluster so that :

$$\begin{aligned}\Theta &= (\theta_1, \dots, \theta_K) \\ &= \begin{pmatrix} \theta_{1,1} & \dots & \theta_{1,K} \\ \vdots & \ddots & \vdots \\ \theta_{M,1} & \dots & \theta_{M,K} \end{pmatrix}\end{aligned}$$

### 3.3.2 Full likelihood of the Hidden Markov random field model

The conditional density function  $f_i, i \in S$  can be expressed as :

$$\begin{aligned}f_i(y_i | z_i; \Theta) &= f_i(y_i | z_i; \theta_{z_i}) \\ &= \prod_{m \in M} \theta_{z_i, m}^{y_{i,m}} \times (1 - \theta_{z_i, m}^{1-y_{i,m}})\end{aligned}\tag{5}$$

Looking at both fields  $Z$  and  $Y, Z$  together, the complete likelihood of the model is expressed as :

$$\begin{aligned}P_G(\mathbf{y}, \mathbf{z} | \Theta, \beta) &= f(\mathbf{y} | \mathbf{z}, \Theta) P_G(\mathbf{z} | \beta) \\ &= W(\beta)^{-1} \exp\{-H(\mathbf{z} | \beta) + \sum_{i \in S} \log(f_i(y_i | z_i, \theta_{z_i}))\}\end{aligned}\tag{6}$$

Because equation (6) is a Gibbs distribution, using the Hammersley-Clifford theorem we can conclude that the conditional field  $Z, Y$  is another Markov Random Field with the Energy function

$$H(\mathbf{z}, \mathbf{y} | \beta, \Theta) = H(\mathbf{z} | \beta) - \sum_{i \in S} \log(f_i(y_i | z_i, \Theta))$$

In our case, the goal is to recover the unknown realization of  $Z : \mathbf{z}$ . To this end we need to maximize the values of all the parameters of the model  $\psi = (\Theta, \beta)$ , and to chose the optimal number of clusters,  $K$ .

### 3.4 PARAMETER ESTIMATION USING THE EM ALGORITHM

As mentioned before, the aim is to assign each cell  $i$  to one of the  $K$  possible clusters. To do so, it is interesting to consider the Maximum Posterior Marginal (MPM) that maximizes  $P(Z_i = h | \mathbf{y}, \boldsymbol{\psi})$ , where the  $\boldsymbol{\psi}$  are unknown and need to be estimated. To this end, the Expectation Maximisation [28] (EM) principle can be applied. The EM algorithm consists in the Expectation step (E) where the expectation of the model's likelihood with the current parameters is computed and the Maximization step (M) where the latent variables that maximize the model's expectation computed in the E step are found. The two steps are repeated until a convergence factor is reached, that is when the number of cell changed from one cluster to another is smaller than 1% of the total number of clustered cells.

#### 3.4.1 Initialization

The first step of the algorithm is to initialize the model's parameter. To this end, it is possible to directly assign values for  $\boldsymbol{\psi}^0$ , or to generate an initial clustering  $\mathbf{z}^0$  from which the initial  $\boldsymbol{\psi}^0$  will be derived.

I decided to use a combination of both approaches, with arbitrary values assigned to  $\beta^0$ , typically 0, and the use of an initial clustering to compute the values of  $\boldsymbol{\Theta}^0$ . Indeed, for  $h \in 1, \dots, K, m \in M$ , because of the emission model, each  $\theta_{h,m}$  is the probability that  $m$  is expressed in cluster  $h$ . Consequently, given a clustering  $\mathbf{z}^0$  with function  $\text{Expr}_{h,m}$  the number of cells expressing gene  $m$  in cluster  $h$  and function  $\text{Num}_h$  the total number of cells in cluster  $h$  I set:

$$\theta_{m,h}^0 = \frac{\text{Expr}_{h,m}}{\text{Num}_h}$$

#### 3.4.2 E step

In the E step the parameters are fixed and the expectation of the model's likelihood  $Q(\boldsymbol{\psi} | \boldsymbol{\psi}^l)$  at iteration  $l > 0$  can be derived from equation 6 as:

$$Q(\boldsymbol{\psi} \mid \boldsymbol{\psi}^l) = \sum_{\mathbf{z}} p(\mathbf{z} \mid \mathbf{y}; \boldsymbol{\psi}^l) \log p(\mathbf{y}, \mathbf{z}; \boldsymbol{\psi})$$

Which can be further decomposed as :

$$Q(\boldsymbol{\psi} \mid \boldsymbol{\psi}^l) = \underbrace{\sum_{\mathbf{z}} p(\mathbf{z} \mid \mathbf{y}; \boldsymbol{\psi}^l) \log p(\mathbf{y} \mid \mathbf{z}; \boldsymbol{\Theta})}_{R_y(\boldsymbol{\Theta} \mid \boldsymbol{\psi}^l)} + \underbrace{\sum_{\mathbf{z}} p(\mathbf{z} \mid \mathbf{y}; \boldsymbol{\psi}^l) \log p(\mathbf{z} \mid \boldsymbol{\beta})}_{R_z(\boldsymbol{\beta} \mid \boldsymbol{\psi}^l)} \quad (7)$$

Equation (7) allows me to separately optimise  $R_y$  and  $R_z$ .

$R_y$  can be re-written using equation(4) as:

$$\begin{aligned} R_y(\boldsymbol{\Theta} \mid \boldsymbol{\psi}^l) &= \sum_{\mathbf{z}} p(\mathbf{z} \mid \mathbf{y}; \boldsymbol{\psi}^l) \sum_{i \in S} \log f_{z_i}(y_i; \boldsymbol{\Theta}) \\ &= \sum_{i \in S} \sum_{h=1}^K [\log f_h(y_i; \boldsymbol{\Theta})] p(Z_i = h \mid \mathbf{y}; \boldsymbol{\psi}^l) \end{aligned}$$

Therefore, in the M step I will need to compute the following probability:

$$t_{ih}^{l+1} = p(Z_i = h \mid \mathbf{y}; \boldsymbol{\psi}^l)$$

Computing this conditional probability is problematic because of the dependence between neighbouring “cubes”, and computing an exact value is computationally expensive. Indeed, each point being dependent upon its neighbours, and the neighbours being themselves dependent upon their neighbours, unsurprisingly computing these conditional probabilities becomes exponentially complex as the number of connected nodes in the graph grow. Additionally for  $R_z$ , as mentioned previously, it is also necessary to compute the value of the normalizing constant  $W(\boldsymbol{\beta})$ .

To compute those quantities, approximations are needed. Methods to do so include Besag’s pseudo-likelihood [10] to compute  $W(\boldsymbol{\beta})$ , and simulating the posterior distribution of  $Z$  given  $\mathbf{y}$  with the parameters at iteration  $l$ , with a Gibbs sampler to estimate  $t_{ih}^{l+1}$  [21].

However, another method exists, the mean field approximation originally proposed in the field of statistical mechanics. Since then, it has been used in a variety of fields including computer vision [133]

and to approximate the distribution of both  $W(\beta)$  (with a single  $\beta$ ) and  $t_{ih}^{l+1}$  [137]. I present here the extension of this method to a model with one  $\beta$  parameter per cluster.

### 3.5 MEAN FIELD APPROXIMATIONS

The idea behind this approximation is to compute intractable quantities at any point  $i \in S$  by setting all the other sites in the field to their mean values. Keeping in mind the Markov property expressed in equation (1), when considering a single site  $i \in S$ , setting all the other sites in the graph to a defined value is equivalent, in the case of an MRF, to setting only the values of  $N(i)$ .

When computing  $t_{ih}^{l+1}$ , the mean fields approximation yields the following fixed point equation for  $i \in S$  and  $1 \leq h \leq K$  [26]:

$$t_{ih}^{l+1} \approx \frac{f_h(y_i; \theta_h^l) \exp\{\beta_h^l \sum_{j \in N(i)} t_{jh}^{l+1}\}}{\sum_{u=1}^K f_u(y_i; \theta_u^l) \exp\{\beta_u^l \sum_{j \in N(i)} t_{ju}^{l+1}\}} \quad (8)$$

For the normalizing constant  $W(\beta)$ , by applying the mean-field approximation, using equation (3),  $W(\beta)$  can be written as:

$$W(\beta) = \sum_{z'} \exp(-H(z')) \approx \sum_{i \in S} \sum_{z_i} \exp(-H(z_i)) = \sum_{i \in S} \sum_{z_i} \exp(\beta_{z_i} \sum_{j \in N(i)} 1[z_i = z_j])$$

With this new set of equations, it becomes possible to estimate all quantities needed in the E step in order to compute the model's expectation.

### 3.6 M STEP

After the E step, maximizing  $\psi$  is relatively straightforward. Equation 7 yields:

$$\begin{aligned} \Theta^{l+1} &= \arg \max_{\Theta} R_y(\Theta | \psi^l) \\ \beta^{l+1} &= \arg \max_{\beta} R_z(\beta | \psi^l) \end{aligned}$$

For  $\Theta$ , once the  $t_{ih}^l = p(Z_i = h | y; \psi^l)$  have been computed during the E-step, those probabilities may be used to assign each cell

to its most probable cluster at step  $l$ . This is a hard clustering approach, which is a technical choice but of course the probabilities  $t_{ih}^l$  could instead be used to compute a fuzzy clustering criterion for instance, the Hathaway's fuzzy clustering criterion as described in [26].

Once the new partition is created, the values of  $\Theta$  that maximize the model's expectation can be computed iteratively for cluster  $h \in 1, \dots, K$  and gene  $m \in M$ . Specifically if  $\text{Expr}_{h,m}$  denotes the number of cells expressing gene  $m$  in cluster  $h$  and  $\text{Num}_h$  denotes the total number of cells in cluster  $h$ , we can write:

$$\theta_{m,h}^{l+1} = \arg \max_{\Theta} R_y(\Theta \mid \psi^l) = \frac{\text{Expr}_{h,m}}{\text{Num}_h}$$

In order to maximize  $\beta^{l+1}$ , an iterative approach such as the gradient ascent algorithm, the positive version of the gradient descent algorithm [17] was used for each  $\beta_h^{l+1}, h \in [1, K]$  over the function  $R_z(\beta \mid \psi^l)$ .

The described EM algorithm leads, after convergence, to a partition over  $K$  clusters that finds a local maximum of the model's expectation. Importantly, the maximum reached is only a local one as indeed the EM algorithm does not guarantee to reach the global maximum of a function. It is interesting to note that this fact makes the initialization of the algorithm a crucial step. I will discuss this further in Chapter 4.

### 3.7 ESTIMATING $K$

Without any prior knowledge, choosing the right number of clusters  $K$  is challenging. I decided to use an *a posteriori* method relying on the final log Likelihood of the model derived from equation (6):

$$\log L(\psi) = \log P_G(y, z \mid \Theta, \beta)$$

Because  $\log L(\psi)$  monotonically increases with the number of parameters of the model (i.e the number of cubes), I employed a penalized likelihood approach to infer the number of clusters. Specifically, if  $P$  is the total number of parameters in the model and  $N$  the cardinality of  $S$ , I calculated the Bayesian Inference Criterion (BIC) [18] as:

$$-2 \log L(\Psi) + P \log N$$

By computing the final likelihood for a large range of possible  $K$  values, the minimal resulting BIC will be chosen as the optimal number of classes,  $\hat{K}$ . When applied to the biological data however, this approach is not ideal as I will describe later in this thesis (see Chapter 5) but yields good results when applied to simulated data (see Chapter 4).

### 3.8 ALGORITHMIC OVERVIEW

In this section I give an overview of how I implemented the main algorithms described in this Chapter, namely the EM algorithm 1 and the gradient ascent algorithm 2.

Listing 1: EM algorithm in C pseudo-code

```
/*retrieving parameters*/

/*Starting initialization*/
/*Reading initialization file*/
if(initialization provided) {
    Read initialization file
    Assign cluster values to  $z^{(0)}$ 
}
/*Random initialization*/
else {
    /*Generating R random initializations*/
    for(R runs) {
        Generate random initialization
        Compute likelihood
    }
    Select initialization with highest likelihood
    Assign cluster values to  $z^{(0)}$ 
}

/*
*z(0) is now defined
*Compute the initial parameters values
*/
Compute  $\Theta^{(0)}$  from  $z^{(0)}$ 
Set  $\beta^{(0)}$  to the user defined value
```

```

/*Start EM procedure*/
/*Alternate E step and M step until convergence is reached*/
while(Clusters changed < user defined convergence limit) {
  /*E step*/
  Compute densities from the emission model
  Fixed point algorithm to compute  $t_{ih}^{(l)}$ 
  /*Create  $z^{(l)}$ */
  Assign each cell  $C_i$  to new cluster using  $t_{ih}^{(l)} = p(Z_{C_i} = h)$ 

  /*M step*/
  Compute  $\Theta^{(l+1)}$  from  $z^{(l)}$ 
  Gradient ascent algorithm to compute  $\beta^{(l+1)}$ 
}

/*Output clustering results*/

```

Listing 2: Gradient ascent algorithm in C pseudo-code

```

/*Computing each  $\beta_h$  sequentially*/
/*We use a fixed step*/
step = 0.1
Foreach(h in K) {
  while(convergence is not reached) {
    current likelihood = likelihood(model)
     $\beta_{current} = \beta_h$ 
     $\beta_h = \beta_{current} + step$ 
    Derivate Likelihood Plus = likelihood(model) + current
    likelihood
     $\beta_h = \beta_{current} - step$ 
    Derivate Likelihood Minus = likelihood(model) - current
    likelihood

    /*Which way to go?*/
    if(Derivate Likelihood Plus > 0 || Derivate Likelihood
    Minus > 0) {
      if(Derivate Likelihood Plus > Derivate Likelihood Minus)
      {
         $\beta_h = \beta_{current} + step$ 
      }
      else {
         $\beta_h = \beta_{current} - step$ 
      }
    }
  }
  else {
    /*We reached convergence*/
  }
}

```



```

         $\beta_h = \beta_{\text{current}}$ 
        convergence is reached
    }
}
}

```

### 3.9 IMPLEMENTATION

I implemented the HMRF method in the programming language C. The source code, compiled binaries and a user manual are available on my Github profile [http://github.com/jboggp/MRF\\_Platynereis\\_2014](http://github.com/jboggp/MRF_Platynereis_2014).

### 3.10 SUMMARY

The goal was to allocate the  $S = 32,203$  “cubes” described above in Chapter 2 into  $K$  clusters, where  $K$  is unknown, using the binarized matrix of  $M = 86$  gene expression measurements,  $Y$ . To incorporate spatial information into the clustering scheme, I assumed that  $Z$ , the (latent) vector of length  $S$  that describes the allocation of cells to clusters, satisfies a first-order Markov Random Field (MRF), where the probability that a cell is allocated to a given state depends only upon the states of its immediate neighbours (Figure 12). Additionally, within cluster  $h$  ( $h \in 1, \dots, K$ ), I assumed that the expression of gene  $m$  follows a Bernoulli distribution with parameter  $\theta_{m,h}$ . The  $M \times K$  matrix  $\Theta$  denotes the full set of Bernoulli parameters. In a typical MRF, the degree of spatial cohesion is determined by a single parameter  $\beta$ , which is assumed to be constant for all clusters [113, 136]. However, in the context of tissue organisation, it is reasonable to expect that the degree of spatial cohesion will differ between clusters; consequently, a separate value of  $\beta$  is estimated for each of the  $K$  clusters.

To estimate the parameters of the model an Expectation-Maximisation (EM) based approach has been used in conjunction with mean-field approximations to infer intractable values [20]. Finally, to choose the optimal number of clusters,  $K$ , I used the Bayesian Information Criterion (BIC).

The next step is to validate the method's behaviour and to assess the quality of the results compared to the other non-spatial clustering schemes described in [Chapter 2](#).

## METHOD VALIDATION AND PERFORMANCE ANALYSIS ON SIMULATED DATA

---

### 4.1 SIMULATING DATA WITH A SPATIAL COMPONENT

Simulating data with a spatial component is a not a trivial problem. Existing methods rely on MCMC approaches as described in [21]. However, in the *P. dumerilii* in-situ data, with a relatively large number of nodes in the graph ( $\sim 34,000$ ), this is computationally expensive [8]. To overcome this problem, I exploited the fact that the *Platynereis* dataset already possesses a spatial component. As outlined in Figure 13, the simulation starts by clustering the gene expression data using different values of  $K$  with the HMRF method described in chapter 3 and by storing the resulting parameter estimates. Subsequently, I use the values of the estimated parameter  $\Theta$  to simulate binarized gene expression data from  $K$  clusters where, for cluster  $h$ , the expression of gene  $m$  is simulated from a Bernoulli distribution with parameter  $\theta_{m,h}$  as described in 4.1.1. This non-spatial simulated data is then reintroduced in the spatial context of the biological data (4.1.2) leading to a simulated dataset with all parameters being fully determined. In the next paragraphs, I will describe each step of this simulation scheme.

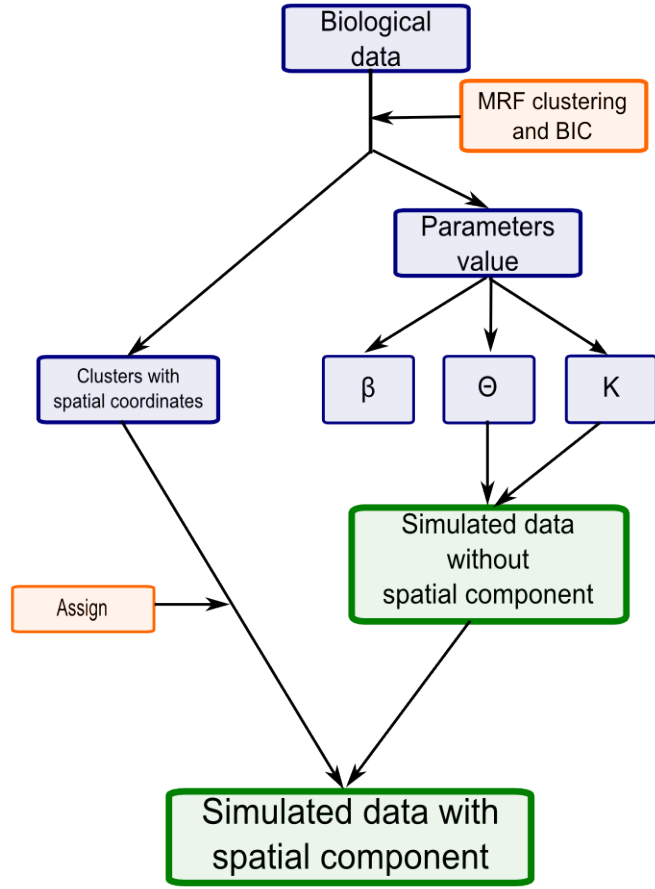


Figure 13: **Simulation scheme used to generate gene expression data with a spatial component and known parameters.** The values of  $\Theta$  are used to generate a dataset of clusters with the same gene expression profile as the reference. Each simulated cell is then assigned to its corresponding spatial location so that the simulated data keeps the spatial structure of the biological data.

#### 4.1.1 Simulating non-spatial gene expression data

The first step of the simulation scheme is to simulate binary gene expression data for  $S = 32,203$  sites and  $M = 86$  genes belonging to  $K$  clusters. Each cluster will be assigned  $N_h$  sites with  $h \in [1, K]$ . Given the emission model described in Chapter 3, for each gene and each cluster, a  $K \times M$  matrix  $\Theta$  is needed where each  $\theta_{h,m}$  represents a Bernoulli parameter corresponding to the probability that each site in cluster  $h$  expresses gene  $m$ .

In order to generate a biologically coherent  $\Theta$  matrix, I applied the HMRF method to the true biological data for  $K$  clusters and used the resulting  $\Theta$  matrix to simulate new data. The clustering of the biological data also generates the number of cells per cluster  $N_h, \forall h \in K$ .

Once the parameters values are available it is relatively straight forward to simulate a vector of gene expression for the  $N_h$  sites in each cluster.

#### 4.1.2 *Introducing a known spatial context*

Each simulated data point is then assigned to the same spatial location as the corresponding “cube” in the biological dataset, meaning that both the simulated and the biological datasets have the same neighbouring graph. By using simulated gene expression data equivalent in the same spatial context as the true data, the hypothesis is that the set of parameters  $\beta$  will stay relatively stable when the simulated data are clustered. Consequently, the values of  $\beta$  obtained after clustering the true data may be used as reference values.

#### 4.1.3 *Expected results*

Given this simulation scheme, the expected result after clustering the simulated data is a strong conservation between the “true” values  $\hat{\psi}$  obtained from clustering the biological data and the estimated values  $\tilde{\psi}$  obtained after clustering the simulated data.

## 4.2 COMPARING CLUSTERING RESULTS USING THE JACCARD SIMILARITY COEFFICIENT

### 4.2.1 *Theoretical problem in comparing clustering results*

To compare clustering results, several metrics exist to estimate the similarity between two lists of clusters. One of the most widely used ones is the Jaccard coefficient [59]. For two clustering results, for instance the output of two approaches when clustering the same data  $A$  and  $B$ , the Jaccard coefficient quantifies the similarity between  $A$  and  $B$ . In other words, the higher the Jaccard coefficient between  $A$

and B, the more similar the two clustering sets are.  $J(A, B)$  is defined as:

$$J(A, B) = \frac{|A \cap B|}{|A \cup B|}$$

Although theoretically very simple, in practice computing this metric is not trivial. Indeed, depending on the clustering method used and on the initialization, even if the clustering results are 100% identical, they may be misaligned.

This means that for method A *cluster 1* could for example be *cluster 5* in method B. In order to compute the Jaccard coefficient and compare clustering results, it is necessary to be able to align different sets. This problem may be solved by computing the Jaccard coefficient for all possible combinations of clusters between A and B. However, computationally when K increases, computing the Jaccard coefficient for this exponentially increasing number of combinations quickly becomes expensive. Consequently, I developed a similarity specificity matrix approach as described in the next paragraph to align the clustering results before computing the Jaccard coefficient.

#### 4.2.2 Alignment via similarity-specificity matrix

The “count” matrix D and the “similarity/specificity” matrix H for comparing two clustering outputs,  $z$  and  $z'$ , each with K clusters, so that  $z = \bigcup_{h \in [1, K]} c_h$  and  $z' = \bigcup_{h \in [1, K]} c'_h$  are defined as:

$$D = \begin{pmatrix} |c_1 = c'_1| & \dots & |c_1 = c'_K| \\ \vdots & \ddots & \vdots \\ |c_K = c'_1| & \dots & |c_K = c'_K| \end{pmatrix}$$

and

$$H_{ij} = \frac{D_{ij}}{\sum_a D_{aj} \sum_b D_{ib}}$$

With  $z$  the set of reference clusters (in the case of the simulation study,  $z$  is the set of “true” clusters obtained after clustering the biological data), for each row of the matrix H, the column with the highest value is selected as the corresponding cluster.

In the case of two sets of clusters being extremely similar the alignment is successful and no information is lost. However some errors

may arise if the two cluster sets are substantially different. For example if one cluster  $h_{z_1}$  in  $z$  is split into two clusters  $h_{z'_4}, h_{z'_5}$  in  $z'$ , the alignment process will assign them both to  $h_{z_1}$ , meaning that, because  $K$  is the same for  $z$  and  $z'$  one cluster in  $z$  will have no corresponding cluster in  $z'$ . In such cases, some information will be lost during the alignment process.

This type of error is very hard to avoid without controlling the initialization of the clustering, which would bias the results. Therefore, the Jaccard coefficient will not necessarily be linearly correlated with the similarity between the reference clusters and the clusters under study, instead it will have a tendency to worsen faster than the dissimilarity due to the alignment step. It remains however a good indicator of the divergence between clustering sets. An example of cluster alignment is shown through the values of  $\Theta$  by comparing Figure 14a and Figure 14b.

Now that I have established a method to compare cluster sets, I need to validate the correct estimation of the model's parameters, as described in the next section.

### 4.3 VALIDATION OF PARAMETERS ESTIMATION AND MODEL SELECTION

#### 4.3.1 Estimation of $\Theta$

To validate the consistency in estimating the values of  $\Theta$ , I compare the “true” values used to simulate the data with the values obtained after clustering the simulated data.

A simple example with  $K = 6$  is presented in Figure 14: each cell of the heatmaps  $HM_{h,h'}$  with  $h, h' \in K$  represents the mean of the vector of absolute pairwise differences  $\theta_{h,m} - \theta_{h',m}$ . Figure 14a shows these values before alignment and Figure 14b after. As expected, after alignment the small values are aligned in the diagonal showing that each cluster  $h'$  exhibits highly similar values of  $\Theta$  compared to its corresponding cluster  $h$  in the reference.

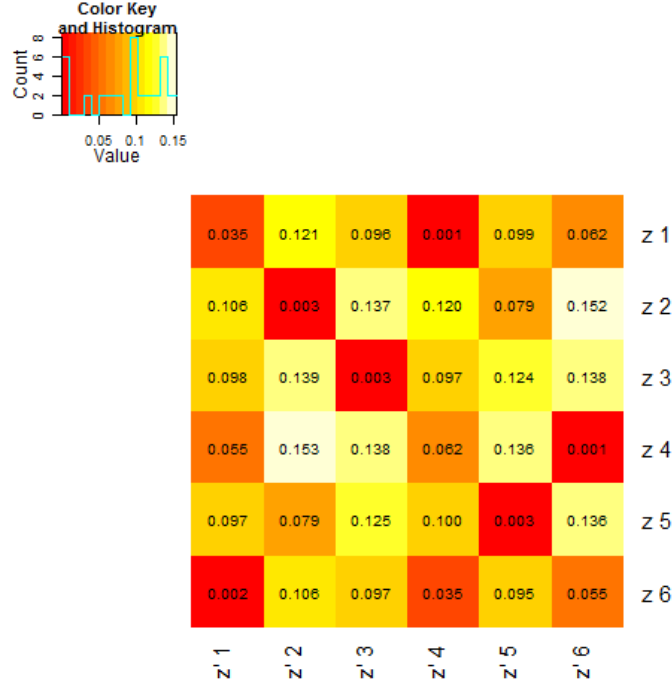
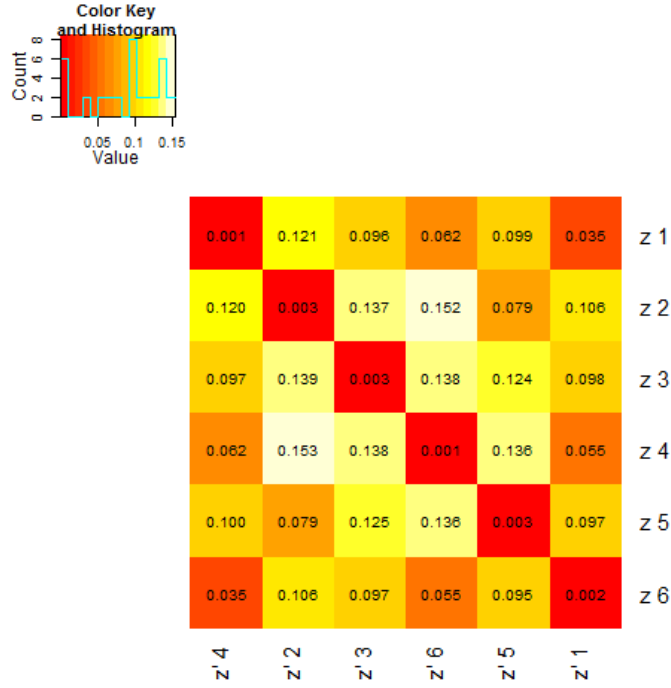
(a) "Proximity" between values of  $\Theta$  before alignment(b) "Proximity" between values of  $\Theta$  after alignment

Figure 14: Validating the estimation of  $\Theta$  for  $K = 6$ . On the x axis are shown the 6 clusters obtained after clustering the simulated data. On the y axis are shown the 6 "true" reference clusters. Each cell of the heatmap corresponds to the mean of the absolute pairwise (with respect to the 86 genes considered) difference between "true" and simulated  $\Theta$  values. A small number means that the difference between the reference  $\Theta$  values and the ones obtained after clustering the simulated data is very small.



It is also interesting to note that comparing the similarity between the inferred and true clusters with the Jaccard coefficient implicitly assesses the accuracy of the estimation of  $\Theta$ : if the inferred and true clusters are identical, the estimates of  $\Theta$  must be equal to the true values. In practice, a Jaccard coefficient of 1 implies perfect agreement. Figure 18 shows the value of the Jaccard coefficient for several clustering methods including the HMRF (red points). The very high value of the Jaccard coefficient suggests that the values of  $\Theta$  are consistently estimated for  $K \in [4, 80]$  (see 4.4 for the full description of Figure 18)

#### 4.3.2 Estimation of $\beta$

To determine how accurately the values of  $\beta$  are estimated, I compare the true and inferred mean values of  $\beta$  for different values of  $K$ , as shown in Figure 15 (red and green dots). I chose to compare the mean values instead of comparing  $\beta$  in a pairwise manner because of the alignment errors described in the previous paragraph. Indeed, for example if one true cluster is split in two after clustering the simulated data, there isn't a simple rule about how the value of  $\beta$  should be distributed between the two resulting clusters. In this context using the mean value allows a consistent comparison of the overall value of  $\beta$ , even though the sensitivity for extreme values is lost.

Analysing Figure 15, I observe that the values of  $\beta$  increase with  $K$ , which is to be expected since more clusters implies the existence of more transition areas (sites where neighbours do not belong to the same cluster). Because the inner spatial structure of the data is conserved regardless of  $K$ , this makes an increase of each component of  $\beta$  necessary to maintain the optimal spatial coherency of the full model.

Interestingly, Figure 15 also shows a slight but consistent underestimation of  $\beta$ . This can be explained by noting that the simulation scheme used may reduce the spatial coherency within clusters. Specifically, as illustrated in Figure 16, clusters may not display homogeneous expression of a given gene: instead. Depending upon the value of  $\theta$ , a gene will be expressed only in a fraction of cells. In reality, the cells in which such genes are expressed may have a coherent spatial structure within the biological cluster that is lost in the simulation, thus explaining the consistently smaller value for  $\beta$  that are

estimated.

To explore this further, I performed a second simulation using the parameter values estimated from the first simulation as a reference. In this context no further loss of spatial coherency was expected, which was indeed confirmed as shown by the blue curve in Figure 15.

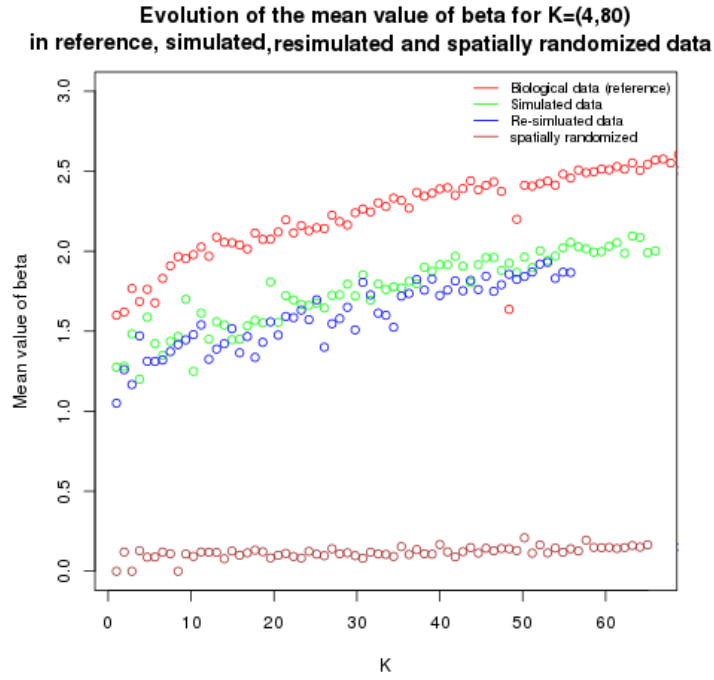


Figure 15: **Validating the estimation of beta.** This Figure shows the evolution for  $K \in [4, 80]$  of the mean value of  $\beta$  across all the clusters. The red dots represent the biological data clustering (i.e the reference in our simulations scheme). The green dots represent the results obtained after clustering simulated data, which shows an underestimation of  $\beta$ . To confirm that this underestimation come from the simulation scheme and not the clustering method, the simulated data was used as the reference to generate a “second generation” of simulated data, suppressing the simulation scheme bias (see Figure 16). The results of this re-simulation are shown by the blue dots, which exhibit no underestimation of  $\beta$ . Finally the brown dots represent the mean value of  $\beta$  on the same simulated data but spatially randomized, as expected the  $\beta$  are now estimated to 0.

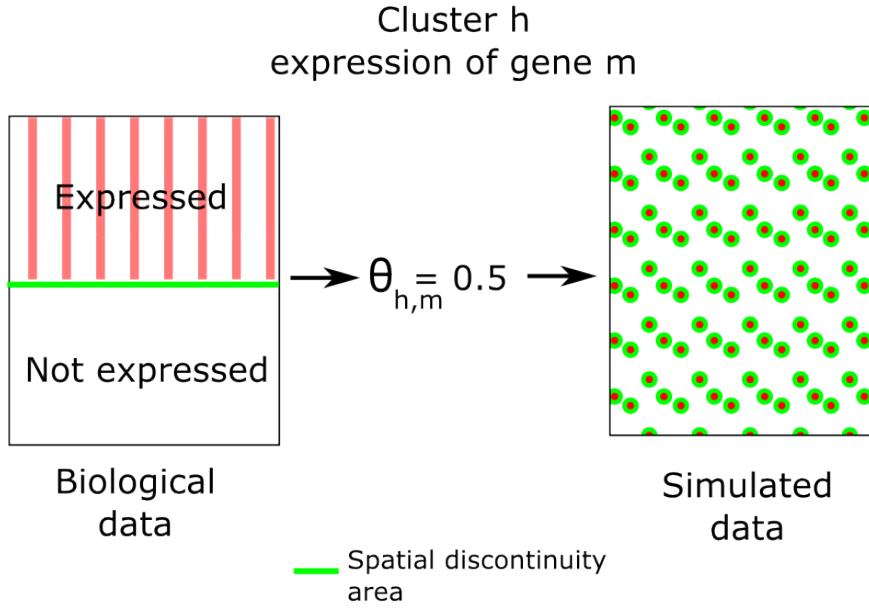


Figure 16: **Decrease in spatial coherency due to the simulation scheme.** For an example cluster  $h$ , gene  $m$  may only be expressed in half of the cells. This will yield  $\theta_{h,m} = 0.5$ . However, in the biological data, the cells expressing gene  $m$  may be spatially coherent (i.e., located close to one another), leading to a reduced area of expression discontinuity (the green line). By contrast, in the simulated data the expression of such a gene will lose its spatial coherency, leading to an increased area of expression discontinuity. The number of cells having a neighbour with some differences in the gene expression pattern is directly linked to the value of  $\beta_h$  through the energy function described in Chapter 3. This explains the underestimation of  $\beta$  observed in Figure 15.

To validate further our estimation of  $\beta$ , I randomized the coordinates of the simulated “cubes” to lose any spatial component before re-clustering the data. As expected, we observed that the estimates of  $\beta$  were very close to 0 for all clusters (Figure 15, brown dots), as well as there being very similar Jaccard coefficient values (relative to the true values) for the independent mixture and the MRF model as shown in Figure 18B. Both of these observations provide confidence in our assertion that the model is able to consistently estimate the values of  $\beta$  and that the spatial component of the model plays an important role in the fit.

### 4.3.3 Choosing $K$

Finally, assessing the ability of the model to choose the correct number of clusters,  $K$  is crucial. To this end, the “true” number of clusters underlying the simulated data  $\hat{K}$  was compared to the inferred value,  $\tilde{K}$  obtained after applying the BIC method (see Chapter 3). The results for two representative choices of  $K$  are shown in Figure 17 and demonstrate that our clustering approach, in conjunction with the BIC, is able to accurately determine the optimal number of clusters.

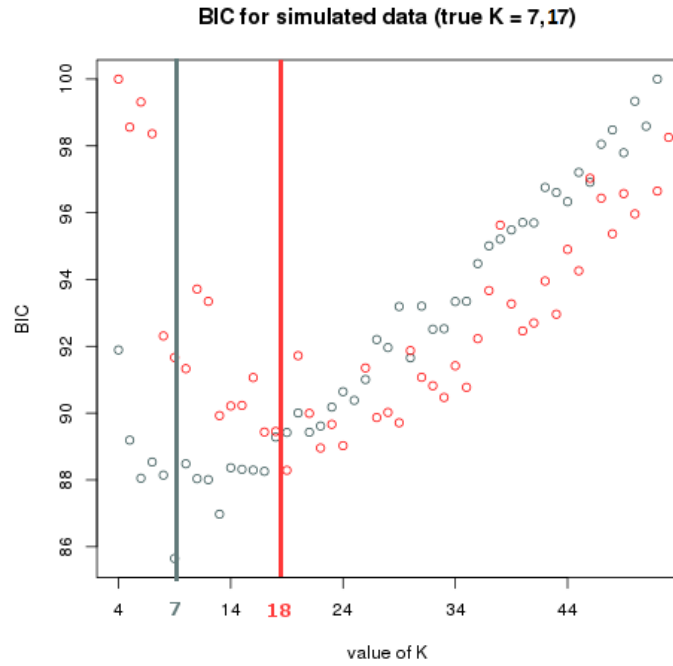


Figure 17: **Estimating the BIC from the simulated data.** The BIC is plotted on the y-axis for different values of  $K$  on the x-axis. The red and the grey points correspond to the BIC estimated when the underlying data have 17 and 7 clusters, respectively. The minimum BIC value is 18 and 7, respectively, suggesting that the MRF approach in conjunction with the BIC accurately estimates the optimal number of clusters.

## 4.4 METHOD PERFORMANCE AND INITIALIZATION

As pointed out previously, initialization is a key step of the HMRF clustering. Working on the simulated data allows a comparison of clustering results generated with a variety of initialization schemes.

#### 4.4.1 *The EM principle and local maximum*

As explained in Chapter 3, the HMRF clustering I developed relies on a Maximum Posterior Marginal (MPM) approach, and the EM algorithm is used to estimate the unknown parameter values. The likelihood function that needs to be maximised may possess a varied set of stationary points. Thus, convergence to the global maximum with the EM algorithm, depends strongly on the parameters initialisation. To overcome this problem, different initialisation strategies have been proposed and investigated (see for instance [11, 64, 81]).

In particular, if the procedure is initialized with a set of clusters that are close to a local maximum in the likelihood function, the EM algorithm will converge to this local maximum and will never reach the global maximum of the model.

#### 4.4.2 *Random initialization vs Hclust initialization*

To shed some light on the initialization scheme issue I compared two theoretically opposed initialization schemes :

- A random approach: 10.000 random initialization were generated for  $K \in [4, 70]$  and for each, the initial likelihood of the model was computed. The initialization with the highest initial likelihood was selected to start the EM algorithm.
- A directed approach: the data were clustered using the non-spatial hClust method described in Chapter 6 and the resulting set of clusters were used to initialize the EM algorithm.

The results are shown in Figure 18 (black and green dots on panel A). Looking at the effect of the initialization scheme on the quality of the resulting clusters via the Jaccard coefficient for  $K \in [4, 70]$  it is clear that, unsurprisingly, considering that the EM algorithm does not guarantee to reach the global maximum, the random initialization scheme performs better than the directed initialization scheme. Indeed, for the HMRF randomly initialized, the average Jaccard coefficient is around 0.8 when it averages only 0.6 when initialized with hClust.

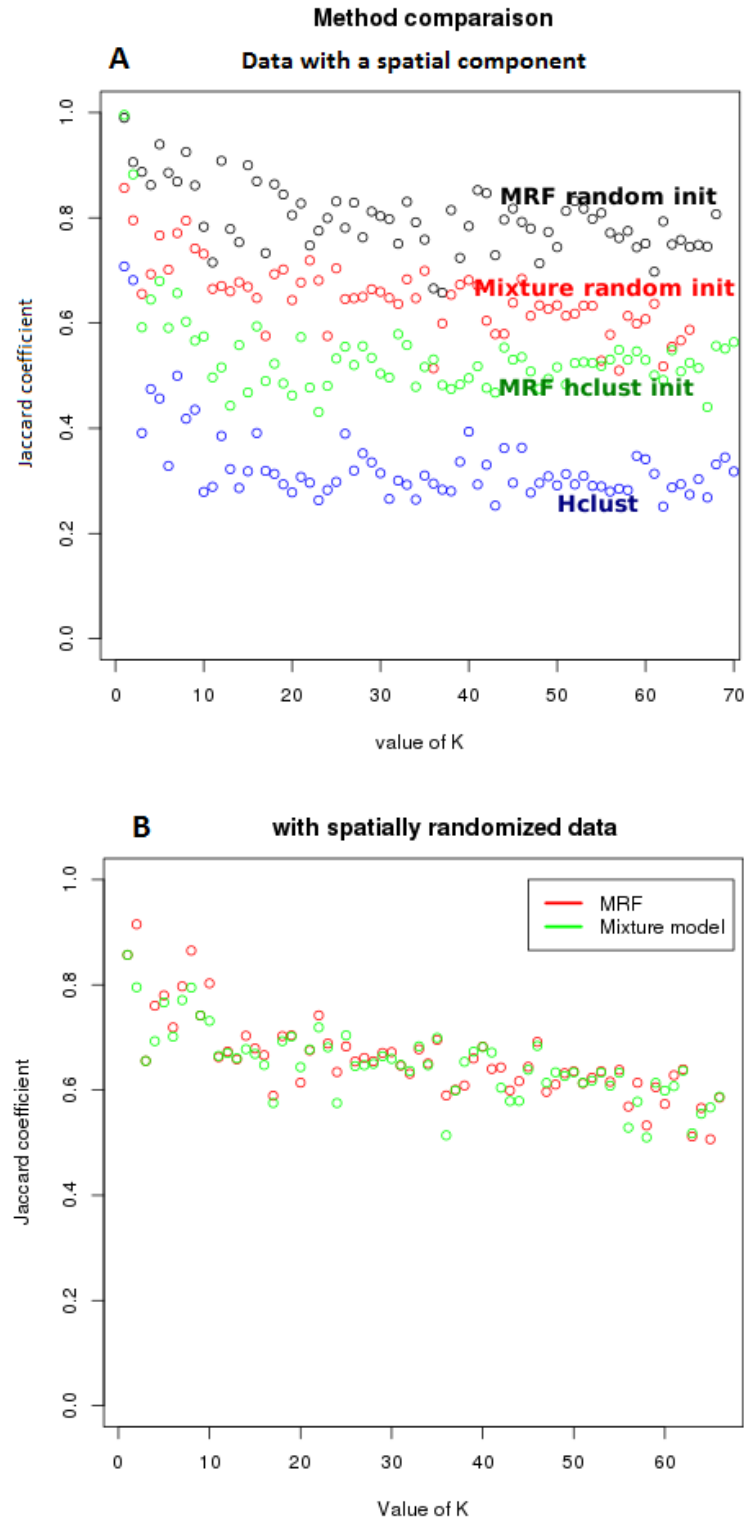


Figure 18: **Jaccard coefficient between true and resulting clusters on the simulated data with different methods and initializations.** Panel A compares the performance of the MRF method with a random initialization with an independent mixture model also with a random initialization, the MRF method initialized with the hClust classification and hClust alone on data simulated with a spatial component. Panel B shows the Jaccard coefficient for the MRF method and independent mixture model both with a random initialization; in this case both methods are applied to simulated data that lacks a spatial component.

Following this observation, for the rest of this thesis and especially in Chapter 5, the HMRF method will be randomly initialized.

#### 4.5 METHOD PERFORMANCE COMPARED TO HCLUST AND INDEPENDENT MIXTURE MODELS

Because the simulated data provides a clear set of true clusters and parameter values, it allows the HMRF clustering to be compared to other clustering methods in terms of clustering quality via the Jaccard coefficient. Additionally, computing time being a key factor for large datasets, I provide in this section some key figures about the execution time of the different methods.

##### 4.5.1 *Quality of the clustering results*

The resulting Jaccard coefficients obtained by comparing the true clusters and the clusters generated by different approaches are shown in Figure 18 for  $\tilde{K} \in [4, 70]$ . The HMRF method, when used with a random initialization scheme, has an average Jaccard coefficient of 0.8, and clearly demonstrates better performance than the other methods. The second best performing method is the independent mixture model with a random initialization, which has an average Jaccard coefficient of 0.7. Since the independent mixture approach is equivalent to the MRF with all the  $\beta$  parameters set to zero (i.e., without a spatial component) this suggests that accounting for the spatial aspect yields improved results. hClust also performs relatively poorly with an average Jaccard coefficient around 0.4.

Although as mentioned previously, the Jaccard coefficient may not be linearly correlated with the quality of the clustering results because of the alignment step which can create biases, this simulation study shows that the HMRF consistently outperforms the other methods tested.

##### 4.5.2 *Computing time*

I have demonstrated in the previous paragraph that the HMRF clustering method yields better results in terms of clustering than the other tested methods. However, the fact that the method takes into consideration the spatial dependencies between data points means

that it will be computationally more expensive than non spatial methods, especially as the number of sites increases.

The number of clusters  $K$  also has an important influence on the computing time. Given a fixed number of sites  $S = 32.203$ , I ran the HMRF, and the mixture model methods on simulated datasets for  $K \in [4, 60]$  and have obtained, the computing times shown in Figure 19 (on the same machine).

Because of the necessity to estimate every component of  $\beta$  at every step through a gradient ascent algorithm (see Chapter 3), and the increased complexity of computing the likelihood of the model when  $K$  increases, it is unsurprising to see that the HMRF approach necessary computing time has an exponential relationship with  $K$ . On the other hand, the independent mixture model approach does not need to perform these calculations, and exhibits a linear evolution. However, as seen in the previous paragraph, the spatial component of the model seems to improve the clustering quality significantly. Consequently, the HMRF approach might prove useful when  $K$  is relatively low. Indeed, until  $K = 30$  the required computing time required for the HMRF is not dramatically higher compared to the mixture model approach. In practice, this is likely to be the case as complex biological tissues are not made of hundreds of sub-tissues.

The computing time required for hClust is quite high as shown is Figure 19 (blue line), but is constant for any number of clusters  $K \in [2, S]$ . Indeed, once the dendrogram is computed (see Chapter 6), cutting the clustering tree to any number of clusters is trivial. It is also interesting to note that the clustering results for all values of  $K$  are computed in one run with hClust when the other methods need a full run for each value of  $K$ . Although I have shown in Figure 18 that the clustering performances of hClust are clearly below those of the HMRF and the independent mixture models methods, the fact that the results for all values of  $K$  are obtained at once, regardless of the relatively high computing time, might be advantageous in some cases.



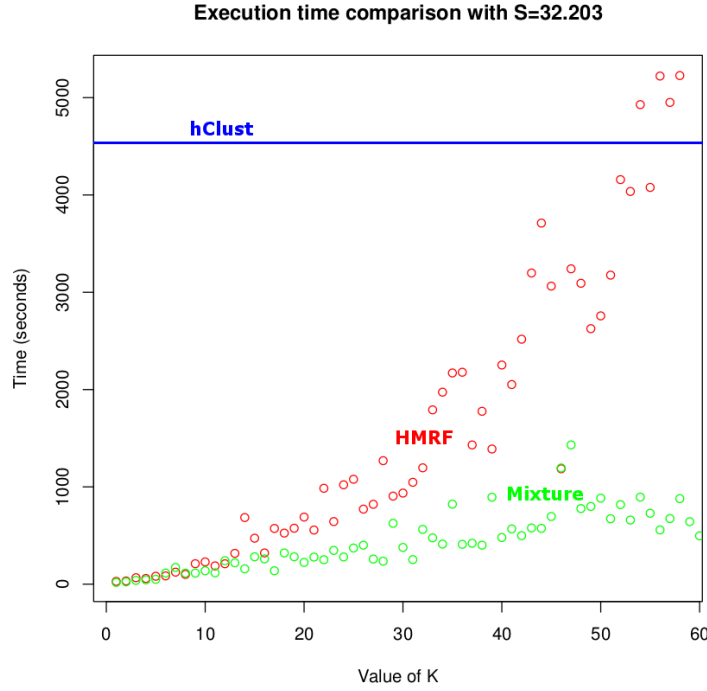


Figure 19: **Computing time required by different clustering methods for**  $K \in [4, 60]$  On the x axis is shown the value of K used to cluster the 32.203 data points. The red dots represent the computing time required by the HMRF method, the green dots by an independent mixture model approach and the blue line for hClust.

#### 4.6 SUMMARY

In this Chapter, I have presented the simulation study conducted to evaluate the performances of the HMRF clustering method described in Chapter 3. First, I have described the method used to simulate data with known spatial characteristics. Subsequently, I validated that all the parameters of the model were estimated correctly and consistently by the EM algorithm. I then discussed the performance of the method regarding the initialization scheme, and concluded that a random initialization yielded the best results. Finally I used the simulated data to compare the performances of the HMRF method compared to other clustering methods, the result of which was that even though the method is quite costly in terms of computing time when the number of clusters increases, it clearly outperforms both the independent mixture model and the hClust clustering methods in terms of accuracy.

Having validated the method, I will present in the next Chapter the results obtained when the HMRF clustering was applied to the single cell in-situ hybridization data described in [Chapter 2](#).

## HMRP CLUSTERING IN THE BRAIN OF *PLATYNEREIS DUMERILII*

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### 5.1 CHOOSING K WITH THE BIC ON BIOLOGICAL DATA

After validating the HMRP method using simulated data as detailed in Chapter 4, I now present the clustering results when the method is applied to the single cell expression dataset generated from the brain of *P. dumerilii*. Before interpreting the biological meaning of the inferred clusters, the first step is to choose K. To this end, as presented in Chapter 3 I applied the BIC method.

However, as shown in Figure 20 (grey dots), the BIC does not reach a clear minimum but instead reaches a plateau after a given number of clusters. This is most likely due to the highly, but not perfectly symmetrical nature of the brain: with a small K, the same “tissue” on both the left and the right hand side of the brain will belong to the same cluster. However, because the two sides of the brain are not perfectly symmetrical, as K increases the left and right part of the same “tissue” will be clustered separately. As a result, the likelihood continues to increase sufficiently to explain the flattened BIC curve.

Moreover, this hypothesis seems to be confirmed by the fact that when computing the BIC on the right and left side of the brain separately, the curve has in both cases a clear minimum as shown in Figure 20 (red and green dots). Given this, I opted to choose K as the point where the BIC curve reaches a plateau, that is when the derivative of the BIC curve become 0. I chose the start of the plateau stage if the BIC because, assuming the symmetry issue explained before, the BIC will reach a stable value when the cells on both sides of the brain are classified in the optimal number of clusters while conserving the left/right symmetry of the brain. *Consequently for the rest of the Chapter, I considered the clusters identified for  $K = 33$ .* Importantly, the BIC starts to rise after  $K = 66$ , which seems to confirm, assuming the symmetry hypothesis described above, that  $K = 33$  is a sensible choice.

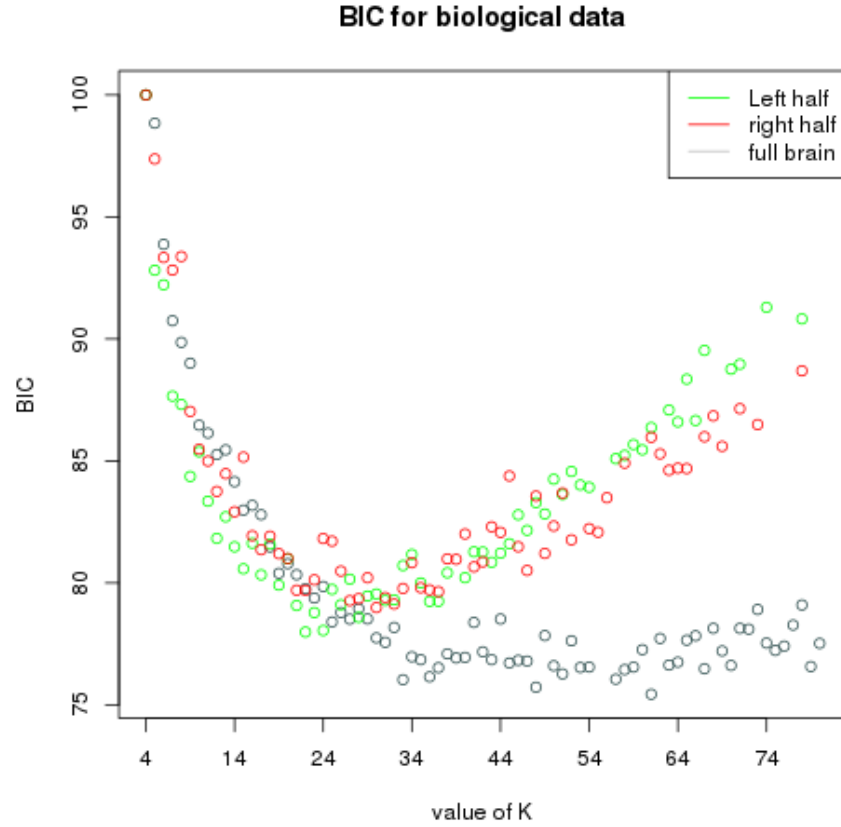


Figure 20: **BIC results on biological data.** Results are shown for  $K \in [4, 80]$  (x axis) with the full brain, and for the left and right half separately. The y axis shows the BIC value as a % of the highest BIC value for each dataset.

The main output of the method is a list of  $S = 32.203$  cluster assignments, that is, the cluster each “cube” of the in-situ hybridization data belongs to. With this output and the spatial coordinates of each cube, it is easy to use the bioWeb3D tool presented in Chapter 6 to visualize the clusters in the brain. However, downstream analysis solely based on the spatial localization of the clusters is insufficient, and it is possible to take advantage of the model’s output parameter values to analyse and interpret the biological meaning of the resulting clusters.

## 5.2 PARAMETER INTERPRETATION

The parameter  $\Theta$  can be used to shed light on the biological meaning of the inferred clusters. As described in the previous chapters, for  $h \in K$  and  $m \in M$ ,  $\theta_{h,m}$  is the probability that gene  $m$  is expressed in

a given cell contained in cluster  $h$ . Therefore, the values of  $\Theta$  provide a link between the mathematical model and downstream biological interpretation.

However, in practice, not all of the 86 genes will provide insight into the biological function of a given cluster. For instance, in the case of a ubiquitously expressed gene,  $g$ , the value of  $\theta_{h,g}$  will be high for all clusters. To overcome this problem, I developed a score,  $S$ , for each gene,  $m$  and each cluster  $h$ , where:

$$s_{hm} = \frac{\theta_{h,m}}{\sum_a \theta_{a,m}}.$$

For each gene,  $m$ , and cluster,  $h$ ,  $s_{hm}$  is large if gene  $m$  is specific to cluster  $h$ . Consequently, the top scoring 3 or 4 genes for each cluster will represent a specific stereotypical expression pattern that will help infer or confirm the identity of the functional tissue represented by each cluster.

### 5.3 FINDING KNOWN BIOLOGICAL STRUCTURES TO VALIDATE THE METHOD

To validate the downstream analysis approach presented, I first considered some well characterised regions within the *Platynereis* brain.

#### 5.3.1 *P. dumerilii's eyes*

Arguably the best-studied regions of the brain in *Platynereis* are the eyes: the brain has 4 eyes, two larval and two adult, and their locations and expression fingerprints are well known. As shown in Figure 21, our approach generates two spatially coherent clusters that correspond to each of these regions. Importantly, the best scoring genes that characterise these clusters are biologically meaningful: *rOpsin* and *rOpsin3*, both members of the well-described *opsin* family of photosensitive molecules [117, 103], best distinguish the adult eye and larval eyes respectively, consistent with the in-situ data images shown in Figure 22.

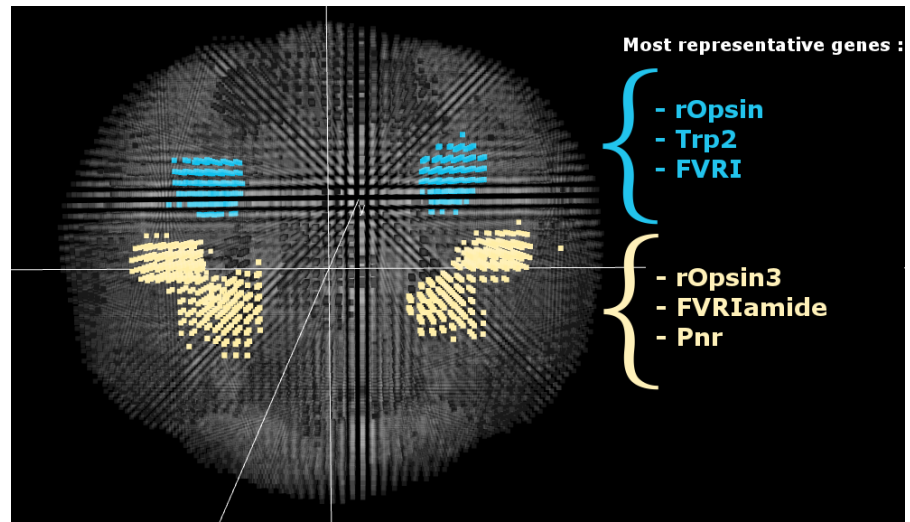


Figure 21: Eyes in the brain of *Platynereis* as clustered by the HMRF method. Adult (blue cluster) and larval (yellow cluster) eyes in separate clusters with their top 3 most representative genes.

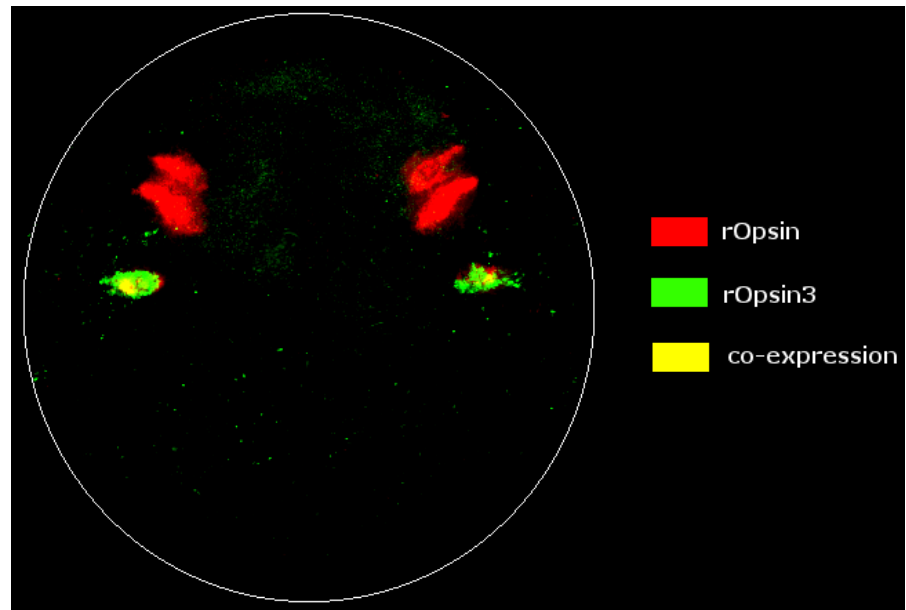


Figure 22: In-situ hybridization image for rOpsin and rOpsin3 in the full brain at 48hpf (Apical view). Z-projection of the expression of rOpsin (red) in both the adult eyes and the larval eyes, rOpsin3 (green) specifically in the larval eyes and co-expression areas in some areas of the larval eyes in the full brain of *Platynereis* at 48hpf. The white circle is a schematic outline of the brain. This image been obtained directly from the data published in [120].

### 5.3.2 Mushroom bodies

As well as the eyes, a second region of the *Platynereis* brain, the mushroom bodies (which corresponds to the pallium, a layers of neurons that cover the upper surface of the cerebrum in vertebrates [120]), are also clearly identified by our approach (Figure 23). They have been described anatomically and molecularly in *P. dumerilii* in [120]. In this paper the authors define the mushroom bodies as a ventral regions, define by a subset of the expression pattern of gene *BF1* and by the same genes as the top scoring genes that define my cluster, *Emx*, *Wnt8*. As shown schematically in Figure 24 from [120], the localization of the mushroom bodies (MB) is coherent with the inferred cluster in Figure 23.

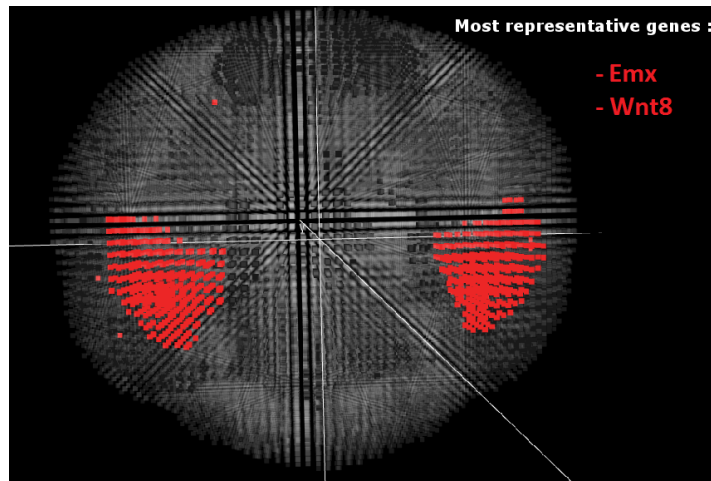


Figure 23: **Mushroom bodies in the brain of *Platynereis* as clustered by the HMRF method.** Mushroom bodies and their most representative genes.

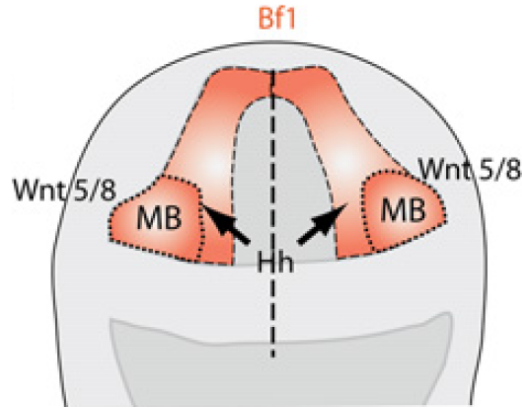


Figure 24: **Schematic representation of the mushroom bodies in the brain of *Platynereis* by [120].** MB: mushroom bodies

### 5.3.3 Motor regions

Experimentally, when the brain is dissociated from the rest of the larvae, the most basal part contains the developing motor regions. These motor regions are clustered together as shown in Figure 25. Indeed, the green cluster defines a region on the basal side of the larvae that can be associated both by its localization and by its most representative genes (*MyoD* [127, 84] and *LDB3* [66, 80]) with the starting point of the developing muscles of the adult animal. *MyoD* has been shown to play a key role in the differentiation of muscles during development in vertebrates and invertebrates [127, 84] and *LDB3* codes for the protein LDB3, which interacts with the myozenin gene family that has been implicated in muscle development in vertebrates [80].

Again, it is possible to cross-validate the function of this region against previous studies. In this case, [40] used muscle specific phalloidin staining at 48hpf to visualize the developing motor region in the larvae's brain, the result of which is reproduced from [40] in Figure 26.



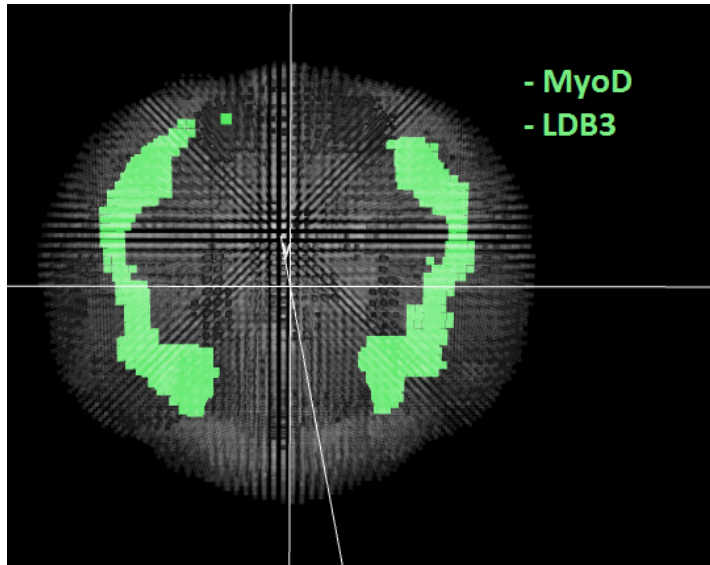


Figure 25: **Developing motor region in the brain of *Platynereis* as clustered by the HMRF method.** Basal motor regions and their most representative genes.

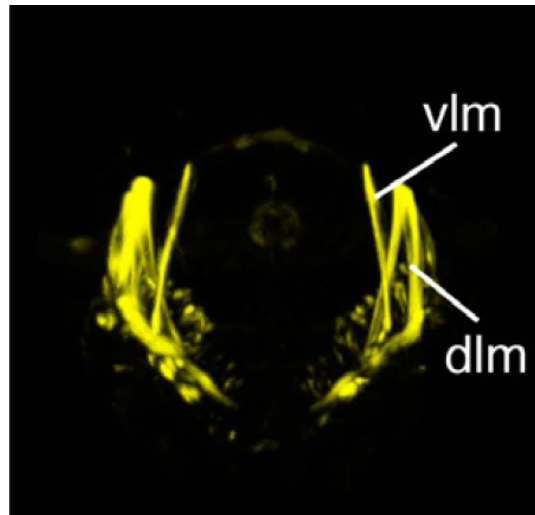


Figure 26: **Developing motor region in the brain of *Platynereis* visualized in-situ by phalloidin staining.** This Figure is reproduced from [40]. vlm: ventral longitudinal muscle; dlm: dorsal longitudinal muscle.

The eyes, the mushroom bodies and the developing motor regions validation provided good confidence that the HMRF method yielded sensible results and that the gene scoring developed was able to successfully define a specific gene expression fingerprint for each cluster. However, of the  $K = 33$  clusters, some of the defined regions are not easily recognizable when compared against the known biology of *P.*

*dumerilii*. These regions are very interesting as they may represent previously unstudied sub-populations of cells in the brain.

#### 5.4 GENERATING FUNCTIONAL HYPOTHESES ABOUT UNKNOWN BIOLOGICAL TISSUES

As well as identifying clusters corresponding to known cell types, I also identified clusters that might correspond to less well studied sub-types with specific biological functions.

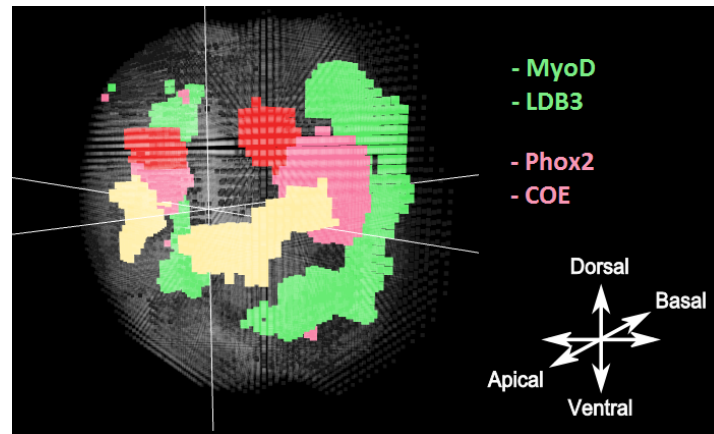


Figure 27: **A putative tissue of developing neurons between the eyes and the larvae's developing muscles.** The yellow and red clusters are the eyes as seen in Figure 21. The green cluster represents the developing muscles on the basal side of the larvae, as the location and the most specific genes strongly suggest. The pink cluster is a putative tissue that makes an interesting link between the eyes and the muscles. The most representative gene of this tissue is *Phox2*, a homeodomain protein required for the generation of visceral motor-neurons in *Drosophila* [15]

Given the location of the eyes (Figure 21) and the developing muscles (Figure 25), the location of the pink cluster in Figure 27 is interesting. This cluster surrounds the larval eyes, the adult eyes and reaches the developing muscles described above. Looking at the most representative genes for this pink cluster, it is interesting to note the presence of *Phox2*, a homeodomain protein that has been shown to be necessary for the generation of visceral motor-neurons (neurons of the central nervous system that project their axons to directly or indirectly control muscles) as described generally in [16] and in *Drosophila* [15]. The second most representative gene, *COE*, has also been shown to play a role in *Platynereis* and *Drosophila* neural tissue development

[27]. In this context, although we lack biological validation, we can hypothesise that the cells within this particular cluster could be developing neurons that link the eyes to the muscles of *Platynereis*.

Although this hypothesis remains purely speculative and would need validation in the laboratory, this example is an interesting proof-of-concept that this clustering method can prove useful for hypothesis generation. Indeed, the analysis of the parameter values and the spatial localization attached to the clusters has allowed me to place with a reasonable level of confidence a functional hypothesis about a tissue that was not clearly defined either spatially or functionally.

## 5.5 METHOD SENSITIVITY COMPARED TO OTHER CLUSTERING METHODS

To complement the comparison work described in Chapter 4, I decided to assess, for the biological tissues outlined in the previous paragraphs, the sensitivity of the HMRF method compared to the independent mixture model EM and to hClust.

In Figure 28 are shown the clusters obtained with the hClust method. Some of the regions are conserved across clustering techniques, in particular the eyes. however the hClust results are much less precise than those of the HMRF method. In particular the both the adult and the larval eyes are clustered alongside a second region that has no biological meaning (red and yellow cluster in Figure 28). Furthermore, the developing muscles are not picked up at all by hClust.

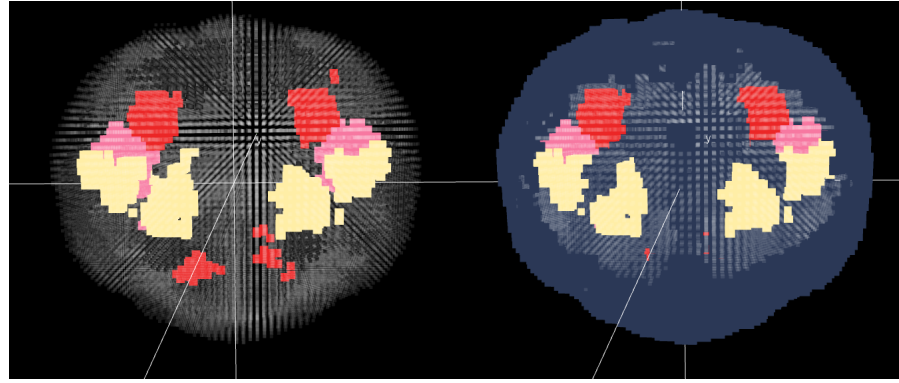


Figure 28: Clusters obtained with hClust after alignment onto the MRF results. The Adult eyes are well isolated (red) although a region in the ventral part of the brain is classified in the same cluster which is biologically nonsensical. The larval eyes (yellow) are also picked up but along side a second region. Finally if hClust picks up a part of the putative tissue of developing neurones described above (pink), it does not find the muscles at all. Instead the region where the muscles are found by the HMRF method is part of a large cluster of cells forming a layer around the brain (purple cluster on the right).

In Figure 29 are shown the clusters obtained with the independent mixture model method. It is generally closer to the results obtained with the HMRF. However, the resulting picture is extremely noisy. Furthermore, for the muscles region, this noise is linked to biological imprecisions. Indeed, contrary to the cluster outputted by the mixture model method, as shown in the in-situ staining presented in Figure 26, biologically, *P. dumerilii*'s larvea at 48hpf does not present a either a dorsal or ventral region in the middle of the symmetry axis.

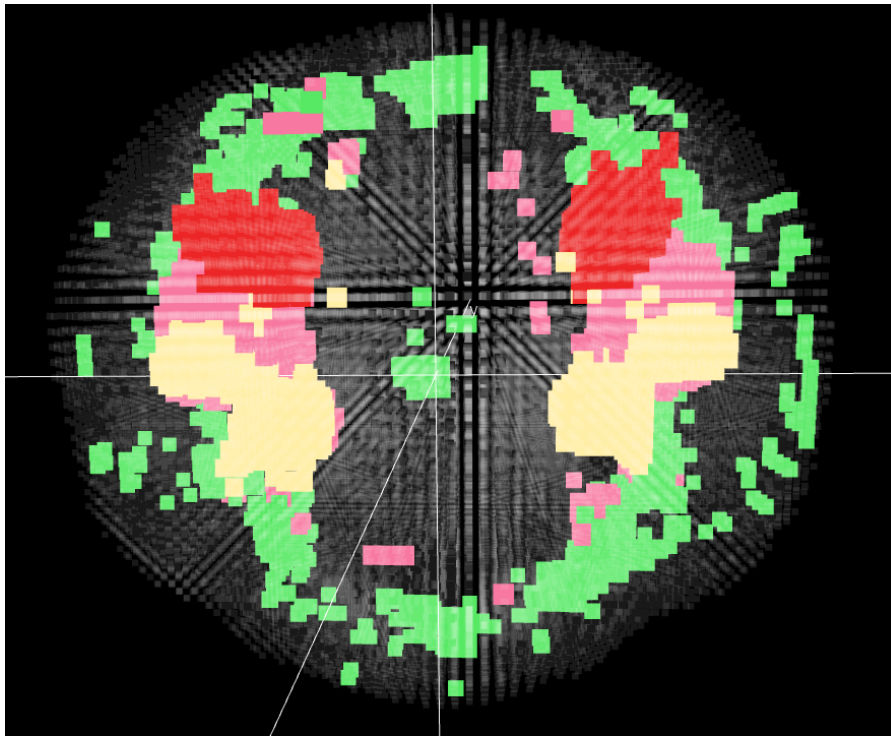


Figure 29: Clusters obtained with the independent mixture model with the same initialization as the one used for the results presented in the paragraphs above for the HMRF. The Adult eyes are well isolated (red). The larval eyes (yellow) as well. The muscles and the region of potential developing neurons are picked up as well. However if all the regions are recognizable, they are extremely poorly defined spatially with a lot of noise and little spatial coherency. In the case of the muscles, when comparing with the in-situ imaging in Figure 26, it is clear that the HMRF results are closer to the biological reality as there is no fully dorsal or ventral regions in the developing muscles.

## 5.6 SUMMARY

I applied the HMRF clustering method described in Chapter 3 to the binarized in-situ hybridization data presented in Chapter 2. I described how the BIC method was adapted to chose the optimal number of clusters  $K = 33$ .

In order to analyse the resulting clusters, I developed a scoring method based on a “specificity” matrix which extracts the most specific genes for each cluster. Thanks to the 3D visualization tool described in Chapter 6, and the most specifically expressed genes for each cluster, I was able to validate the method biologically by localiz-

ing 3 well studied regions of the brain. Additionally I confirmed that the top 3 genes were consistent with the known biology of *P. dumerilii*.

Furthermore, I demonstrated how my approach allows the generation of functional hypotheses about regions that are not well known. In particular, I discussed a previously unstudied tissue that may consist of developing neurons directly linking the eyes to the developing muscles.

The work described in Chapters 3, 4 and 5 has been published in September 2014 [99].

## VISUALIZING TISSUES FROM 3D SINGLE CELL EXPRESSION DATA

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### 6.1 VISUALIZING CLUSTERING RESULTS IN 3D WITH BIOWEB3D

#### 6.1.1 *Background*

Visualisation is a key challenge in the analysis of large biological datasets, especially when dealing with organized structures with distinct sub-clusters [106]. This is particularly important when analysing 3-Dimensional (3D) datasets. When a biological process or feature has been described spatially by a set of 3D referenced points, either via laboratory work (confocal microscopy for example) or generated within a simulation, with some data attached to each point in space, the first step in interpreting the data is to visualise it. Once the data are visualised and their quality assessed, downstream analysis can proceed. For example, a typical second step is to cluster the observations into different classes based upon the information associated with each point; those results will also need visualisation.

While various 3D visualisation tools have been developed, they have typically been made available via a locally installed piece of software such as BioLayout Express<sup>3D</sup> [41], Arena3D [94], 3D Genome Tuner [124], Amira 3D [112], V3D [95], the Allen Brain Atlas [71] or Cytoscape [107]. These tools are very complete and usually complex to operate for non-expert users. Moreover, they require installation on every machine they are used on, which makes sharing inconvenient. To address this issue, some 3D visualisation tools have been built online and are accessible through the browser directly, such as AstexViewer [49], which is utilised by the Protein Databank Europe via a Java Applet. More recently, visualisation tools developed using HTML5/WebGL capabilities have been described, although they have focused on very specific applications, such as analysing radiology data [67].

Importantly, before bioWeb3D [98], no tool has allowed biologists to view their own 3D data directly online in an easy, fast, interactive

and secure way. Using WebGL and the JavaScript 3D library Three.js, bioWeb3D aims to be a simple, generic tool for tackling this problem.

### 6.1.2 Implementation

bioWeb3D allows the user to represent any 3D dataset on their browser by defining only two files. The two files can either be formatted as JSON or XML files, two widely used structured formats on the web [128], or directly as Comma Separated Values files (CSV).

The first file used by the application, referred to as the *dataset file*, contains the spatial coordinates of every point in the dataset. The second type of file used, the *information layer* file, describes one or several information layers that are associated with every point defined in the first file. For example, if each point defines the location of a cell within a tissue, the second file could describe whether a particular gene is expressed in each cell. That way the tissue expression profile can be represented in the spatial context of the tissue.

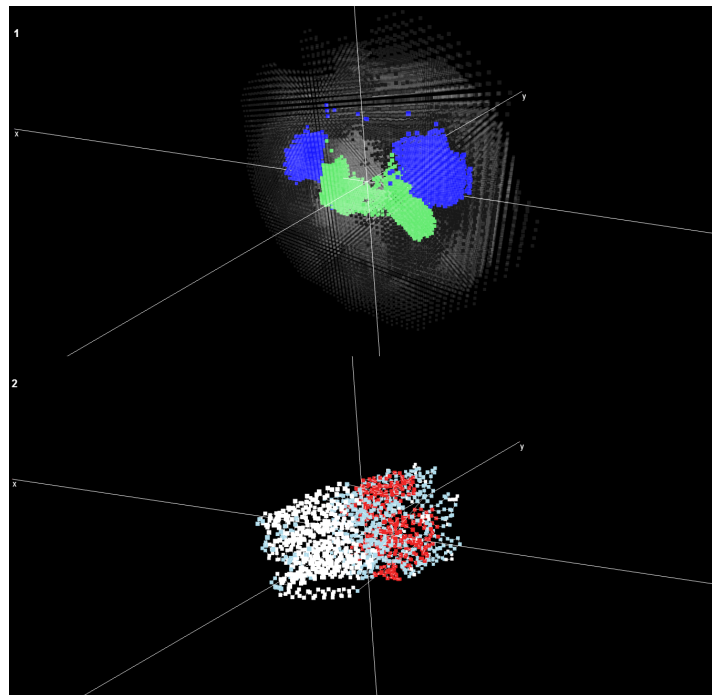


Figure 30: bioWeb3D allows several datasets to be visualized at the same time in up to 4 different “worlds”



Datasets can be viewed and compared in up to four “worlds” (each world refers to a separate visualisation sub-window) at the same time (see Figure 30). Although browser based, the application, fully written in Javascript, does not need to send any data to the host server. Instead, the modern internet browser’s local file system reading capabilities are used through the HTML 5 FileReader functionality. This allows the application to handle, in a very short period of time, large datasets while ensuring that the privacy of the data is maintained.

bioWeb3D is fully written in HTML/Javascript. It relies heavily upon a relatively recent 3D javascript library called Three.js [19]. This library is used as the main interface between WebGL (cross-platform, royalty-free web standard for a low-level 3D graphics API) [42] and javascript. More specifically, bioWeb3D allows the generation and manipulation of simple Three.js objects. Indeed the primary challenge associated with the creation of bioWeb3D has been to design interactions between the 3D visualisation and the user interface in the most efficient way.

Although the focus is on making bioWeb3D simple and easy to use, some options are available to customise how datasets are represented. The application can be used to visualise sequential information, such as 3D protein structures, in which case a solid line can be drawn between the points (Figure 30 (bottom)). In other situations, such as when a population of cells is considered, the points are viewed as individual particles. The information layers are visualised by colouring the 3D points according to the class that each point belongs to.

The 3D data are rendered using simple 2D quadrilaterals positioned in the 3D space according to their coordinates. This simple technique has been selected to keep bioWeb3D as light-weight as possible whilst ensuring good quality visualisation performance and fluidity.

JSON is the recommended format to input files into bioWeb3D because of its rigorous structure and its fast object generation, which is directly built into all of the primary internet browsers’ interpreter. Compared to other data-interchange languages, such as XML, JSON is also easily human readable thanks to a light-weight syntax.

However, some applications might output data only in an XML format and not JSON, as the latter is generally more web oriented. For this reason bioWeb3D can also accept XML as an input format.

Furthermore, much data generated in the biological sciences is stored within CSV files. Converting CSV documents to the JSON or XML format is not always trivial. In order to facilitate this process, the application is also able to directly render simple CSV files that follow a certain format as an input. The file formats to input data into bioWeb3D are described with examples in [Appendix A](#).

### 6.1.3 Results

The goal of bioWeb3D is to allow scientists unfamiliar with visualisation software to explore 3D data very quickly without having to install any software. To illustrate its utility I used bioWeb3D to visualize some preliminary results within the single cell gene expression data of *P. dumerilii*'s brain. In the context of bioWeb3D, the locations of the “cubes” are used to generate the “Dataset” file and information about the sets of cells that define clusters with similar gene expression profiles are used to generate the “Information Layer” file. In [Figure 31](#) the results are illustrated — each point represents a pseudo-cell and its colour indicates the class (or cluster) to which it belongs to, here only two clusters are highlighted.

bioWeb3D can be used to visualise datasets derived from a wide variety of biological assays. Examples are shown on the Github wiki [\[96\]](#), where a 3D representation of a Principal Component Analysis (PCA) carried out with R and the 3D structure of a protein extracted from the PDBe database are displayed.

More generally, the user can interact with the visualisation via an interface on the right of the screen, which contains three panels as shown in [Figure 32](#). In the “dataset” panel, the user can choose the *datasets* and *information layer* files that should be represented in each world. This panel also allows the user to show/hide specific classes of the selected information layers. Each dataset file entered will create a new sub-panel where the user can input *information layer* files for that world. Selecting an *information layer* in the drop-down list will display the data in the current world and generate a list of classes that the user can modify regarding their visibility and colour. The “View”

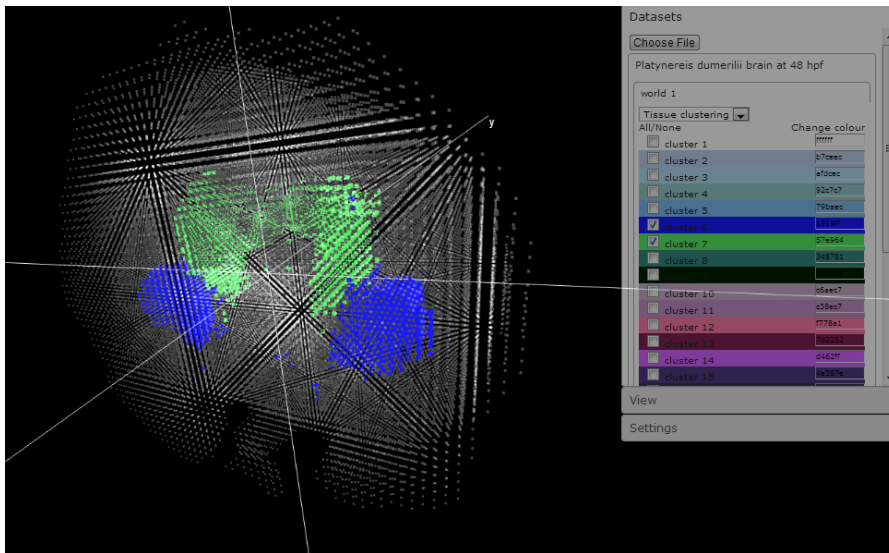


Figure 31: The 3D location of cells within the brain of the marine annelid *Platynereis dumerilii* is shown. Two classes are displayed (in green and blue) along with the shadow of the remaining cells. The User interface is visible on the right of the screen and can be hidden. See 1 for a presentation of *P. dumerilii* and Chapter 2 for detailed presentation of the data.

panel enables the user to choose which of the worlds are shown on the screen, ranging from 1 to 4. Finally, the “Settings” panel provides the user with a number of options that affect all worlds and all datasets, such as modifying the axes scales, modifying the transparency and size of raw data points and information layer coloured points. The user can also choose to enable centering of the data around 0 or leave the coordinates as inputted.

#### 6.1.4 Discussion

Many 3D visualisation software tools, most of which require local installation, exist and provide similar functionalities with standard 3D format input such as Wavefront .OBJ. Some are extremely generic and powerful like Blender or Amira 3D. However, these tools are not typically oriented towards a scientific audience. Moreover, those that are more focused on science are often targeted towards a very specific application, especially in the medical sciences [124]. In this context, I believe that bioWeb3D can be useful as it is completely generic and browser based. It should also be noted that recent browser improvements regarding GPU acceleration through the WebGL paradigm al-



Figure 32: The three control panels to control visualization in bioWeb3D.

A: the datasets panel, where new datasets and new information layer files can be inputted. From the dataset panel, information layers can be selected and unselected, and datasets attached or detached from the “worlds”. B: the view panel where the user can choose the worlds to display. C: the settings panel where the user can customize visualization.

low bioWeb3D to visualise several hundred thousand points. Additionally, local software is usually platform specific, which is not the case for browser based applications.

As mentioned previously, browser based 3D visualisation tools currently exist mainly in the form of Java Applets. This technology has attracted much criticism in 2012 regarding security flaws, leading the “United States Computer Emergency Readiness Team” to advise that all Java Applets should be disabled due to current and future Java vulnerabilities [121]. The development of WebGL technology is viewed by many as a candidate for replacing Applets.

The main current limitation of a WebGL based application is the machine and browser compatibility. Only computers with fairly recent graphic cards will be able to run a 3D environment. It should also be noted that Microsoft has notified the developer community that Internet Explorer is not scheduled to support WebGL in the near future. However, importantly, Chrome, Firefox, Safari and Opera all now support WebGL applications. Moreover, WebGL is also supported on mobile platforms such as iOS or Android [32].

As a fully open source software, the source code for bioWeb3D is available on Github [96], a web platform that allows interested parties

to collaborate on the development of the project. In the wiki page “Contribute to bioWeb3D”, directions to alter or add capabilities to bioWeb3D are provided for users who wish to get involved.

#### 6.1.5 *Conclusions*

bioWeb3D is designed to be a simple and quick way to view 3D data with a specific focus on biological applications. Being browser-based, the software can be easily used from any computer without the need to install a piece of software. Importantly, bioWeb3D has been designed to offer a very straightforward and easy-to-use working environment. Despite current limitations in terms of compatibility or rendering performance for large numbers of points, I believe that bioWeb3D will enable non-experts in 3D data representation to quickly visualise their data and the information attached to it in many biological contexts, thus facilitating downstream analyses.

#### 6.1.6 *Availability and requirements*

The full source code is available on the Github page of the project [96]. A live version of the software is online [97]. You will require a graphical card and a browser with WebGL capabilities to run bioWeb3D.



## SPATIAL BACK-MAPPING OF SINGLE CELL RNA-SEQ DATA

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### 7.1 SINGLE CELL RNA SEQUENCING, BUILDING A MAP OF THE FULL TRANSCRIPTOME

#### 7.1.1 *Single cell RNA sequencing*

The scale shift from tissue to single cell is harder to achieve for RNA-seq than for in-situ hybridization assays. As described in the Introduction 1.2, an important factor for the success of RNA-seq assays is the input quantity of RNA to be sequenced. Taking mammalian cells as a reference, the quantity of RNA depends a lot on the cell type considered and can vary between 10 and 50 pg per cell, only 2% of which is mRNA [55, 57]. With such a small input quantity, distinguishing biological variation between different cells from the technical variation linked to mRNA capture rates and to cDNA amplification protocols is extremely challenging.

However, with the creation of new protocols [102, 115], and the rise of microfluidics approaches that facilitate the extraction and sequencing of single cells [91], the last couple of years have seen a dramatic increase in the number of single cell RNA-seq based studies [58, 76, 131, 111, 30]. However, challenges still need to be overcome in order to analyse further complex tissues using such approaches.

#### 7.1.2 *Technical noise in single cell RNA-seq data*

Single cell RNA-seq is also prone to high levels of noise. This technical noise is caused by the minute amounts of starting RNA material. A study led by Philip Brennecke, Simon Anders and Jong Kyoung Kim [14], proposes a statistical method to overcome this high noise level and distinguish between biological variation and technical variation in the gene expression levels.

To illustrate the dramatic increase in noise level, they used a series of dilution assays, reducing step by step (5000 pg, 500 pg, 50 pg, 10 pg) the input quantity of RNA fragments extracted from total *Arabidopsis thaliana* RNA with two technical replicates each time using the single cell RNA-seq Tang protocol [115]. The authors of the study let me analyse this data, and after normalizing by the size factor using the Bioconductor package DESeq [1] the scatter plots shown in Figure 33 were generated.

It is clear from these dilution assays that the noise level is correlated with the input quantity. Even though highly expressed genes are consistently well quantified even with 10 pg input material, for most of the genes, with less than 50 pg input RNA it seems dangerous to assume the results of single cell RNA-seq as quantitative with the current technological capabilities.

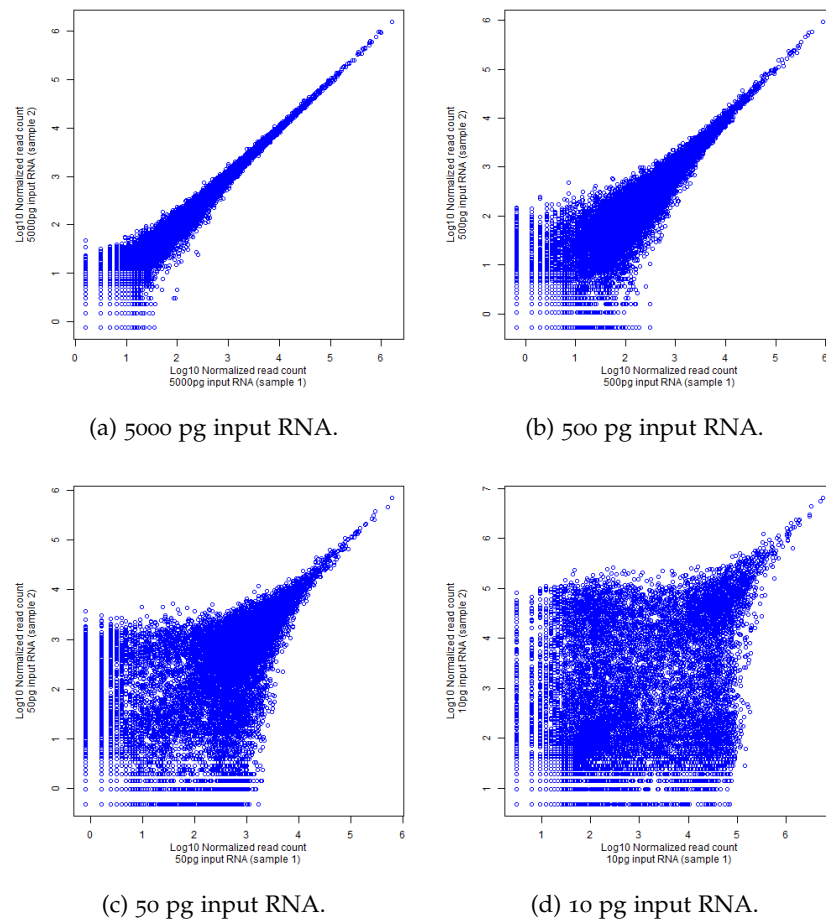


Figure 33: Dilution series of total *A. thaliana* RNA



The paragraphs above have shown that neither in-situ hybridization nor RNA-seq data are fully quantitative when the scale is lowered to the single cell level. To avoid problems linked to the noise level in the rest of this study, a solution was to binarize single cell datasets. However, binarization is not a trivial problem as discussed in the following section.

### 7.1.3 *Mapping back gene expression to a spatial reference*

Single cell RNA-seq captures a snapshot of the entire transcriptome of a given cell at a given point in time. However, to analyse cells from a complex tissue, current protocols require that the tissue be reduced to a suspension of single independent cells. This prevents the user from keeping track of any spatial information about the cells. Hence, when analysing single cell RNA-seq data from a complex tissue, back-mapping every cell to its original location becomes a crucial problem.

A recent paper published in *Cell* [34] describes a purely mathematical way to approximate the spatial organisation of sequenced single cells using a series of statistical methods to segregate and map single cells RNA-seq data obtained from mice otocysts onto a reference sphere. The method mainly based on Principal Components Analysis, allows them to reconstruct a “image” of the otocyst.

To push the method presented in [34] further, we could achieve back-mapping of the single cells to a different dataset with a spatial reference. This reference should consist of an independent assay where gene expression in the considered tissue is defined for enough genes at a spatially small enough resolution to find for each sequenced cell, if not its exact original location, at least a restricted region of the tissue from which the sequenced cell originated with a high probability.

Fortunately, in-situ hybridization assays provide exactly this type of data and I will present in the last section of this Chapter (7.2) a methodological proof-of-concept of this back-mapping in the brain of *P. dumerilii* with 72 sequenced single cells. However, before that, I will discuss the impact of the noise level in both in-situ hybridization and single cell RNA-seq assays on the quantitative nature of the resulting datasets.

## 7.2 PRELIMINARY RESULTS ON SINGLE CELL RNA-SEQ IN *p. dumerilii*'S BRAIN

### 7.2.1 Single cell RNA-seq in *Platynereis*' brain

A collaborations with Kaia Achim in the Arendt lab in EMBL provided us with a unique RNA-seq dataset of 72 single cells from *P. dumerilii*'s 48hpf developing brain.

Experimentally, the work consisted in setting up *P. dumerilii* batches, picking up 50-100 individuals at 48hpf. These were washed in Ca-Mg free sea water and incubated in a mixture of pronase which breaks extracellular matrix and thioglycolate (helps to break the chorion). After this treatment, the trunks and epispheres (brains) were separated. 40-60 epispheres were then picked out, transferred to Phosphate buffered saline (PBS) and then incubated for 1 minute in PBS containing collagenase to break more extracellular matrix. After two PBS washes, the cells were dissociated by pipetting up and down then washed again in 1 ml of PBS and concentrated by centrifuging (1 min, 1000 rpm). Cells were re-suspended in 20 microliters of PBS, of which 5 microliters could be loaded on the capture chip.

Fluidigm's C1 Single-Cell Auto Prep System instrument with the Fluidigm Single-Cell Auto Prep IFC chip optimized for 10-17 micron cells were used as shown in Figure 34. The reverse transcription was performed using Clontech SMARTer Ultra Low Input RNA Kit and for on-chip PCR the Clontech ADVANTAGE-2 PCR kit. Sequencing libraries were prepared using Nextera DNA Sample Preparation kit from Illumina.

With two chips and a capture rate of 65%, 72 libraries were sequenced including 11 cells from first chip. From the second chip 35 live single cells, 17 dead single cells, 3 wells containing 2 cells, one with 4 cells, and 3 unsure ones resulting in 72 raw reads files as shown in Table 1.

Of course those results do not include the spatial localization of the cells as the protocol requires the separation of the coherent tissue into a cell suspension. As a crucial point in any downstream analysis, being able to map back the single cells to their original location in the brain is required. To that end, I took advantage of the spatially

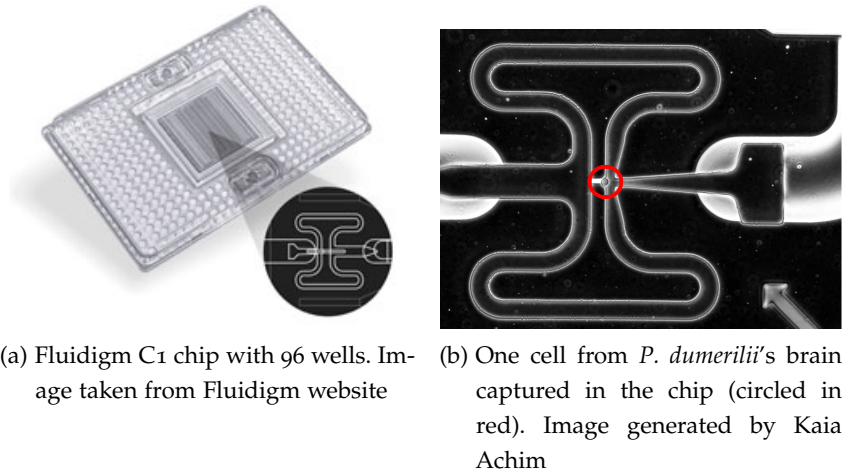


Figure 34: Microfluidics single cell sequencing with C1 chips.

|                           |     |
|---------------------------|-----|
| Chips used                | 2   |
| Capture rate              | 65% |
| Libraries sequenced       | 72  |
| Live single cells         | 38  |
| Dead single cells         | 15  |
| Debris + live single cell | 4   |
| Multiple cells            | 6   |
| Debris/unsure             | 9   |

Table 1: Results over two C1 chips. The experiments were conducted by Kaia Achim.

localized in-situ hybridization described in the previous section.

7.2.2 Mapping RNA-seq data back to PrimR in-situ hybridization assays

Firstly, Bowtie [69] was used to map the RNA-seq raw reads to a reference containing the sequences of the 86 reference genes composing the in-situ hybridization data. The resulting dataset comprises the number of reads mapped back to each of the 86 genes in the 72 cells sequenced (Figure 35).

In order to map back to the in-situ hybridization data, the chosen approach consisted of extracting the genes that were the most specifically expressed for each sequenced cell, before comparing this specific

fingerprint to the in-situ 3D data in order to isolate the regions of the brain where those specific genes are co-expressed.

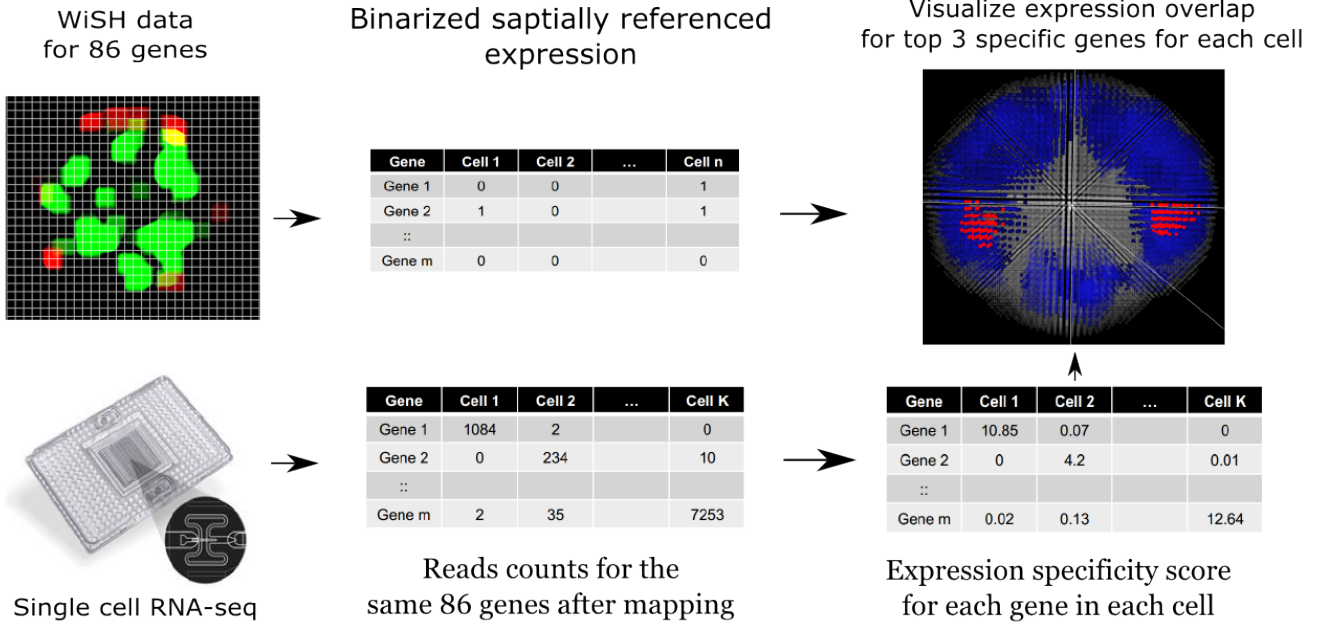


Figure 35: **Spatial back mapping of single cell RNA-seq.** The binarized in-situ hybridization data provides the spatial reference onto which the single cell results will be mapped. All the single cells sequenced are put together and a expression specificity score for each gene and each cell is computed. The mapping is realized using the top 3 or 4 most specific genes for each cell.

Given the set of 86 considered genes  $M$ , and the set of 72 cells  $C$ , with the read count matrix  $D$  of size  $M \times C$ , the expression specificity ratio  $r_{m,c}$  can be computed for each cell and each gene as :

$$r_{m,c} = \frac{D_{m,c}}{\frac{1}{\|C\|} \sum_{a \in C} D_{m,a}}$$

where  $\|C\| = 72$  is the number of cells considered. Subsequently, for each cell, the genes with the highest specificity scores can be determined. On the one hand, this method has the inconvenience of using the average expression level across all considered cells to compute the ratio  $r$ . This means that the ability to precisely infer the original location of each cell, in other words, the mapping quality will depend on the overall sequencing quality. Furthermore, this method's performance relies on the assumption that the data are in fact a collection of cells from different cell types. However, given the experimental protocol described above, this seems to be an acceptable hypothesis.

On the other hand, this mapping method has the advantage of not being sensible to technical noise in the RNA-seq protocol, providing the technical noise between cells remains at a constant level. This justifies the use of read counts in a quantitative way and not as binarized dataset.

The goals of this study were to validate the protocol used in order to obtain single cell RNA-seq results in *P. dumerilii*'s brain and to establish a methodological proof-of-concept on spatially mapping RNA-seq results onto in-situ hybridization data. I will present here a few examples of sequenced cells, their most specifically expressed genes and their resulting potential original location in the brain as well as the probable cell type they belong to.

In Table 2 are shown the most specific genes for four of the sequenced cells. For each cell, this list of genes can be used to visualize the areas within the brain where they are co-expressed according to the in-situ hybridization data. A snapshot of this visualization is shown on Figure 36. In every case, simply looking at the three most representative genes seems to allow a clear localization of the sequenced cells. Of course this mapping is not at the single cell level, but having an idea of the tissue every cell originated from is already a nice proof-of-concept.

From the most specific genes to each cell and their potential localization, it is possible to hypothesize, using previous biological studies, the cell type of each sequenced cell. As shown in Table 2, for cell "X2C911L" the most specifically expressed gene "Emx" has been used as a reference gene to localize the mushroom bodies, a hypothesis which is compatible with the co-expression of "CALM.R29" and "Dach" [120]. Cell "X2C521L" expresses Wnt8 very specifically, a gene shown to be linked to lateral brain development. Cell "X2C61L" can be easily classified as a developing neuron. Indeed both VACht (Vesicular acetylcholine transporter) and ChaT (Choline acetyltransferase) are genes coding for enzymes interacting with the neurotransmitter acetylcholine. Finally cell "X2C241S" displays the specific expression of the gene "Mitf", one of *P. dumerilii* most studied gene and expressed solely in the developing adult eyes [65, 46].

| X2C911L          | X2C521L                     | X2C61L                          | X2C241S     |
|------------------|-----------------------------|---------------------------------|-------------|
| Emx              | Wnt8                        | VACHT                           | Mitf        |
| CALM.R29         | HEN1-Y61                    | ChaT                            | Otx         |
| Dach             | Gsx                         | LYamide                         | Tolloid-Y68 |
| Mushroom<br>body | Developing<br>lateral brain | Differentiated<br>neural tissue | Adult eye   |

Table 2: Top 3 most specific genes for 4 sequenced cells and the potential tissue they belong to. The resulting localization of those four cells inferred from the in-situ hybridization data are shown in Figure 36.

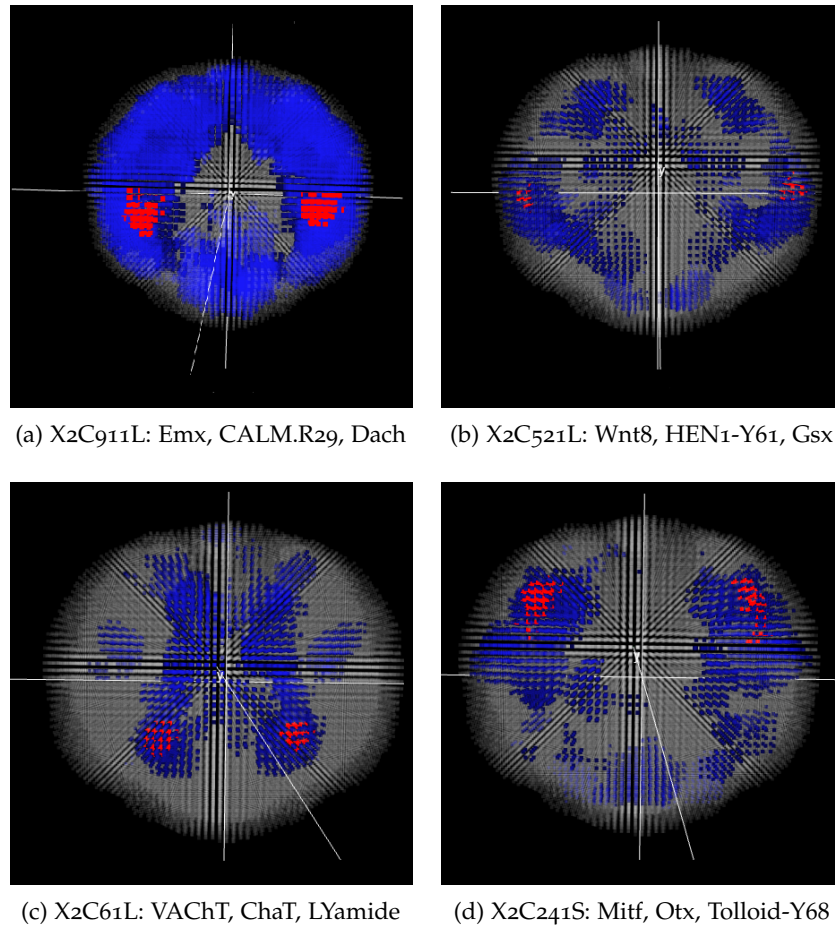


Figure 36: Regions defined by the expression overlap of the top 3 scoring genes in [120] binarized in-situ hybridization data. The red colour shows the co-expression of the three considered genes, the blue areas are those where one or more of the three considered genes are expressed but not all, in grey are the areas where none of the considered genes are expressed. The 4 figures are from an apical view with the dorsal side on top.

Overall, the results of this back-mapping method look very promising. Although at the time of writing, this work is still in progress in collaboration with Kaia Achim and Detlev Arendt, I have been able so far to map-back 27 of the 38 live single cells to a defined area of overlapping expression in the brain using the top 3 or 4 most specific genes. The cells were mapped to an average of 100 cubes defining a spatially coherent region.

I decided to check the probability of obtaining such a result by chance. To this end, I randomly generated 1000 “top 3” genes out of the 86 genes considered in the in-situ hybridization data. For each of these “top 3” randomly generated genes, I computed the number of cubes in the in-situ hybridization dataset where the 3 genes were co-expressed.

Subsequently, I compared the number of overlapping cubes obtained with this random process to the number of overlapping cubes obtained with the top 3 most specific genes from the 38 live single cells. The results are shown as boxplots in Figure 37. The left hand part of the plot shows the number of cubes obtained with the genes selected randomly. In this case the mean number of cubes is extremely close to zero. The right hand part of the plot shows the same results for the top 3 most specifically expressed genes of the 38 alive cells in the single cell RNA-seq dataset and clearly shows an enrichment on the non randomized side.



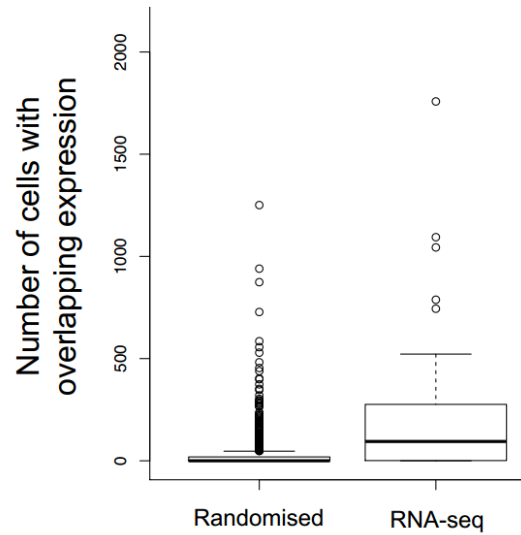


Figure 37: **Back-mapping by chance vs RNA-seq data.** This boxplot shows the number of “cubes” in which the top 3 genes overlap with randomly generated top 3 genes (left N=1000) and the top 3 genes obtained from the live single cells RNA-seq data(N=38).

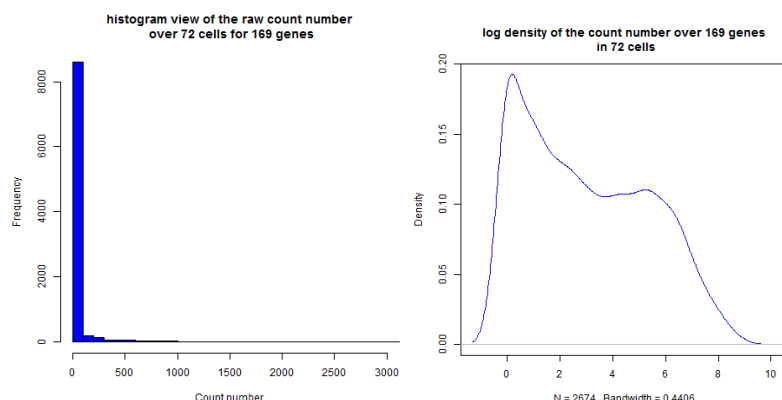
### 7.2.3 Binarizing whole transcriptomes

Even though the back-mapping method describe previously manages to deal with the noise in the data by looking at the most specifically expressed genes, as mentioned for in-situ hybridization, for other methods it could be useful to binarize the data. When dealing with whole transcriptomes, manually finding thresholds to binarize gene expression data is no longer a valid option due to the high number of genes considered. An automated method is thus required. I will discuss possible ways to binarize single cell RNA-seq data, presenting some results cells from the brain of *P. dumerilii*.

A naive approach would be to simply consider that as long as one RNA fragment mapped to a particular gene has been found in a cell, the gene is considered as expressed. Although such a method would be justifiable in the case of a perfect dataset, with no noise or errors, as discussed above 2.3 in the case of single cell RNA-seq the biases created by the mRNA capture rate are too high to rely simply on this method. Indeed, as a first approach on *P. dumerilii*'s dataset, we can see on Figure 38a that the value 0 represents a very dominant peak. The problem in that case is that for read counts of 0 it is dangerous to



consider the gene as non expressed when it could be lowly expressed.



(a) Histogram showing the frequencies of count values over 72 sequenced cells, with the fragments mapped to 169 genes. (b) Density plot for the count values over 0 in the single cell sequencing dataset

Figure 38: Thresholding RNA sequencing data for *P. dumerilii*. The RNA-seq reads are mapped for the 72 cells to 169 genes in the PrimR dataset. This choice was made because at the moment the full genome of *P. dumerilii* is not available for mapping the reads. I believe however that mapping to the entire genome would improve the results significantly.

Another option would be to find a global threshold over the complete dataset. The threshold,  $T > 0$ , would represent the count number of reads for a particular gene and a particular cell needed to consider the gene as expressed.  $T$  could be inferred from the count density over all the genes and all the cells. The expected result would be a 2 peak density with one peak corresponding to the non expressed count values, the second to expressed genes. The binary threshold would then be set between the first and second peak. Although more precise than the previous method, binarizing in such a manner may lead to numerous errors. Indeed, the underlying assumption behind this method is that all genes behave in a similar way. As Figure 38b shows, if a 2 peak behaviour is indeed present, the cut is not extremely clear and an important portion of count numbers actually fall in between the two peaks. This is due to the fact that all expressed genes are not expressed in the same way; some are expressed lowly, some highly. As a result, the density curve tends to flatten making this thresholding method, if better, still not 100% reliable.

The more suitable approach to this thresholding problem would be to compute one threshold per gene based on the density curve for every gene across all cells. However, considering the sparse nature of the count data, no significant results can be extracted with this method without a large enough number of sequenced cells. However, I believe that one threshold per gene would result in a big improvement over the previously mentioned thresholding methods providing sufficient number of data points per gene.

## CONCLUSIONS AND FUTURE WORK

---

### 8.1 CONCLUSIONS

#### 8.1.1 *Summary*

Throughout this thesis I have highlighted my main original contributions while presenting work from collaborators and other groups. I especially tried to convey how my work is part of a global effort to investigate spatially referenced gene expression patterns at the single cell level in complex tissues.

At the time of writing, the field of transcriptomics is undergoing a major revolution with new and evermore accurate sequencing methods requiring less and less starting materials. However, so far no gene expression assay has been able to achieve single cell resolution of the whole transcriptome while at the same time keeping the spatial organization of the tissue intact. On the one hand, in-situ hybridization can provide the spatial component but is not suitable for analysing all expressed genes. By contrast, single cell RNA-seq can provide with full single cell transcriptomes but no spatial reference.

The original contribution presented in Chapter 2 consist in the methods proposed to process and create a binary single cell expression dataset from the data generated by Tomer, alongside a non spatial way to cluster such data namely Hclust.

I have introduced in Chapter 3, what has been my main contribution to the field of transcriptomics during the time of my PhD. The HMRF clustering method I have adapted and extended and applied to the single cell gene expression data was chosen to answer the question of defining cell types from a bottom up approach at the scale of a very complex tissue where the number of cell types is unknown. The method's main ability is to account for the spatial characteristics of the sites in order to favour spatially smooth clustering results. Not only does this spatial smoothness help the visual downstream analysis, I also hypothesize that considering cells that are spatially near

one another to be more likely to belong to the same cell type as biologically relevant and potentially important for reducing the impact of experimental noise on the clustering results.

The HMRF method and specifically the impact of the spatial component on the clustering was evaluated and there were good indication that the approach improves the overall quality of clustering as demonstrated by the simulation study detailed in Chapter 4. Indeed, when compared to other non spatial clustering methods suitable for single cell gene expression datasets, the HMRF method performs consistently better. This in my opinion justifies the long work put into applying and extending this image analysis method to cluster a completely different type of data. The method was also assessed in term of computational burden, and although legends of the perfect clustering method may circulate, they are unfortunately unfounded. In the case of the HMRF, the price for the improved clustering quality compared to non spatial methods is paid with an exponentially increasing computing time with regard to the number of clusters, which limits this approach to datasets where the true number of clusters is less than 40 when clustering tens of thousands of sites for around a hundred genes.

Chapter 5 details the results when I applied the method to the spatially referenced single cell gene expression data from the brain of *Platynereis dumerilii*. The outcome was good and, in particular, I was able to localize well studied structures of the brain in order to validate the method biologically. Furthermore, I described how some clusters localized in poorly documented regions of the brain could be analysed by taking advantage of the model's final parameters. Indeed, I detailed how a specificity score for each gene and each cluster was computed in order to extract the most specific genes to each cluster. This allowed me to characterize a previously unstudied area of the brain and to formulate an hypothesis about the function of its cells.

In the last two Chapters, I have presented projects that were distinct but linked to the main contribution of my thesis. In particular in Chapter 6, I have presented a software tool that I have developed: "bioweb3D". This tool enables scientists who are not visualization experts to easily visualize 3 dimensional data in their web browser without the need to install any software on their computer or to send any data to a remote server. This tool, although fairly basic, has

been of great use for my own work and as a result multiple Figures (36, 27, 25) in this thesis are screen shots of “bioweb3D”. I was also pleased following publication of this tool in *BMC Bioinformatics* [98] to see a few users (around 20 each month) regularly visiting and using “bioweb3D”.

Finally in Chapter 7 I have presented a method developed to combine single cell RNA sequencing data with a spatially referenced in-situ hybridization dataset in order to create spatially referenced full transcriptomes by mapping single cell RNA-seq results onto a spatial gene expression library generated via in-situ hybridization assays. I have demonstrated the efficiency of the method on a preliminary dataset of single cell RNA-seq data in the brain of *P. dumerilii*. This is very recent, and an ongoing effort with my collaborators. However, so far I have been able to map around 75% of sequenced single cells to a restricted area in the brain defined by the in-situ data. At the time of writing, a manuscript to submit this work as a research paper is being prepared.

Even with these satisfactory results there is still work to be done for the clustering method and the single cell RNA-seq back mapping described in Chapter 2.

## 8.2 FUTURE WORK

### 8.2.1 Single cell RNA-seq back-mapping

The single cell back-mapping method detailed in Chapter 7 is the most recent work presented in this thesis. It is an ongoing project with new data available every month. Consequently, the results shown are preliminary and I expect that the method will be developed much further over the next few months. In particular, a combinatorial approach for selecting the most specific genes used in the spatial mapping is currently being investigated.

### 8.2.2 bioWeb3D

As mentioned in Chapter 6, I am fortunate enough to have a few active users using bioWeb3D regularly all over the world. Being open

source, the tool is maintained and updated by me and a few contributors.

Some ideas for future developments have been discussed recently including the ability to make the information layers “hoverable”. In other words, make each coloured cluster in the 3D representation reactive to the mouse passing over and displaying information/statistics about the hovered entity.

Other suggested developments include the ability to save the data on the server temporarily (with a fixed lifespan before the server automatically deletes it) which would allow users to share visualization via a simple URL. This would be an interesting area to explore even though I always developed bioWeb3D with the users’ data security in mind. In that regard, not storing or even receiving any data server side was the absolute insurance of data confidentiality.

Finally the idea of allowing surfaces, textures and sprites in bioWeb3D has been suggested. This of course would make the tool much more complete and allow far more advanced visualization. It would also make it more complex which is in contradiction with the starting idea which was to create a 3D visualization tool for non expert users that wanted a quick way to have a 3D representation of their data without having to go through a large user manual.

### 8.2.3 HMRF future developments

The main areas where the HMRF method needs to be improved is that of adapting the emission model described in Chapter 3 to whole transcriptomes and quantitative gene expression data. Indeed, as explained in Chapter 2, my work has been focused on clustering binarized data for 89 key developmental genes.

With a hypothetical dataset in the brain of *P. dumerilii* containing the quantitative expression levels for whole transcriptome (more than 10.000 genes) of each cell, how would such a dataset impact the theoretical framework described in Chapter 3?

The quantitative aspect of the data would require a modification of the emission model. While a Bernoulli distribution for each gene in

each cluster is suited for binarized data, for quantitative data it would be sensible to use Poisson or negative binomial distribution. Indeed, these are the mainly used approaches to model gene expression measured via RNA-seq in the literature [77, 1]. Quantitative data from gene expression assays could follow technological improvements in to reduce the noise level but it would also be interesting to model the technical noise in order to isolate the quantitative signal [14].

Furthermore, the fact that instead of a few selected genes, cells have to be clustered considering their whole transcriptome represents a theoretical issue because genes are not independently expressed. Indeed, as explained in the Introduction (1), gene expression is a highly regulated mechanism exhibiting high inter-dependence between genes. More particularly, some expressed genes code for regulatory factors that will influence the level of expression of other genes. This inter-dependency is in plain contradiction with the conditional independence hypothesis for gene expression used in the HMRF model (as described in Chapter 3).

This issue may be resolved by developing methods to analyse whole transcriptomes upstream of the clustering to automatically select an ensemble of genes that are at the same time independent and extremely representative of the overall expression patterns in the studied tissue.

Another possible way to deal with this problem would be to try to extend Markov random fields without the conditional independence hypothesis.

Such an approach may prove unnecessary, as it is possible that the errors introduced by some genes' inter-dependence will represent a negligible bias compared to the signal brought by thousands of genes. Simulation studies may be able to decide this issue.

#### 8.2.4 *Final words*

The different parts of the work presented in this thesis will hopefully be used in different contexts than the brain of *P. dumerilii*. In particular the HMRF clustering method may prove useful to study intra-tumour heterogeneity, a crucial area of research to avoid cancer

resurgence [82, 79, 7], when single cell spatially referenced data is available.

I tried to present throughout this thesis the work realized during these four years in a scientifically relevant way and not by following the time line of the projects which was mainly dependent upon data availability. I hope I demonstrated how this work answered consistently some of the questions linked to the spatial context of single cell gene expression assays and why it is important to take it into account.



## Part II

### APPENDIX



## INPUT FILE FORMATS FOR BIOWEB<sub>3D</sub>

---

### A.1 DATASET FILE SPECIFICATION

When the user adds a new *Dataset* file, a new Dataset section is created in the “Data” panel of the application. Each dataset file contains one dataset.

#### A.1.1 JSON format

The *dataset* file should have a root object called “dataset” which contains:

- The “name” property of the dataset (*e.g.*, “my dataset”);
- The “chain” parameter, which should be set to *true* if the points are connected (the default value is *false*) - the data will be considered sequentially, with each point connected by a solid line to the previous and next point according to its order in the dataset file;
- The “points” property, which is a two dimensional array representing a list of (x,y,z) vectors that define the co-ordinates of the points.

Listing 3 is an example of a minimal 3 points dataset file.

#### A.1.2 XML format

The *dataset* XML format used is very similar to the previously defined JSON format. The file must have a root object called “<dataset>” which contains:

- The “<name>” property of the dataset (*e.g.*, “my dataset”);
- The “<chain>” parameter, which should be set to *true* if the points are linked (the default value is *false*) - the data will be considered sequentially, with each point connected by a solid

Listing 3: Json dataset file

```
{ "dataset" : {  
  "name" : "my superb dataset",  
  "chain" : true,  
  "points" :  
    [  
      [  
        0.5,  
        100,  
        -50.5  
      ],  
      [  
        200,  
        10,  
        0.0  
      ],  
      [  
        3,  
        250.15,  
        15  
      ]  
    ]  
  }  
}
```

Listing 4: XML dataset file

```

<?xml version="1.0" ?>
<dataset>
  <name>my superb dataset</name>
  <chain>true</chain>
  <points>
    <point>
      <x>0.5</x>
      <y>100</y>
      <z>-50.5</z>
    </point>

    <point>
      <x>200</x>
      <y>10</y>
      <z>0.0</z>
    </point>

    <point>
      <x>3</x>
      <y>250.15</y>
      <z>15</z>
    </point>
  </points>
</dataset>

```

line to the previous and next point according to its order in the dataset file;

- The “<points>” property, which contains all the single “<point>” elements that define the dataset. Each “<point>” has three properties to define its spatial location, namely “<x>”, “<y>” and “<z>”.

Listing 4 contains the same minimal dataset as Listing 3 but formatted in XML.

### A.1.3 CSV format

Each line represents a point and the three coordinates on each line must be separated by “comma” characters.

As an example, listing 5 carries the same information as the JSON file

Listing 5: CSV dataset file

```
0.5,100,-50.5
200,10,0.0
3,250.15,15
```

in Listing 3. We note that although the spatial information remains the same it is not possible to set a name or to connect the points within a CSV file input.

## A.2 INFORMATION LAYER FILE SPECIFICATION

The *Information layer* file contains information about the points described in the Dataset file. The information in this file has to be given in the same order as the points defined in the Dataset file.

### A.2.1 JSON format

The *information layer* files must have a root element named “information”. Since one information file can define multiple information sets, the structure below “information” is a list. Each element of the list is structured as follows:

- The “name” property (optional);
- The “numClass” property, which indicates the number of different classes the data will be assigned to;
- The “labels” property, which defines a list of names for the “numClass” classes previously defined (optional);
- The “values” property, which defines the class of each point in the dataset. As points do not have single IDs, this property must be in the same order and have the same length as the points defined in the *dataset* file.

For example coming back to the 3 points defined in Listing 3, two information layers could correspond to:

- one clustering algorithm that puts the first two points together in class one and the third point alone in a second class
- a second clustering algorithm that puts each point in a separate class

Listing 6: JSON information layer file

```

{ "information" :
  [
    {
      "name": "clustering algo 1",
      "numClass": "2",
      "labels" : [
        "Category 1",
        "Category 2"
      ],
      "values": [
        1,
        1,
        2
      ]
    },
    {
      "name": "clustering algo 2",
      "numClass": "3",
      "values": [
        1,
        2,
        3
      ]
    }
  ]
}

```

In this case the Information layer file would look like Listing 6.

#### A.2.2 XML format

The *information layer* XML format used is very similar to the previously defined JSON format. The *information layer* files must have a root element named "<information>". Since one information file can define multiple information sets, the structure below "<information>" is a list of "<set>" elements. Each "<set>" element is structured as follows:

- The "<name>" property (optional);
- The "<numClass>" property, which indicates the number of different classes the data will be assigned to;

Listing 7: XML information layer file

```

<?xml version="1.0" ?>
<information>
  <set>
    <name>clustering algo 1</name>
    <numClass>2</numClass>
    <labels>
      <label>Category 1</label>
      <label>Category 2</label>
    </labels>
    <values>
      <value>1</value>
      <value>1</value>
      <value>2</value>
    </values>
  </set>
  <set>
    <name>clustering algo 2</name>
    <numClass>3</numClass>
    <values>
      <value>1</value>
      <value>2</value>
      <value>3</value>
    </values>
  </set>
</information>

```

- The “<labels>” property, which contains as many individual “<label>” properties as the number of different classes. Each “<label>” defines the names for one class (optional);
- The “<values>” property, which contains all the single “<value>” properties, each one defining the class of each point in the dataset. As points do not have single IDs, the “<value>” properties must be in the same order and have the same length as the points defined in the *dataset* file.

Listing 7, carries the exact same information as Listing 6.

**CSV FORMAT** Each column represents the class to which a point belongs. The separation character between columns must be a “comma”. Listing 8, carries the same information as Listing 6. Note that it is not



Listing 8: CSV information layer file

```
1,1  
1,2  
2,3
```

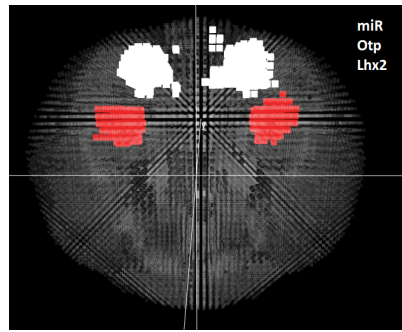
possible to use the “labels” or “name” properties available in Listing [6](#) within a CSV information layer file.



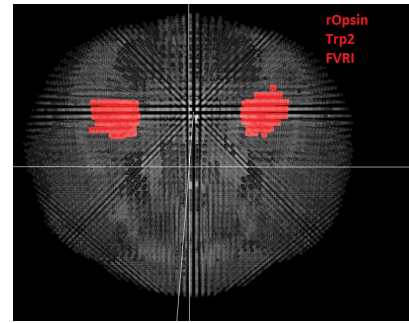
## FULL LIST OF THE CLUSTERS OBTAINED WITH THE HMRF METHOD

---

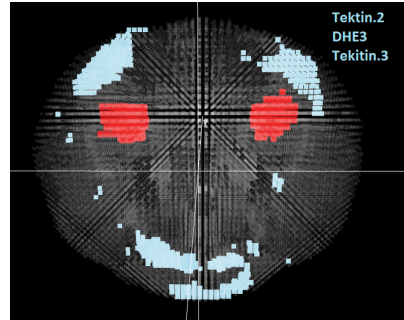
This chapter provides a quick glance over the 33 clusters generated by the HMRF method (see Chapters, [3](#) and [5](#)) in the brain of *P. dumerilii* using the 86 genes selected from the in-situ hybridization data generated by Raju Tomer. Each cluster is presented from an apical point of view alongside the adult eyes (red cluster) for spatial reference. On each images the 3 top scoring (see Chapter [5](#) for an explanation of the scoring process) genes are indicated.



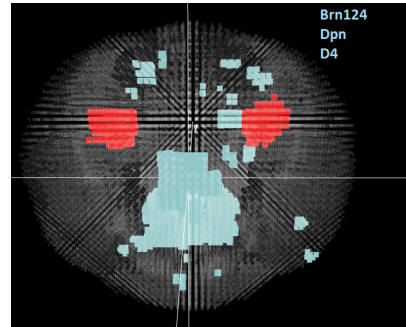
(i) Cluster 1



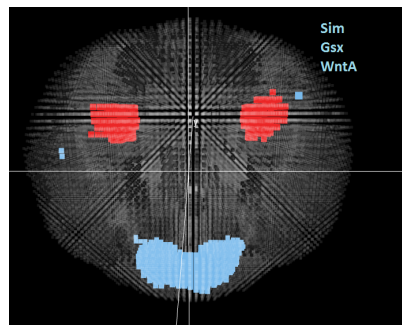
(ii) Cluster 2



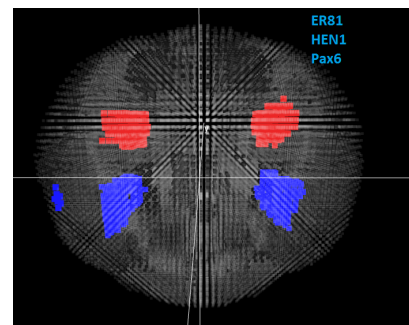
(iii) Cluster 3



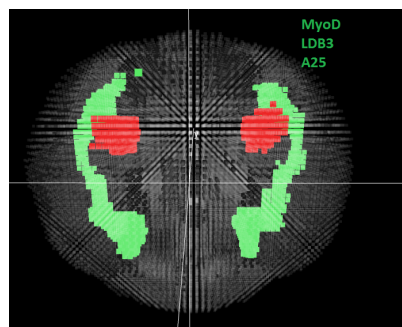
(iv) Cluster 4



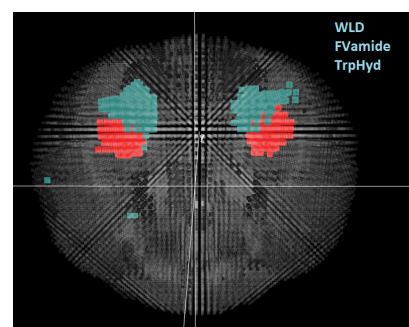
(v) Cluster 5



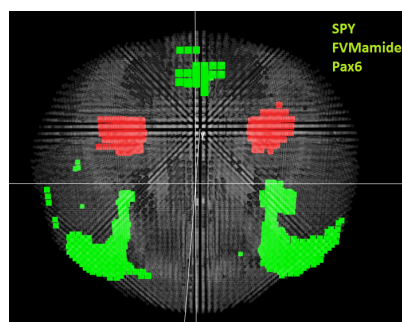
(vi) Cluster 6



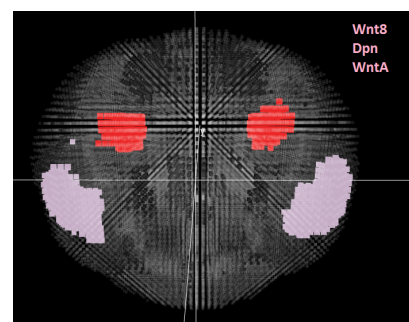
(vii) Cluster 7



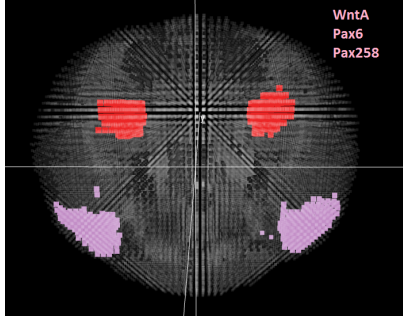
(viii) Cluster 8



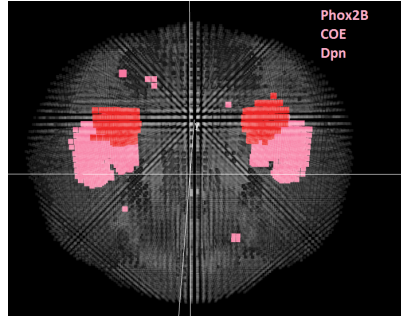
(ix) Cluster 9



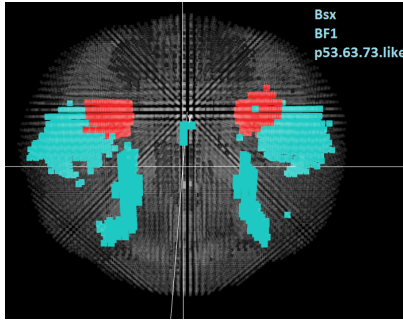
(x) Cluster 10



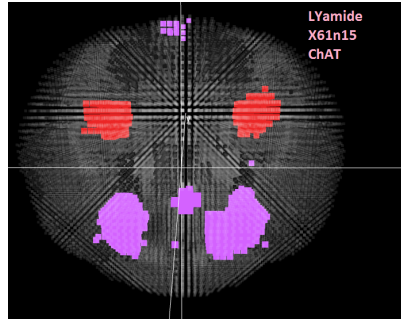
(xi) Cluster 11



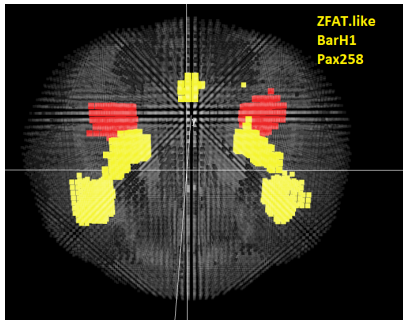
(xii) Cluster 12



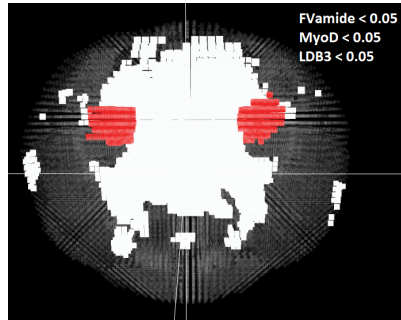
(xiii) Cluster 13



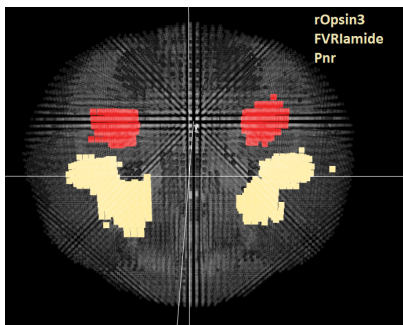
(xiv) Cluster 14



(xv) Cluster 15



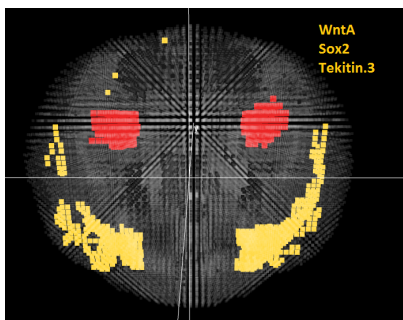
(xvi) Cluster 16



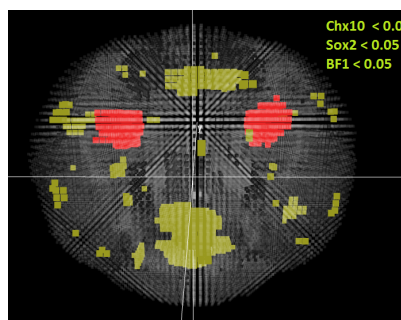
(xvii) Cluster 17



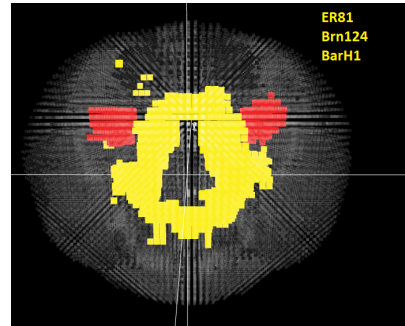
(xviii) Cluster 18



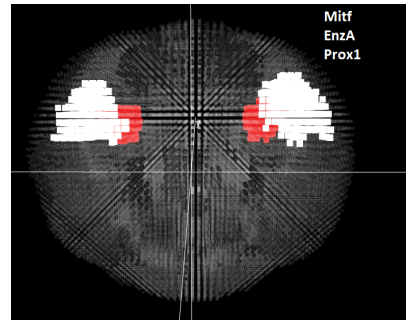
(xix) Cluster 19



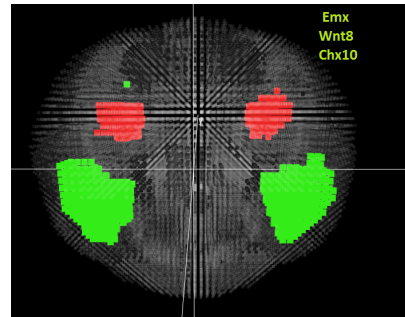
(xx) Cluster 20



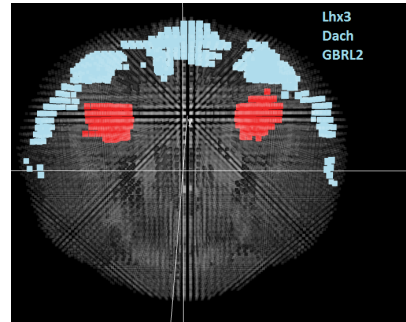
(xxi) Cluster 21



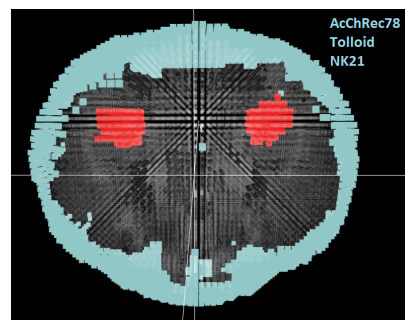
(xxii) Cluster 22



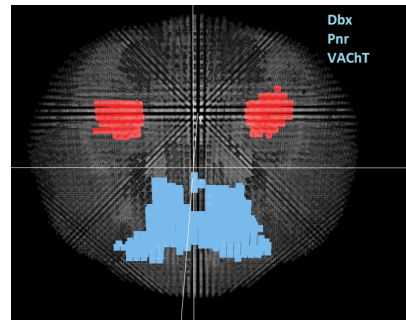
(xxiii) Cluster 23



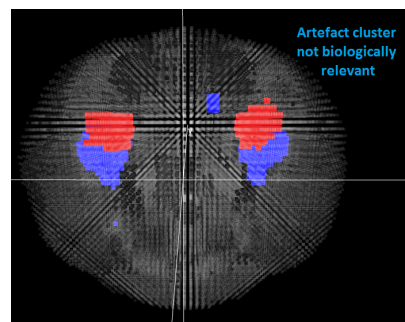
(xxiv) Cluster 24



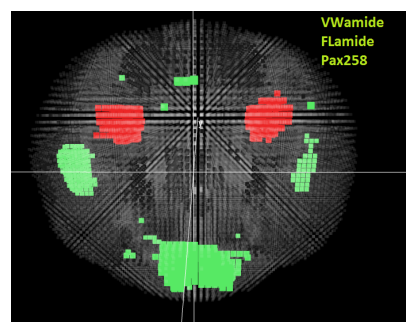
(xxv) Cluster 25



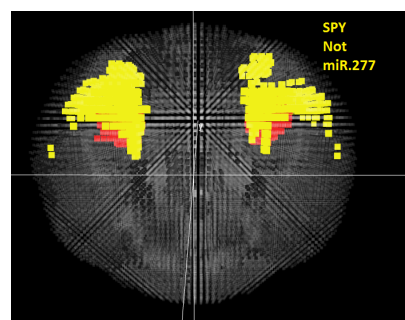
(xxvi) Cluster 26



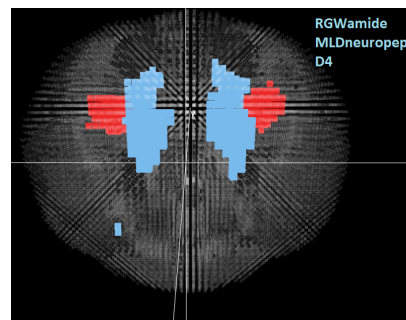
(xxvii) Cluster 27



(xxviii) Cluster 28



(xxix) Cluster 29



(xxx) Cluster 30



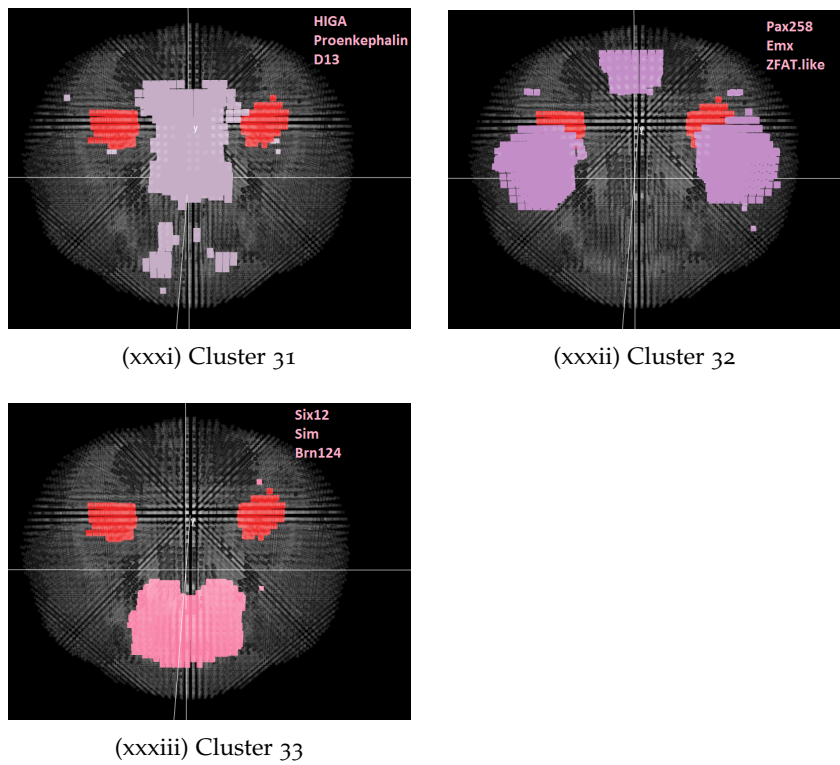


Figure 35: 33 clusters generated by the HMRF method





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